

# **Tutorial, Mechanics; Historical & Scientific Context re Formal Logic, AI, and Logic Machines; And The Terrific Triad**

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Troy, New York 12180 USA

*Intermediate Formal Logic & AI (IFLAI2)*  
8/31/2023



**In the News ...**



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# WHAT IS SCHOOL FOR?



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The past two and a half years have brought disruption after disruption to America's K-12 schools. It's been ... stressful. But these disturbances in our education equilibrium have also given us a chance to step back and ask, "What is school for?"

---

[A]

**Everyone**

by Anya Kamenetz

[B]

**Economic Mobility**

by John Friedman

[C]

**Making Citizens**

by Heather McGhee  
and Victor Ray

[D]

**Care**

by Jessica Grose

[E]

**Wasting Time**

by Bryan Caplan

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**Learning to Read**  
by Emily Hanford

[G]

**Connecting to Nature**  
by Nicolette Sowder

[H]

**Merit**  
by Asra Nomani

[I]

**Hope**  
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[J]

**Parent Activism**  
A conversation with  
public school parents

[K]

**Teaching**  
A conversation with  
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**Us**  
by Fremont High  
School Students

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*Where's for  
becoming a  
logical person,  
and for  
building cool,  
crucial things?*

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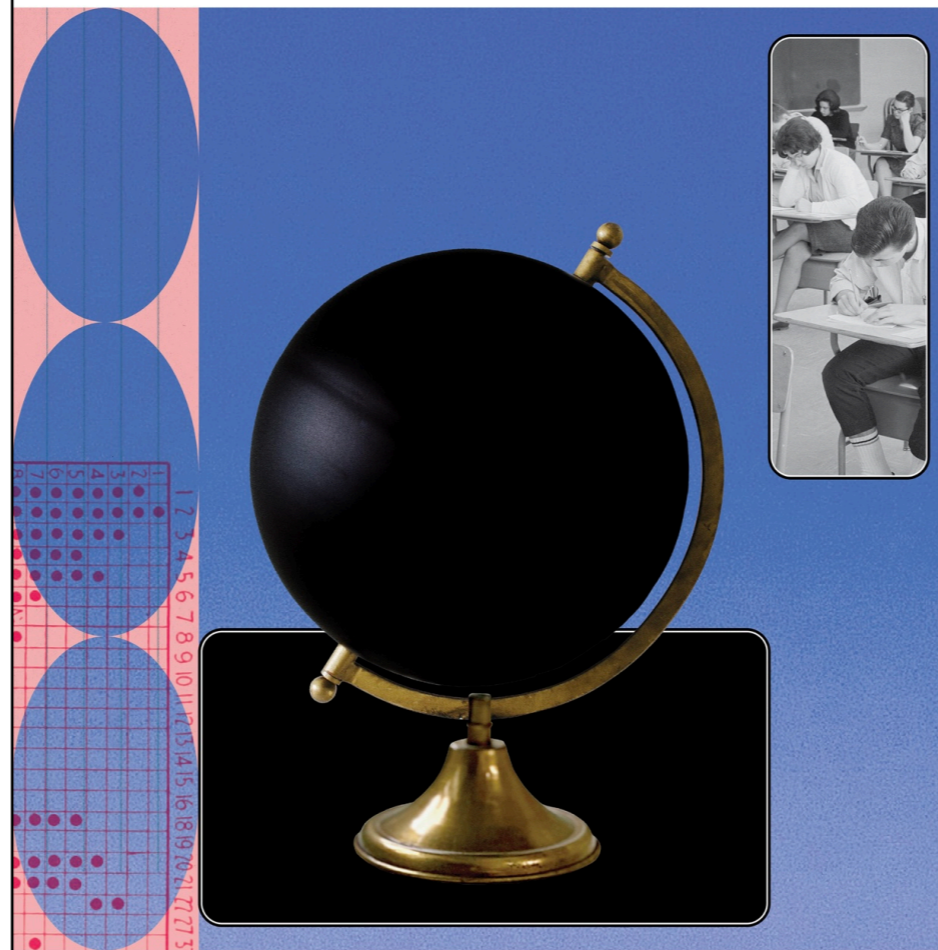


**OPINION**  
GUEST ESSAY

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# School Is for Wasting Time and Money

Sept. 1, 2022





**By Bryan Caplan**

Dr. Caplan is a professor of economics at George Mason University and the author of “The Case Against Education.”

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**Sign Up for the Education Briefing** From preschool to grad school, get the latest U.S. education news. [Get it sent to your inbox.](#)

I have deep doubts about the intellectual and social value of schooling. My argument in a nutshell: First, everyone leaves school eventually. Second, most of what you learn in school doesn't matter after graduation. Third, human beings soon forget knowledge they rarely use.

Strangely, these very doubts imply that the educational costs of the coronavirus pandemic are already behind us. Forced optimism notwithstanding, the remote schooling that millions of students endured during the pandemic looks like a pedagogical disaster. Some researchers found that being in Zoom school was about equivalent to [not being in school at all](#). Others simply found that test scores [rose much less](#) than they normally would.

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Is this argument sound (ie formally valid, with true or at least highly plausible premises)?

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But given my doubts about the value of school, I figure that most of the learning students lost in Zoom school is learning they would have lost by early adulthood even if schools had remained open. My claim is not that in the long run remote learning is almost as good as in-person learning. My claim is that in the long run in-person learning is almost as bad as remote learning.

How do we know all this? My work focuses on tests of adult knowledge — what adults retain after graduation. The general pattern is that grown-ups have [shockingly little academic knowledge](#). College graduates know about what you'd expect high school graduates to know; high school graduates know about what you'd expect dropouts to know; dropouts know next to nothing. This doesn't mean that these students *never* knew more; it just means that only a tiny fraction of what they learn durably stays in their heads.





**Some Mechanics ...**

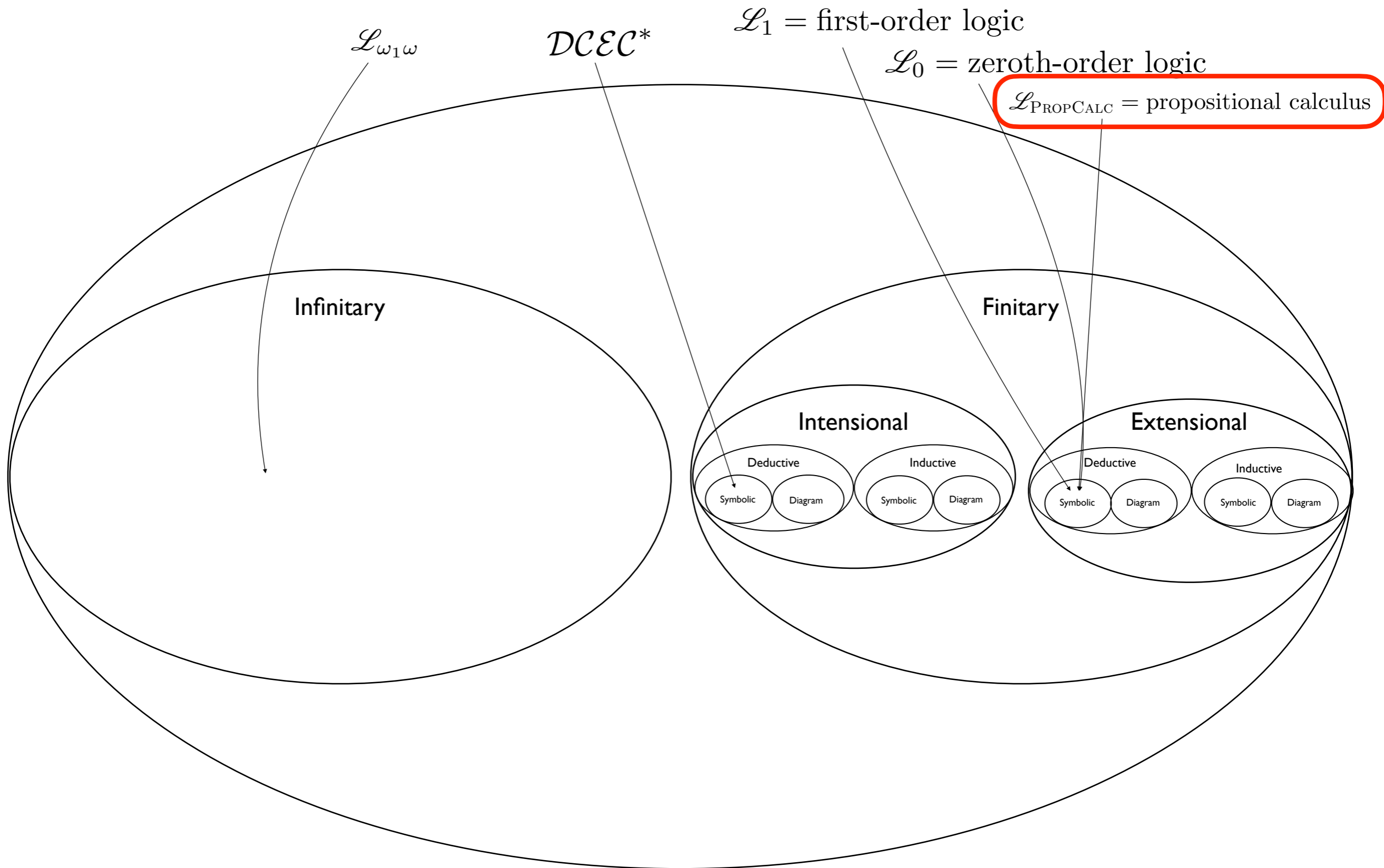
**Some Mechanics ...**

# Some Mechanics ...

IFLAI2 web page is the anchor!

Be all set for class on Sept 7  
in the HyperGrader<sup>®</sup>  
platform ... Glimpse now of  
Coming Review of  
The Three Basic Extensional  
Logics ( $\mathcal{L}_{PC}$   $\mathcal{L}_1$   $\mathcal{L}_2$ ) ...

# The Universe of Logics





A criminal genius nearly a match for Sherlock Holmes (Do you recognize the Dr?) has built a massive hydrogen bomb, and life on Earth is hanging in the balance, hinging on whether you make the logical prediction. Dr M gives you a sporting chance to: make the right prediction, snip or not snip accordingly, and prove that you're right ...





A **criminal genius** nearly a match for Sherlock Holmes  
(Do you recognize the Dr?)





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If one of the following assertions is true then so is the other:

(1) If the red wire runs to the bomb, then the blue wire runs to the bomb; and, if the blue wire runs to the bomb, then the red wire runs to the bomb.

(2) The red wire runs to the bomb.

Given this perfectly reliable clue from Dr Moriarty, if either wire is more likely to run to the bomb, that wire *does* run to the bomb, and the bomb is ticking, with only a minute left! If both are equiprobable, neither runs to the bomb, and you are powerless. Make your prediction as to what will happen when a wire is snipped, and then make your selected snip by clicking on the wire you want to snip! Or leave well enough alone!



Red more likely.

Blue more likely.

Equiprobable.

If one of the following assertions is true then so is the other:

(1) If the red wire runs to the bomb, then the blue wire runs to the bomb; and, if the blue wire runs to the bomb, then the red wire runs to the bomb.

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If one of the following assertions is true then so is the other:

(1) **(and (if redruns blueruns) (if blueruns redruns))** <sup>ue</sup> wire runs to the bomb; and, if the blue wire runs to the bomb, then the red wire runs to the bomb.

(2) **redruns** wire runs to the bomb.

Given this perfectly reliable clue from Dr Moriarty, if either wire is more likely to run to the bomb, that wire *does* run to the bomb, and the bomb is ticking, with only a minute left! If both are equiprobable, neither runs to the bomb, and you are powerless. Make your prediction as to what will happen when a wire is snipped, and then make your selected snip by clicking on the wire you want to snip! Or leave well enough alone!

---

---

Red more likely.

Blue more likely.

Equiprobable.

```
(and (if (and (if redruns blueruns) (if blueruns redruns)) redruns)
      (if redruns (if (and (if redruns blueruns) (if blueruns redruns)) redruns)))
```

(1) `(and (if redruns blueruns) (if blueruns redruns))` blue wire runs to the bomb; and, if the blue wire runs to the bomb, then the red wire runs to the bomb.

(2) `redruns` blue wire runs to the bomb.

Given this perfectly reliable clue from Dr Moriarty, if either wire is more likely to run to the bomb, that wire *does* run to the bomb, and the bomb is ticking, with only a minute left! If both are equiprobable, neither runs to the bomb, and you are powerless. Make your prediction as to what will happen when a wire is snipped, and then make your selected snip by clicking on the wire you want to snip! Or leave well enough alone!



Red more likely.

Blue more likely.

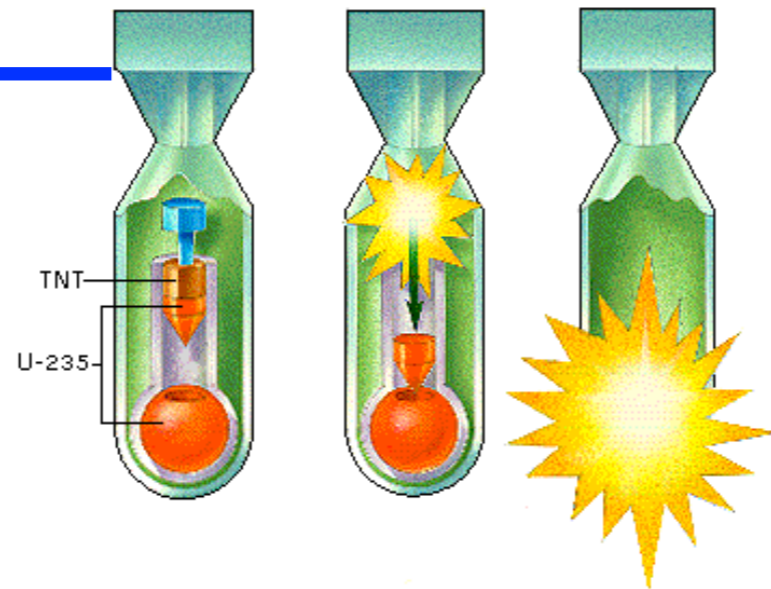
Equiprobable.

\_\_\_\_\_

\_\_\_\_\_

Snip

---



Life  
on  
Earth  
has  
ended

•

advance one more  
slide to see a proof  
that you indeed made  
an irrational  
decision...

**Proposition:** The blue wire is more likely!

**Proof:** (1) can be treated as a biconditional, obviously ( $R \iff B$ ).

There are two top-level cases to consider: (1) and (2) are both true; or both are false. In the case where they are both true, it's trivial to deduce both R and B. So far, then, R and B are equiprobable. What happens in the case where (1) and (2) are both false? We immediately have  $\sim R$  from the denial of (2). But a biconditional is true just in case both sides are true, or both sides are false; so we have two sub-cases to consider.

Consider first the case where R is true and B is false. We have an immediate contradiction in this sub-case, so both R and B can both be deduced here, and we have not yet departed from equiprobable. So what about the case where R is false and B is true? The falsity of R is not new information (we already have that from the denial of (2)), but we can still derive B. Hence the blue wire is more likely. **QED**

\_\_\_\_\_

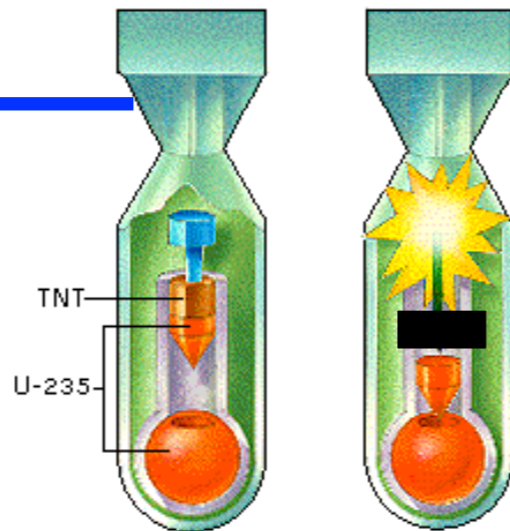
\_\_\_\_\_



---

Snip

---



Life on  
Earth  
is  
saved!

*if you can now hand Dr  
M a proof that your  
decision was the rational  
one!*

Advance one more slide  
to see a proof from  
Bringsjord that yours  
had better match up to

...

**Proposition:** The blue wire is more likely!

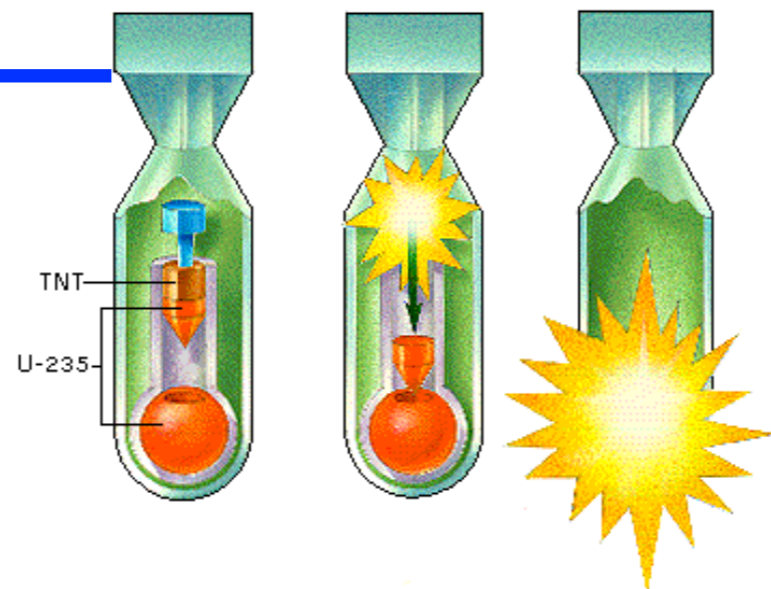
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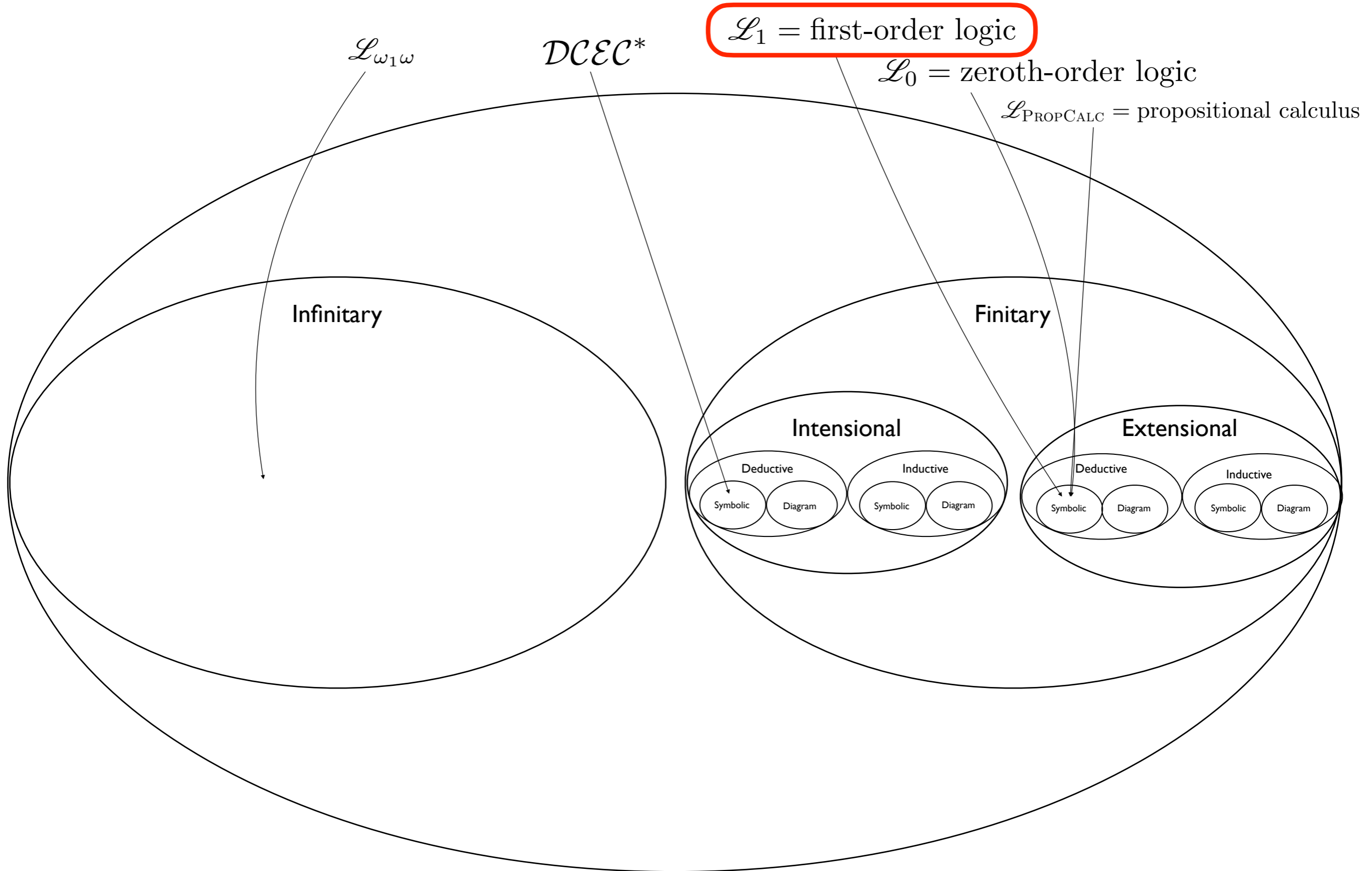
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STOP

**Logicize and solve in your  
HyperSlate® Library by  
Sept 7 class ...**

# The Universe of Logics



# Special Llamas Disjunction

There's a thing such that it's both a llama and a non-llama;

or

there's a thing such that if it's a llama, everything is a llama;

or

there's a thing such that every llama is a non-llama.



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Is this disjunction TRUE, FALSE, or UNKNOWN?

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(Can you (later, if catching up) build a formal, verifying proof in HyperSlate®?)

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# Background Claim

$\mathcal{R}$  Humans, at least neurobiologically normal ones, are fundamentally rational, where rationality is constituted by certain logico-mathematically based reasoning and decision-making in response to real-world stimuli, including stimuli given in the form of focused tests; but mere animals are not fundamentally rational, since, *contra* Darwin, their minds are fundamentally qualitatively inferior to the human mind. As to whether computing machines/robots are fundamentally rational, the answer is “No.” For starters, if  $x$  can’t read, write, and create,  $x$  can’t be rational; computing machines/robots can neither read nor write nor create; ergo, they aren’t fundamentally rational.

**To infinity and beyond! — routinely**

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quantification  
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**abstract-and-valid inference schemata**

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**To infinity and beyond! — routinely**

abstract-and-valid inference schemata

quantification

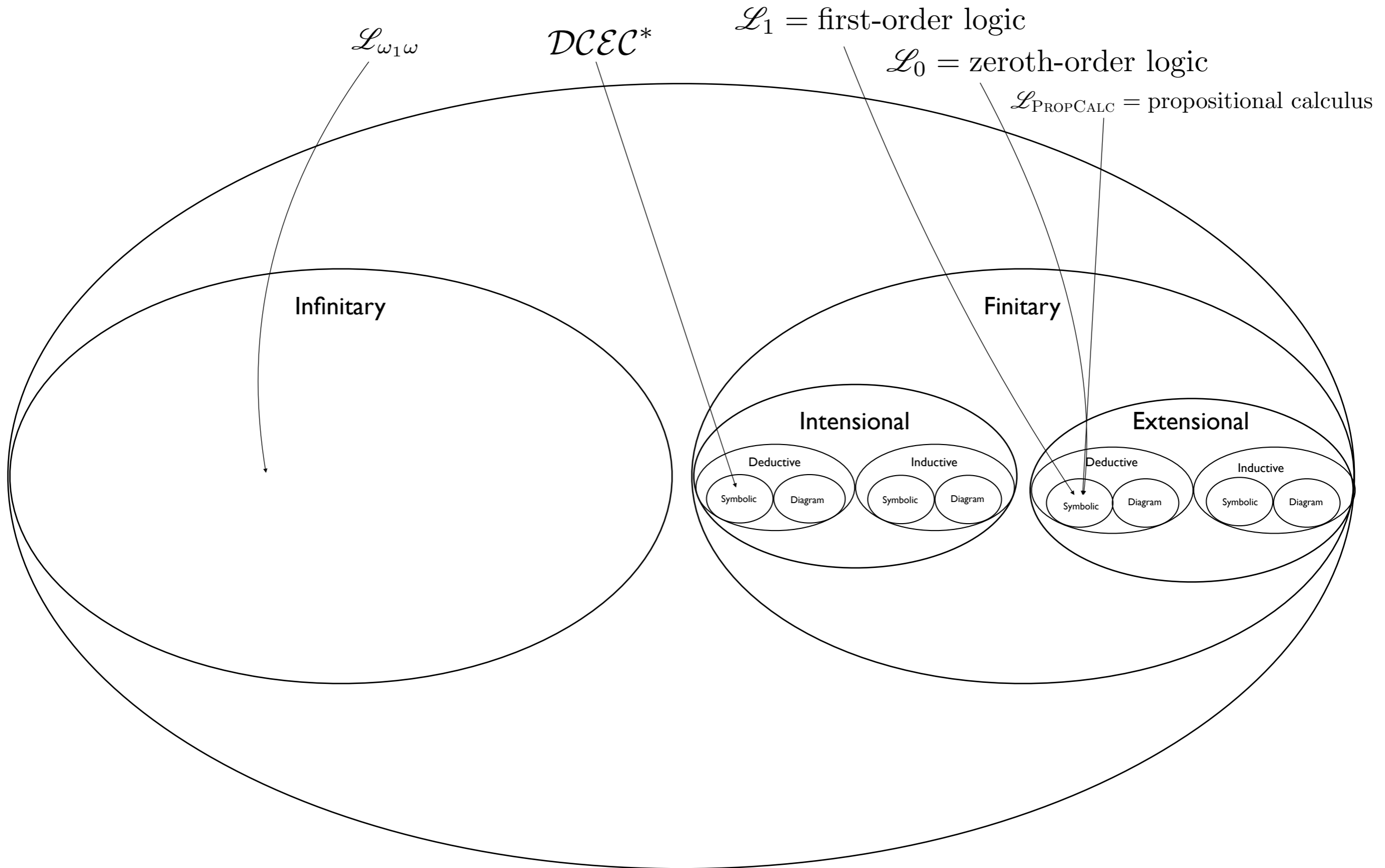
intensional reasoning

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To infinity and beyond! — routinely

# The Universe of Logics



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$\mathcal{L}_2$  = second-order logic

$\mathcal{L}_1$  = first-order logic

$\mathcal{L}_0$  = zeroth-order logic

$\mathcal{L}_{\text{PROPCALC}}$  = propositional calculus

$\mathcal{L}_{\omega_1\omega}$

$\mathcal{DCEC}^*$

Infinitary

Finitary

Intensional

Extensional

Deductive

Inductive

Deductive

Inductive

Symbolic

Diagram

Symbolic

Diagram

Symbolic

Diagram

Symbolic

Diagram

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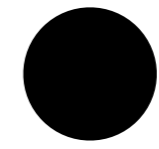
DoubleMindedMan

(Sept 11)

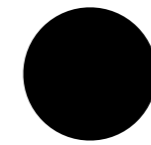
# An Anchoring Logic- and-AI Timeline ...







2023



2023

*IFLA12 @ RPI*

# DCEC\*

## Syntax

$S ::=$  Object | Agent | Self  $\square$  Agent | ActionType | Action  $\sqsubseteq$  Event |  
Moment | Boolean | Fluent | Numeric

$action$  : Agent  $\times$  ActionType  $\rightarrow$  Action

$initially$  : Fluent  $\rightarrow$  Boolean

$holds$  : Fluent  $\times$  Moment  $\rightarrow$  Boolean

$happens$  : Event  $\times$  Moment  $\rightarrow$  Boolean

$clipped$  : Moment  $\times$  Fluent  $\times$  Moment  $\rightarrow$  Boolean

$f ::=$   $initiates$  : Event  $\times$  Fluent  $\times$  Moment  $\rightarrow$  Boolean

$terminates$  : Event  $\times$  Fluent  $\times$  Moment  $\rightarrow$  Boolean

$prior$  : Moment  $\times$  Moment  $\rightarrow$  Boolean

$interval$  : Moment  $\times$  Boolean

$*$  : Agent  $\rightarrow$  Self

$payoff$  : Agent  $\times$  ActionType  $\times$  Moment  $\rightarrow$  Numeric

$t ::= x : S \mid c : S \mid f(t_1, \dots, t_n)$

$t$  : Boolean |  $\neg\phi$  |  $\phi \wedge \psi$  |  $\phi \vee \psi$  |

$\mathbf{P}(a, t, \phi) \mid \mathbf{K}(a, t, \phi) \mid \mathbf{C}(t, \phi) \mid \mathbf{S}(a, b, t, \phi) \mid \mathbf{S}(a, t, \phi)$

$\phi ::=$   $\mathbf{B}(a, t, \phi) \mid \mathbf{D}(a, t, holds(f, t')) \mid \mathbf{I}(a, t, happens(action(a^*, \alpha), t'))$

$\mathbf{O}(a, t, \phi, happens(action(a^*, \alpha), t'))$

## Rules of Inference

$\frac{}{\mathbf{C}(t, \mathbf{P}(a, t, \phi) \rightarrow \mathbf{K}(a, t, \phi))} [R_1] \quad \frac{}{\mathbf{C}(t, \mathbf{K}(a, t, \phi) \rightarrow \mathbf{B}(a, t, \phi))} [R_2]$

$\frac{\mathbf{C}(t, \phi) \ t \leq t_1 \dots t \leq t_n}{\mathbf{K}(a_1, t_1, \dots, \mathbf{K}(a_n, t_n, \phi) \dots)} [R_3] \quad \frac{\mathbf{K}(a, t, \phi)}{\phi} [R_4]$

$\frac{}{\mathbf{C}(t, \mathbf{K}(a, t_1, \phi_1 \rightarrow \phi_2)) \rightarrow \mathbf{K}(a, t_2, \phi_1) \rightarrow \mathbf{K}(a, t_3, \phi_2)} [R_5]$

$\frac{}{\mathbf{C}(t, \mathbf{B}(a, t_1, \phi_1 \rightarrow \phi_2)) \rightarrow \mathbf{B}(a, t_2, \phi_1) \rightarrow \mathbf{B}(a, t_3, \phi_2)} [R_6]$

$\frac{}{\mathbf{C}(t, \mathbf{C}(t_1, \phi_1 \rightarrow \phi_2)) \rightarrow \mathbf{C}(t_2, \phi_1) \rightarrow \mathbf{C}(t_3, \phi_2)} [R_7]$

$\frac{}{\mathbf{C}(t, \forall x. \phi \rightarrow \phi[x \rightarrow t])} [R_8] \quad \frac{}{\mathbf{C}(t, \phi_1 \leftrightarrow \phi_2 \rightarrow \neg\phi_2 \rightarrow \neg\phi_1)} [R_9]$

$\frac{}{\mathbf{C}(t, [\phi_1 \wedge \dots \wedge \phi_n \rightarrow \phi] \rightarrow [\phi_1 \rightarrow \dots \rightarrow \phi_n \rightarrow \psi])} [R_{10}]$

$\frac{\mathbf{B}(a, t, \phi) \ \phi \rightarrow \psi}{\mathbf{B}(a, t, \psi)} [R_{11a}] \quad \frac{\mathbf{B}(a, t, \phi) \ \mathbf{B}(a, t, \psi)}{\mathbf{B}(a, t, \psi \wedge \phi)} [R_{11b}]$

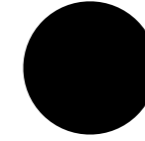
$\frac{\mathbf{S}(s, h, t, \phi)}{\mathbf{B}(h, t, \mathbf{B}(s, t, \phi))} [R_{12}]$

$\frac{\mathbf{I}(a, t, happens(action(a^*, \alpha), t'))}{\mathbf{P}(a, t, happens(action(a^*, \alpha), t))} [R_{13}]$

$\mathbf{B}(a, t, \phi) \ \mathbf{B}(a, t, \mathbf{O}(a^*, t, \phi, happens(action(a^*, \alpha), t')))$

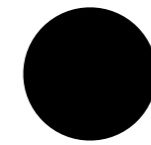
$\frac{\mathbf{O}(a, t, \phi, happens(action(a^*, \alpha), t'))}{\mathbf{K}(a, t, \mathbf{I}(a^*, t, happens(action(a^*, \alpha), t')))} [R_{14}]$

$\frac{\phi \leftrightarrow \psi}{\mathbf{O}(a, t, \phi, \gamma) \leftrightarrow \mathbf{O}(a, t, \psi, \gamma)} [R_{15}]$



2023

IFLAI2 @ RPI



2023

*IFLA12 @ RPI*



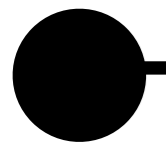
2023

*IFLAI2 @ RPI*

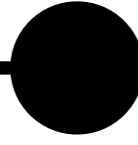


2023

*IFLAI2 @ RPI*



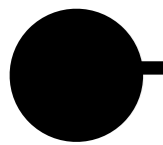
350 BC



2023

*IFLAI2 @ RPI*

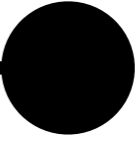




350 BC



Euclid



2023

*IFLAI2 @ RPI*

# Euclidean “Magic”

**Theorem:** There are infinitely many primes.

**Proof:** We take an indirect route. Let  $\Pi = p_1 = 2, p_2 = 3, p_3 = 5, \dots, p_k$  be a finite, exhaustive consecutive sequence of prime numbers. Next, let  $\mathbf{M}_\Pi$  be  $p_1 \times p_2 \times \dots \times p_k$ , and set  $\mathbf{M}'_\Pi$  to  $\mathbf{M}_\Pi + 1$ . Either  $\mathbf{M}'_\Pi$  is prime, or not; we thus have two (exhaustive) cases to consider.

- C1 Suppose  $\mathbf{M}'_\Pi$  is prime. In this case we immediately have a prime number beyond any in  $\Pi$  — contradiction!
- C2 Suppose on the other hand that  $\mathbf{M}'_\Pi$  is *not* prime. Then some prime  $p$  divides  $\mathbf{M}'_\Pi$ . (Why?) Now,  $p$  itself is either in  $\Pi$ , or not; we hence have two sub-cases. Supposing that  $p$  is in  $\Pi$  entails that  $p$  divides  $\mathbf{M}_\Pi$ . But we are operating under the supposition that  $p$  divides  $\mathbf{M}'_\Pi$  as well. This implies that  $p$  divides 1, which is absurd (a contradiction). Hence the prime  $p$  is outside  $\Pi$ .

Hence for *any* such list  $\Pi$ , there is a prime outside the list. That is, there are infinitely many primes. **QED**

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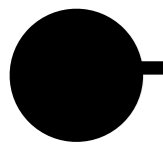
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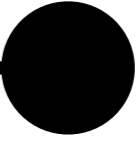
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350 BC

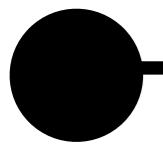


Euclid



2023

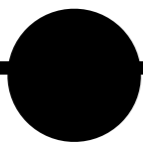
*IFLAI2 @ RPI*



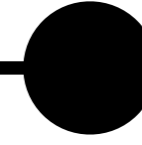
350 BC



Euclid

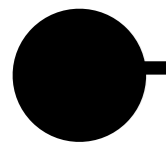


300 BC



2023

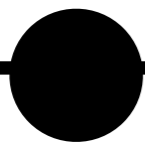
*IFLAI2 @ RPI*



350 BC



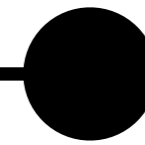
Euclid



300 BC

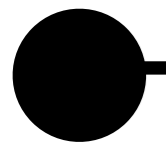


I don't believe in magic! Why exactly is that so convincing? What exactly is he doing?!?

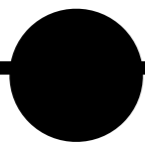


2023

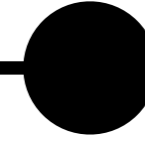
*IFLAI2 @ RPI*



350 BC



300 BC



2023



Euclid



*Organon*

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*IFLAI2 @ RPI*



He's using syllogisms!

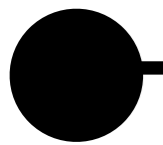
E.g.,

All As are Bs.

All Bs are Cs.

---

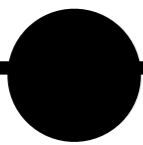
All As are Cs.



350 BC



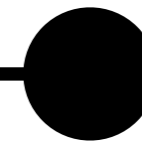
Euclid



300 BC



*Organon*



2023

I don't believe in magic! Why exactly is that so convincing? What exactly is he doing?!?

IFLA12 @ RPI

He's using syllogisms!



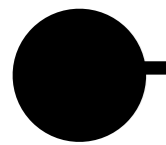
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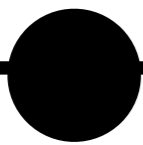
All As are Cs.



350 BC



Euclid

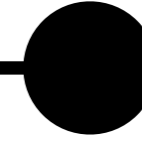


300 BC



*Organon*

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2023

IFLAI2 @ RPI

Balderdash!

He's using syllogisms!



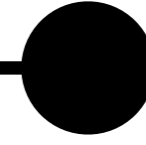
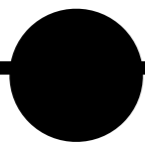
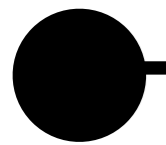
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All As are Cs.



350 BC

300 BC

2023



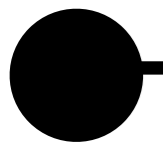
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Euclid

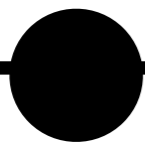
*Organon*

IFLAI2 @ RPI

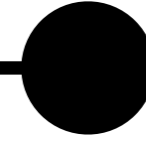
Balderdash!



350 BC



300 BC



2023



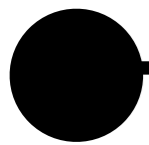
Euclid



*Organon*

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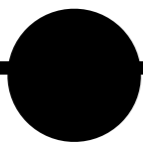
IFLA12 @ RPI



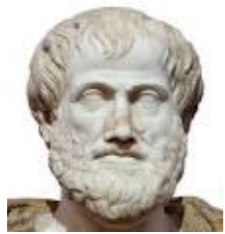
350 BC



Euclid

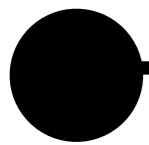


300 BC



*Organon*

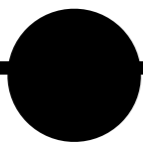
*IFLAI2 @ RPI*



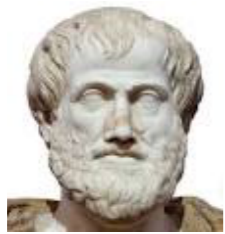
350 BC



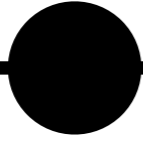
Euclid



300 BC

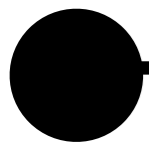


*Organon*



1666

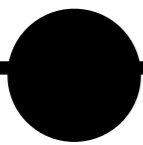
*IFLAI2 @ RPI*



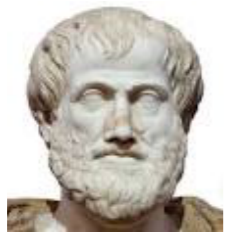
350 BC



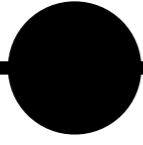
Euclid



300 BC



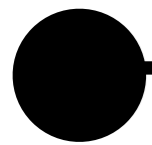
*Organon*



1666



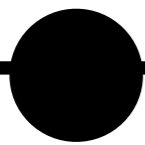
Leibniz



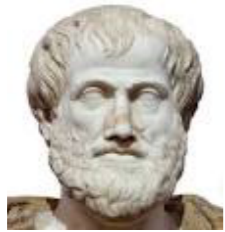
350 BC



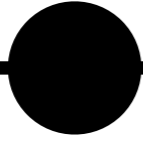
Euclid



300 BC



*Organon*



1666



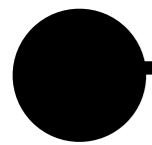
Leibniz



IFLAI2 @ RPI



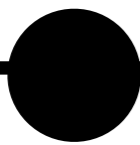
“Universal  
Computational  
Logic”



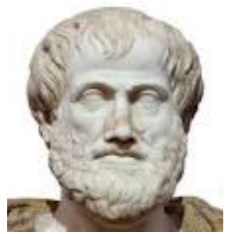
350 BC



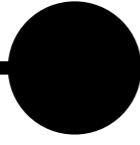
Euclid



300 BC



*Organon*



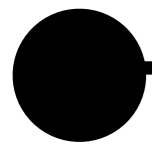
1666



Leibniz



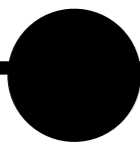
# “Universal Computational Logic”



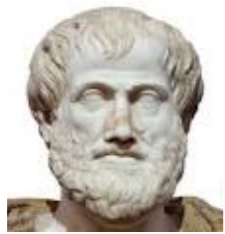
350 BC



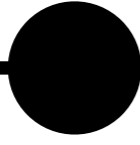
Euclid



300 BC



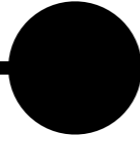
*Organon*



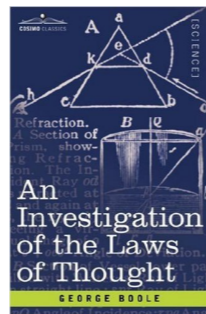
1666



Leibniz

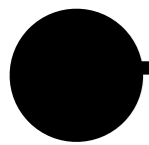


1854



IFLAI2 @ RPI

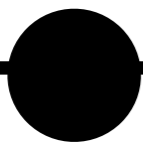
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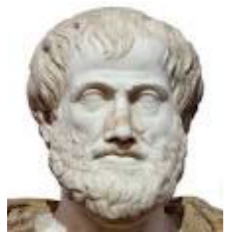
350 BC



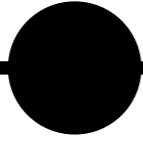
Euclid



300 BC



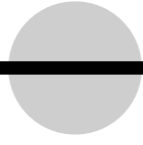
*Organon*



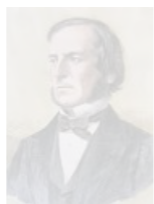
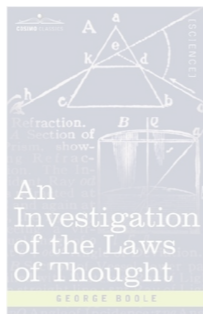
1666



Leibniz



1854

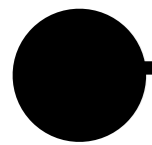


IFLAI2 @ RPI

# “Universal Computational Logic”



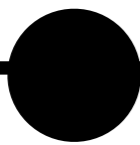
## Logic Theorist (birth of modern logicist AI)



350 BC



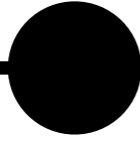
Euclid



300 BC



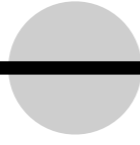
*Organon*



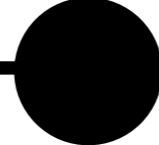
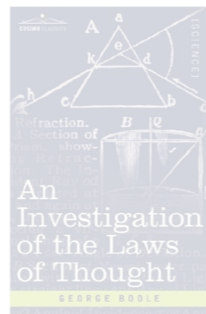
1666



Leibniz



1854



1956



Simon

IFLAI2 @ RPI

# “Astonishing” Logic Theorist Proof @ Dawn of AI

# “Astonishing” Logic Theorist Proof @ Dawn of AI

1	$(\phi \vee \phi) \rightarrow \phi$	axiom
2	$(\neg\phi \vee \neg\phi) \rightarrow \neg\phi$	substitution
3	$(\phi \rightarrow \neg\phi) \rightarrow \neg\phi$	a “replacement rule”
4	$(A \rightarrow \neg A) \rightarrow \neg A$	substitution

# “Astonishing” Logic Theorist Proof @ Dawn of AI

1	$(\phi \vee \phi) \rightarrow \phi$	axiom
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At dawn of AI: 10 seconds.

# “Astonishing” Logic Theorist Proof @ Dawn of AI

1	$(\phi \vee \phi) \rightarrow \phi$	axiom
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At dawn of AI: 10 seconds.

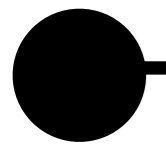
AI of today, e.g. PC provability oracle in  
HyperSlate<sup>®</sup>, *vanishingly* small amount of time.



# “Universal Computational Logic”



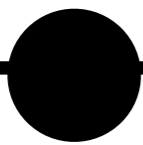
## Logic Theorist (birth of modern logicist AI)



350 BC



Euclid



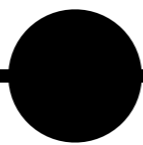
300 BC



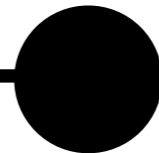
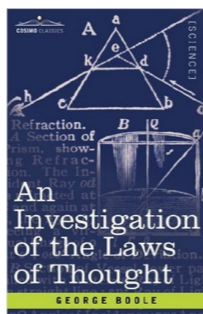
*Organon*



Leibniz



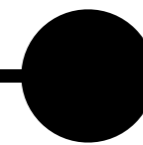
1854



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Simon



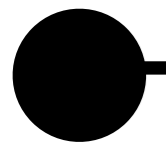
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IFLAI2 @ RPI

# “Universal Computational Logic”



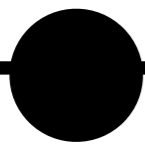
## Logic Theorist (birth of modern logicist AI)



350 BC



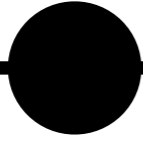
Euclid



300 BC



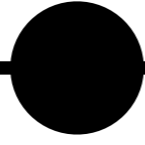
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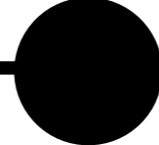
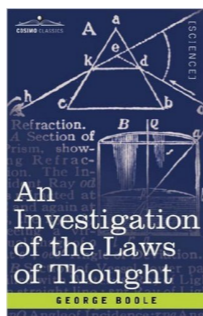
1666



Leibniz



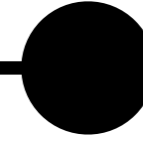
1854



1956



Simon



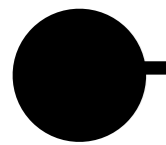
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IFLAI2 @ RPI

# “Universal Computational Logic”



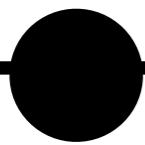
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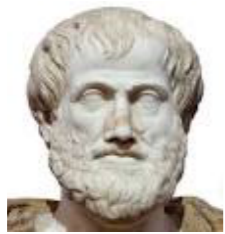
350 BC



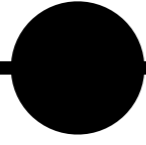
Euclid



300 BC



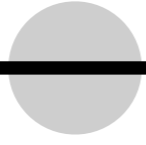
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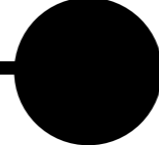
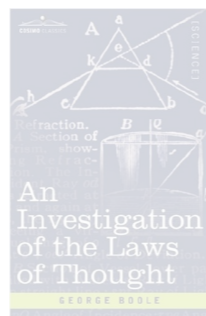
1666



Leibniz



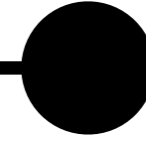
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1956



Simon



2023

IFLAI2 @ RPI

“Universal  
Computational  
Logic”



Logic Theorist  
(birth of modern logicist AI)



350 BC

300 BC

1666

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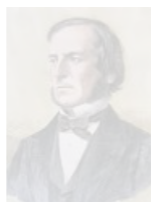
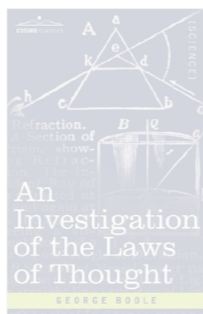
Euclid



*Organon*



Leibniz



Simon

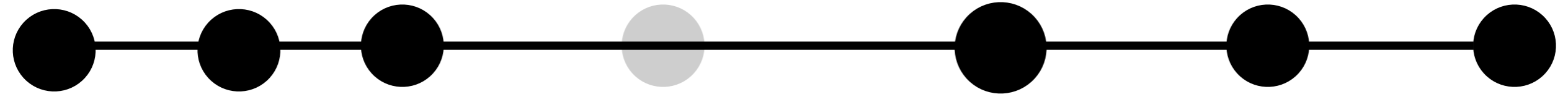
IFLAI2 @ RPI

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“Universal  
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Logic Theorist  
(birth of modern logicist AI)



350 BC      300 BC      1666      1854      1956      2023      2024



Euclid

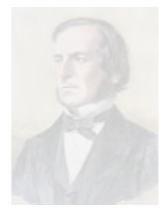
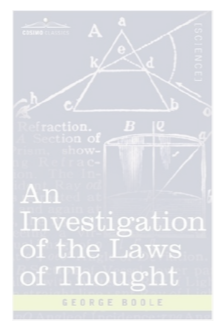


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Leibniz

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1854



Simon

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IFLAI2 @ RPI

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# Entscheidungsproblem

“Universal Computational Logic”



Logic Theorist  
(birth of modern logicist AI)



350 BC      300 BC      1666      1854      1956      2023      2024



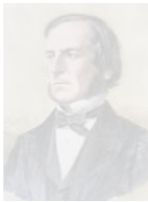
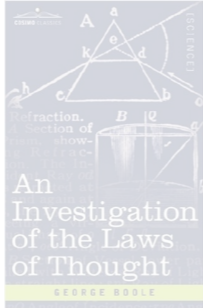
Euclid



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IFLAI2 @ RPI

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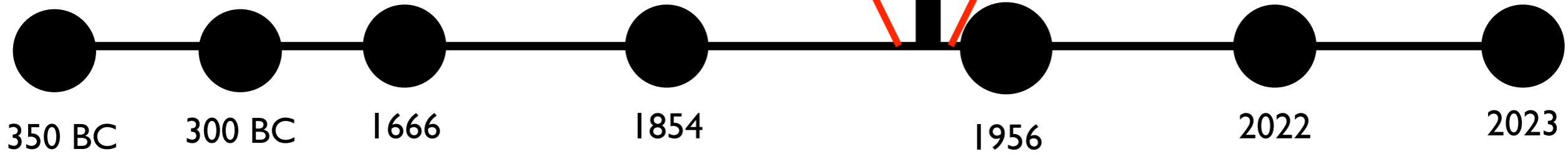
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“Universal Computational Logic”



Logic Theorist  
(birth of modern logicist AI)



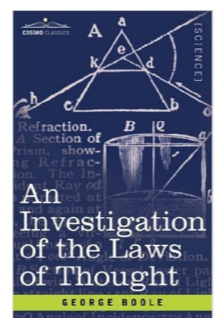
Euclid



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Simon

IFLAI2 @ RPI

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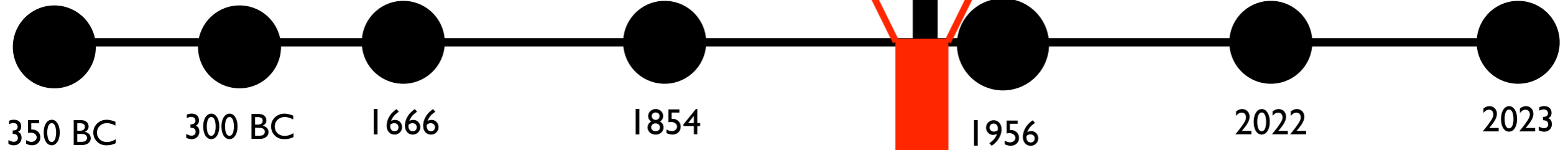
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Logic Theorist  
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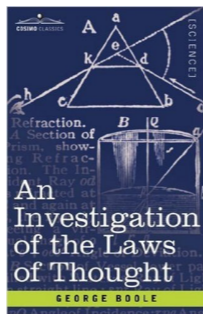
Euclid



Organon



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Simon

IFLAI2 @ RPI

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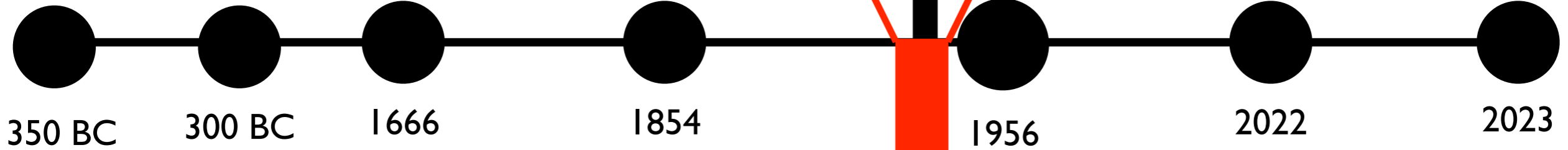
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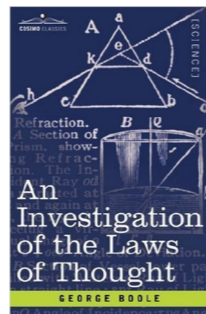
Euclid



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IFLAI2 @ RPI

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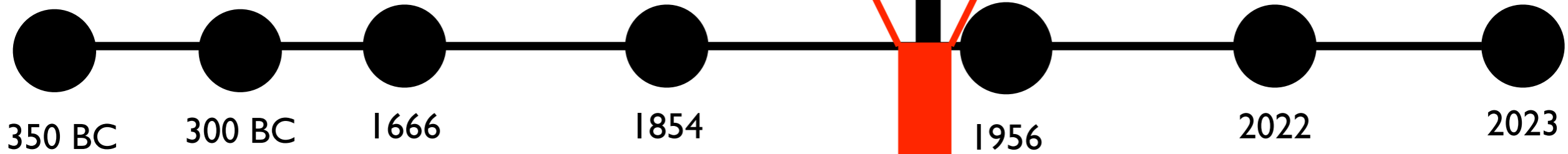
# Entscheidungsproblem



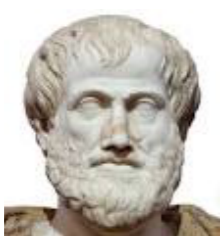
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Logic Theorist  
(birth of modern logicist AI)



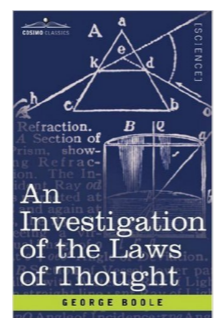
Euclid



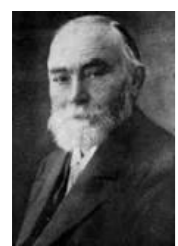
Organon



Leibniz



Simon



Frege

Exceeds Leibniz & de-mystifies Euclid: the “compellingness” of these proofs consists in their being, at bottom, formal proofs in first-order logic (FOL).

IFLAI2 @ RPI

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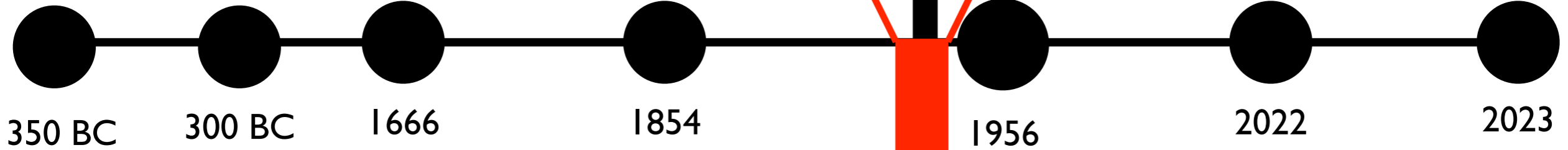
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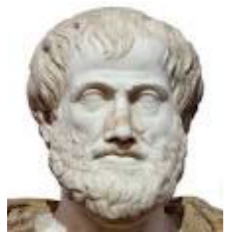
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Logic Theorist  
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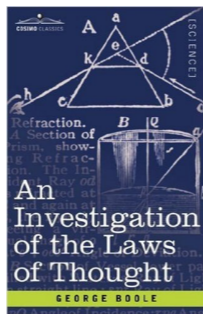
Euclid



Organon



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1854



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Church

IFLAI2 @ RPI

T h e S i n g u l a r i t y ?

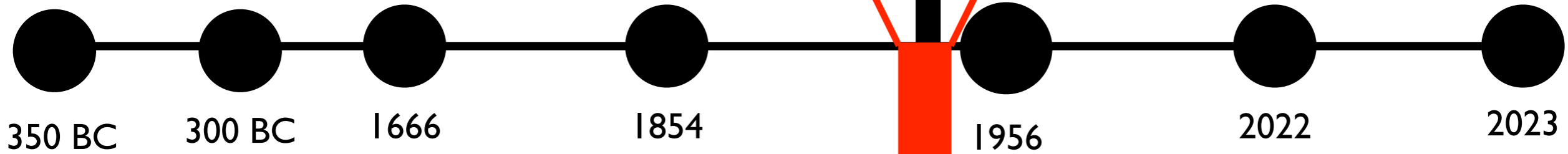
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“Universal Computational Logic”



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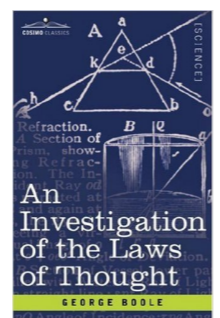
Euclid



Organon



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Turing



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IFLAI2 @ RPI

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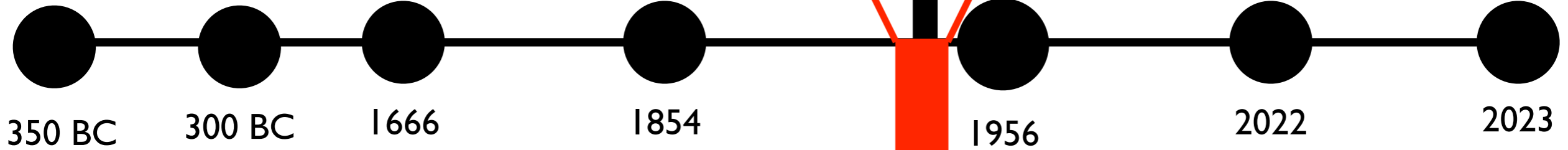
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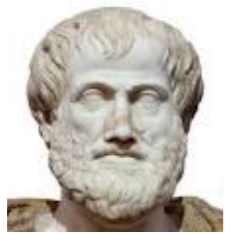
“Universal Computational Logic”



Logic Theorist  
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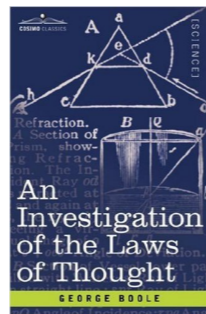
Euclid



Organon



Leibniz



1854



Simon

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Frege

Exceeds Leibniz & de-mystifies Euclid: the “compellingness” of these proofs consists in their being, at bottom, formal proofs in first-order logic (FOL).



Church



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IFLAI2 @ RPI

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T h e S i n g u l a r i t y ?

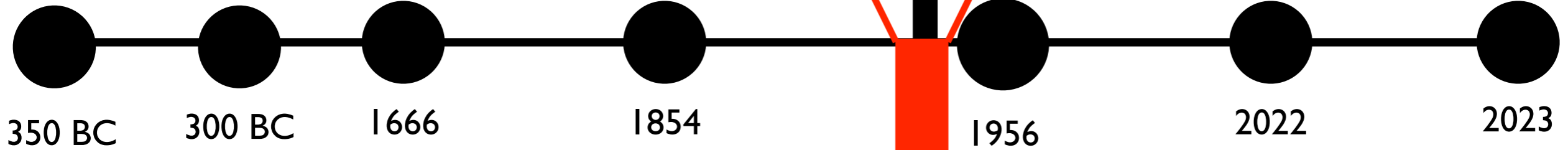
# Entscheidungsproblem



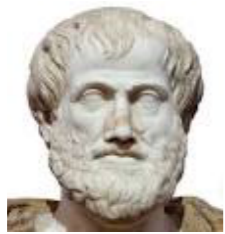
“Universal Computational Logic”



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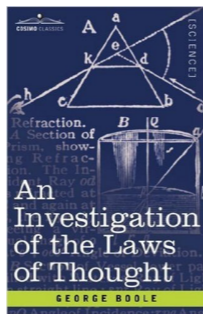
Euclid



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Leibniz



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Church



Turing



Post



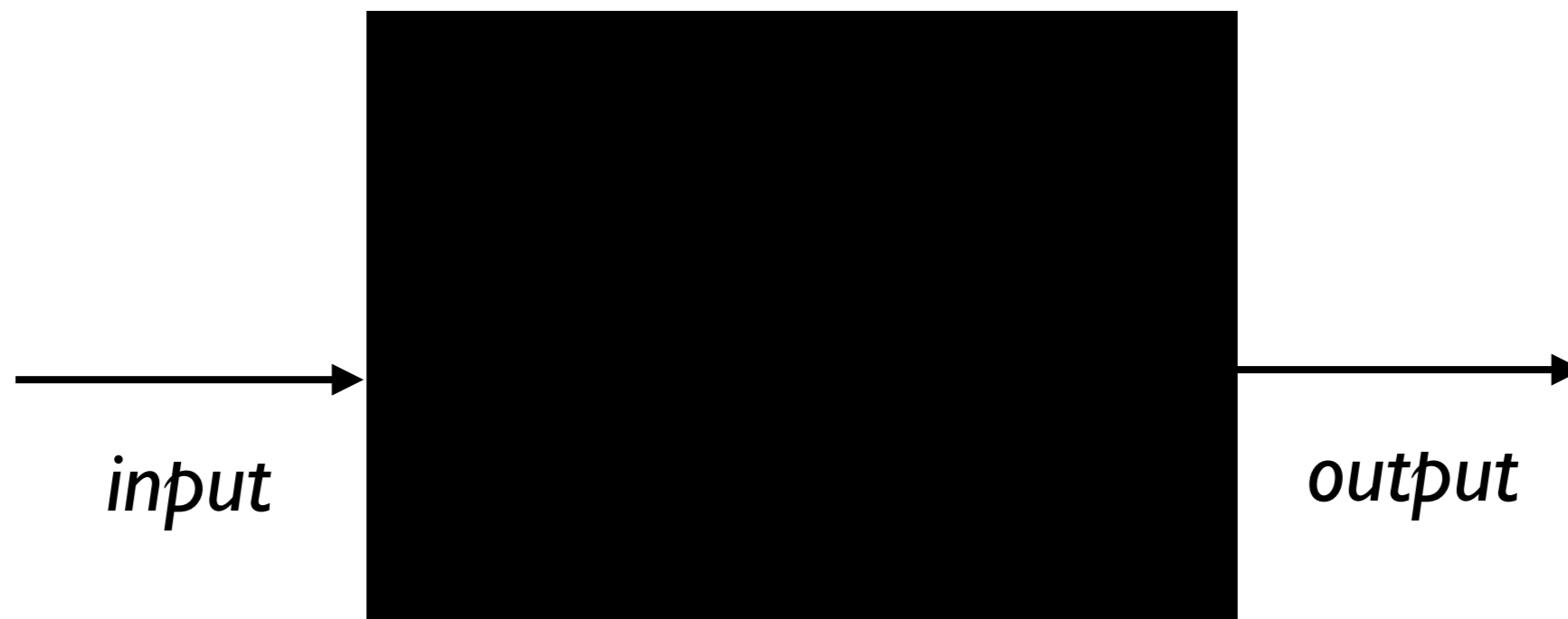
Simon

IFLAI2 @ RPI

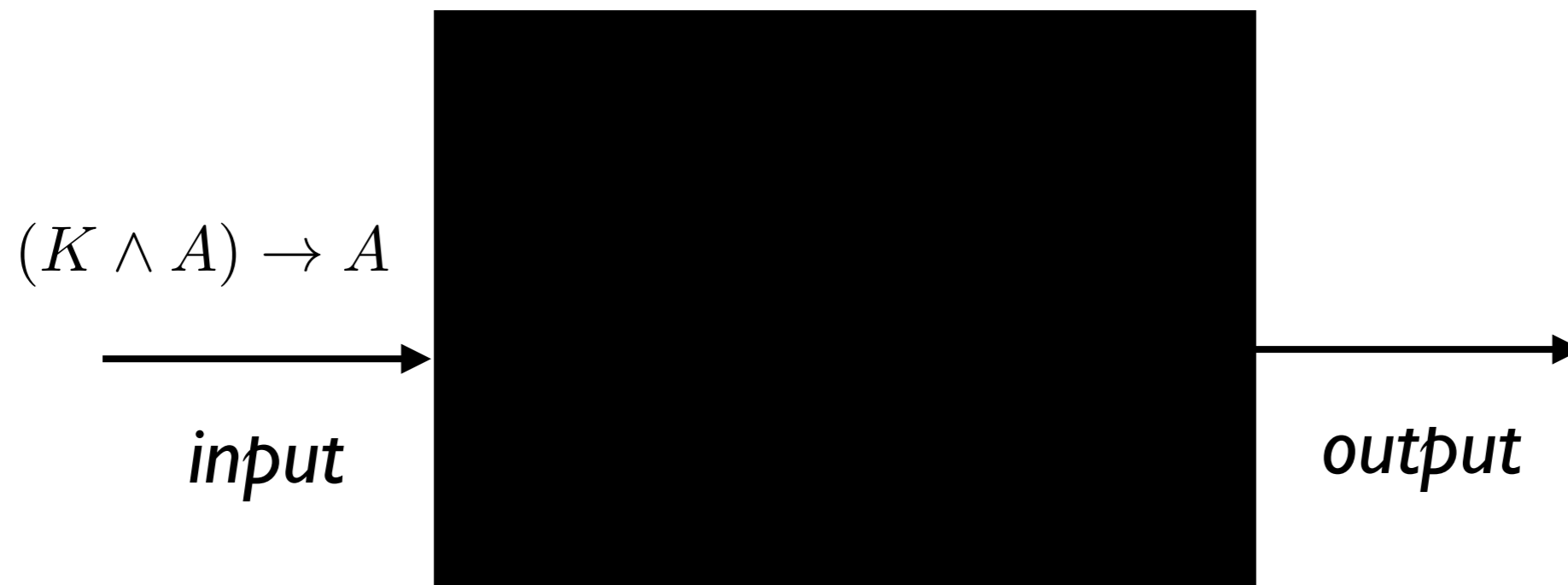
Here’s what a computer is, and given that, sorry, the *Entscheidungsproblem* can’t be solved by such a machine!

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First, the Theoremhood Decision Problem  
( $\text{THEOREM}_{\text{PC}}$ )  
for the Propositional Calculus

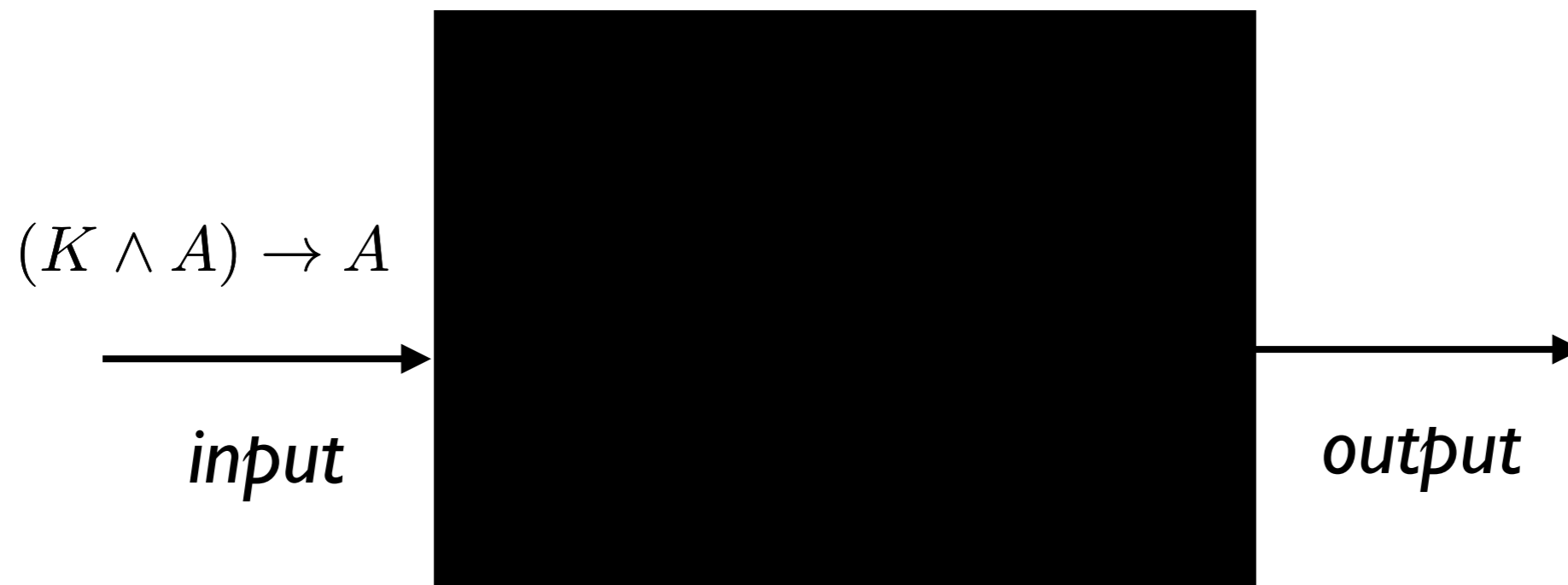


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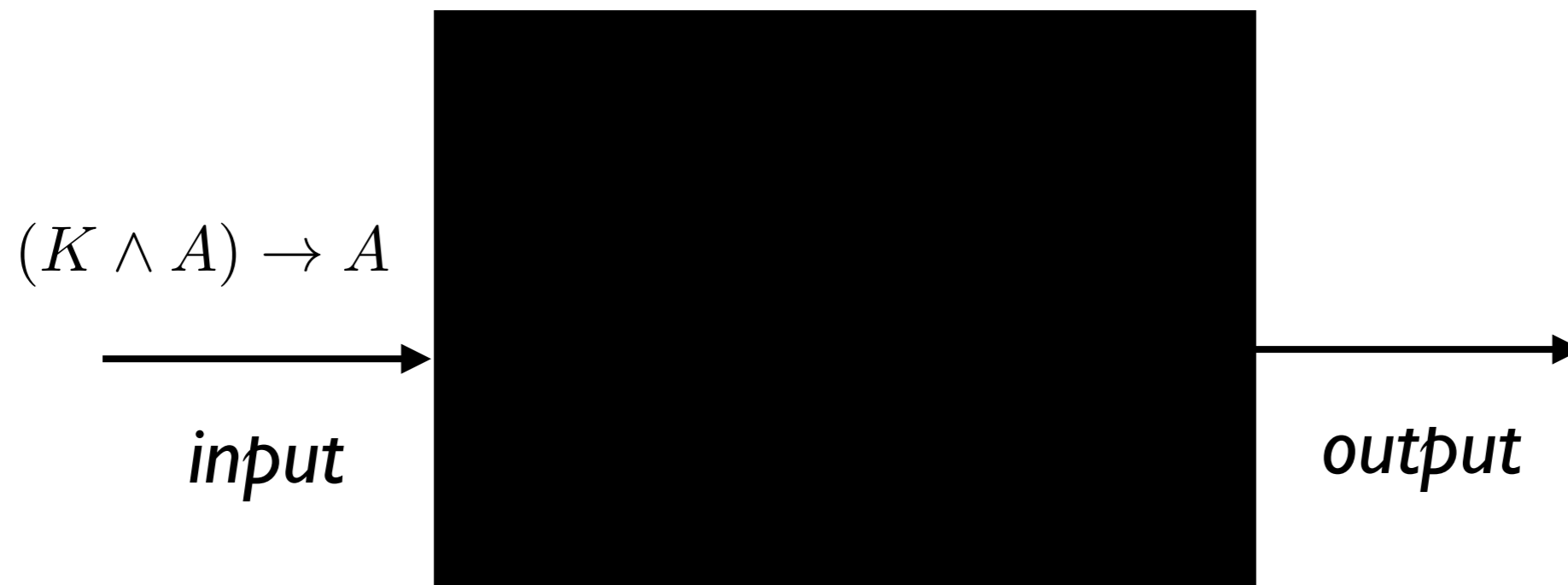




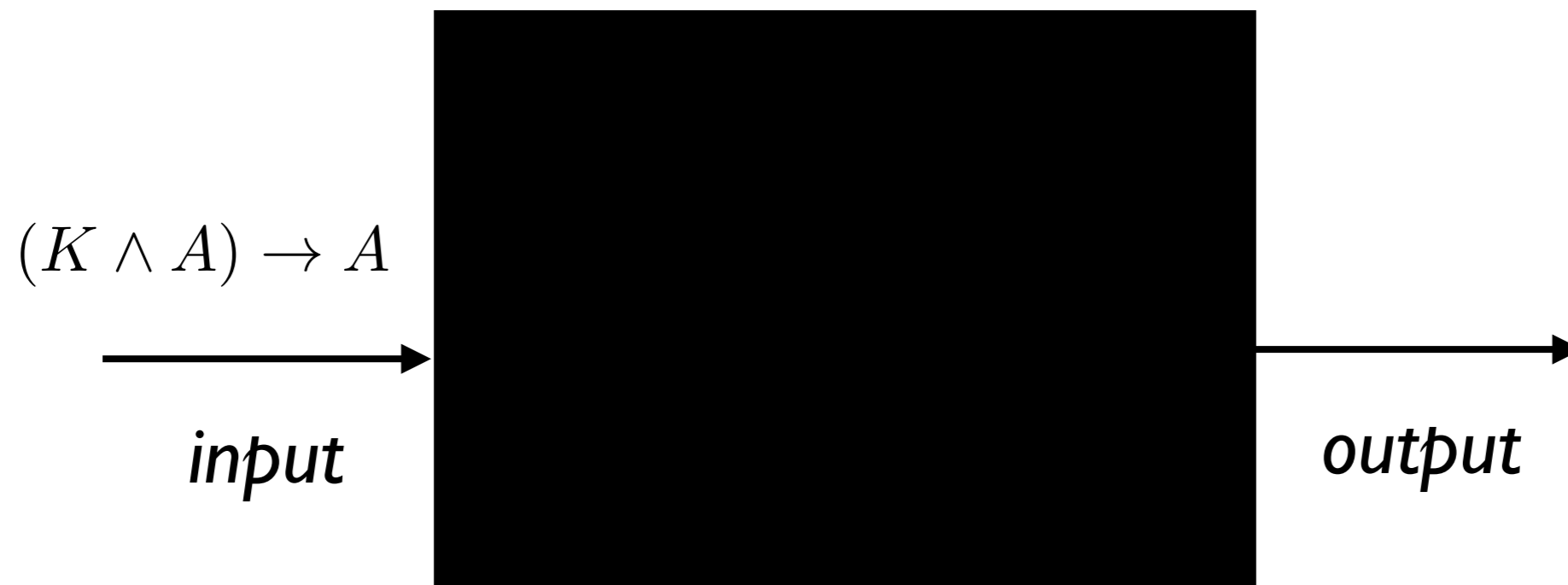
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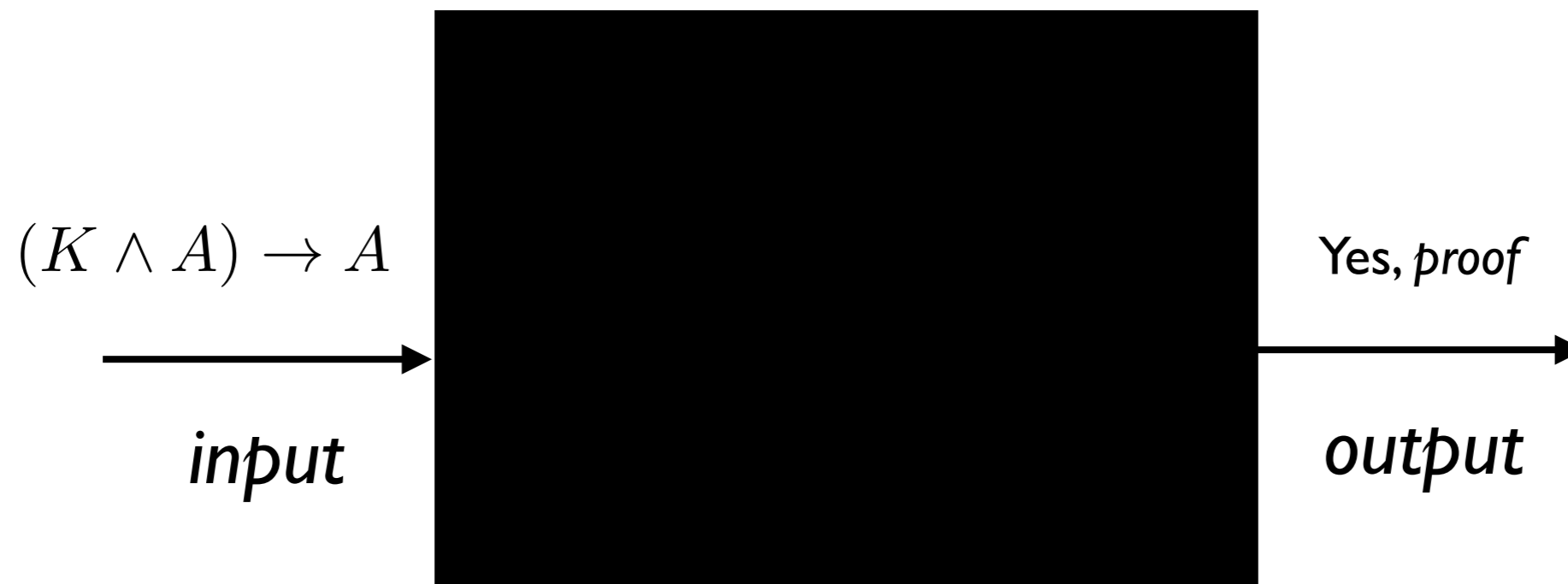
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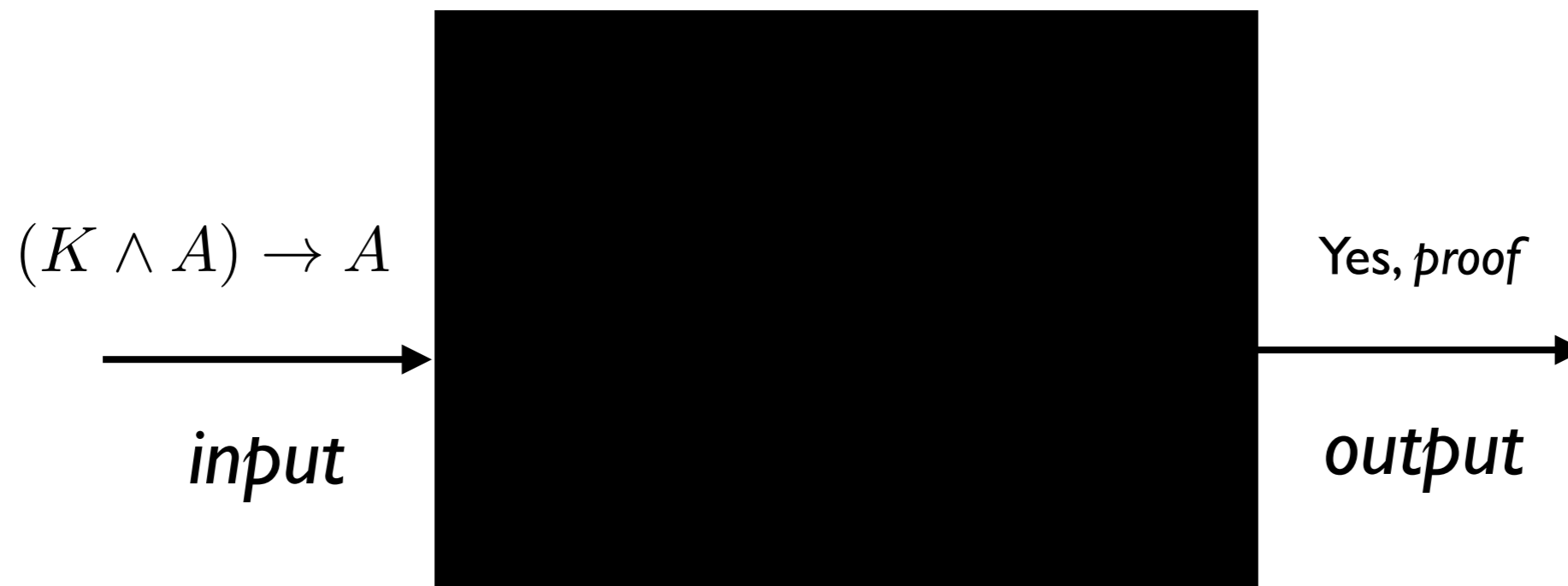
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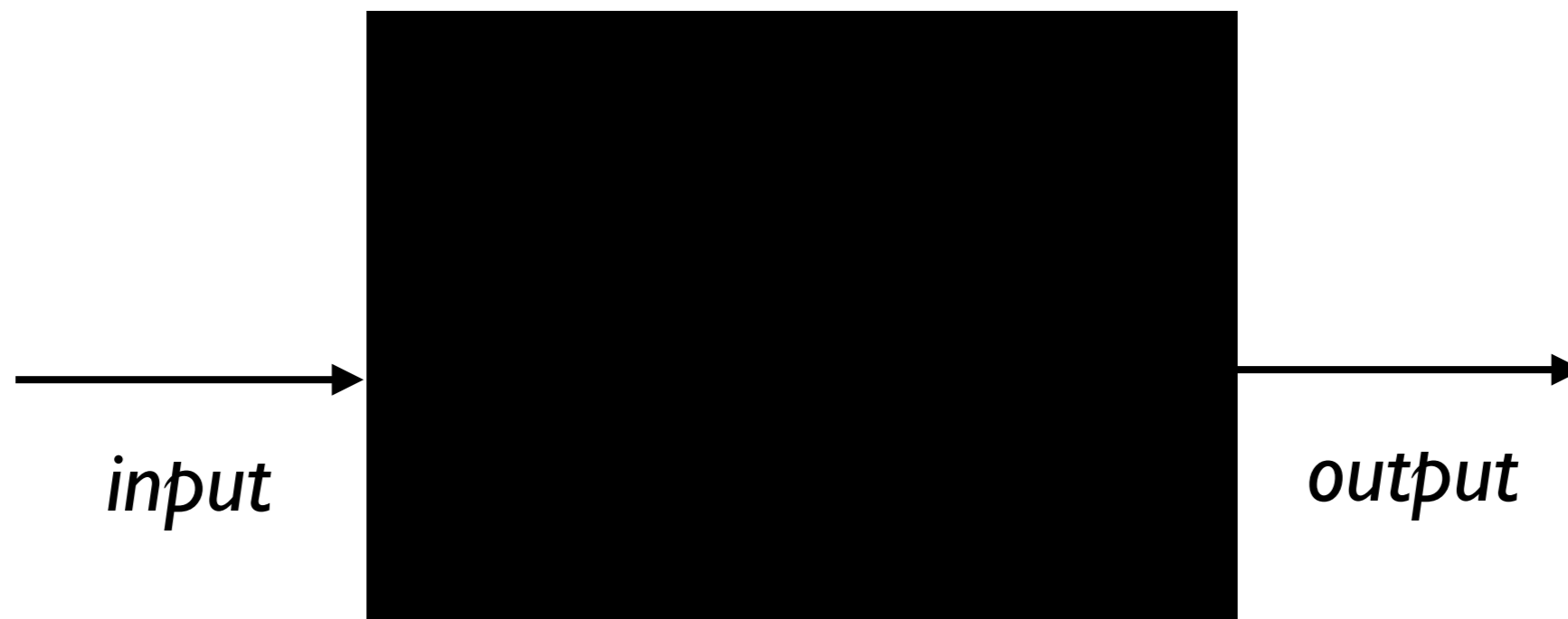


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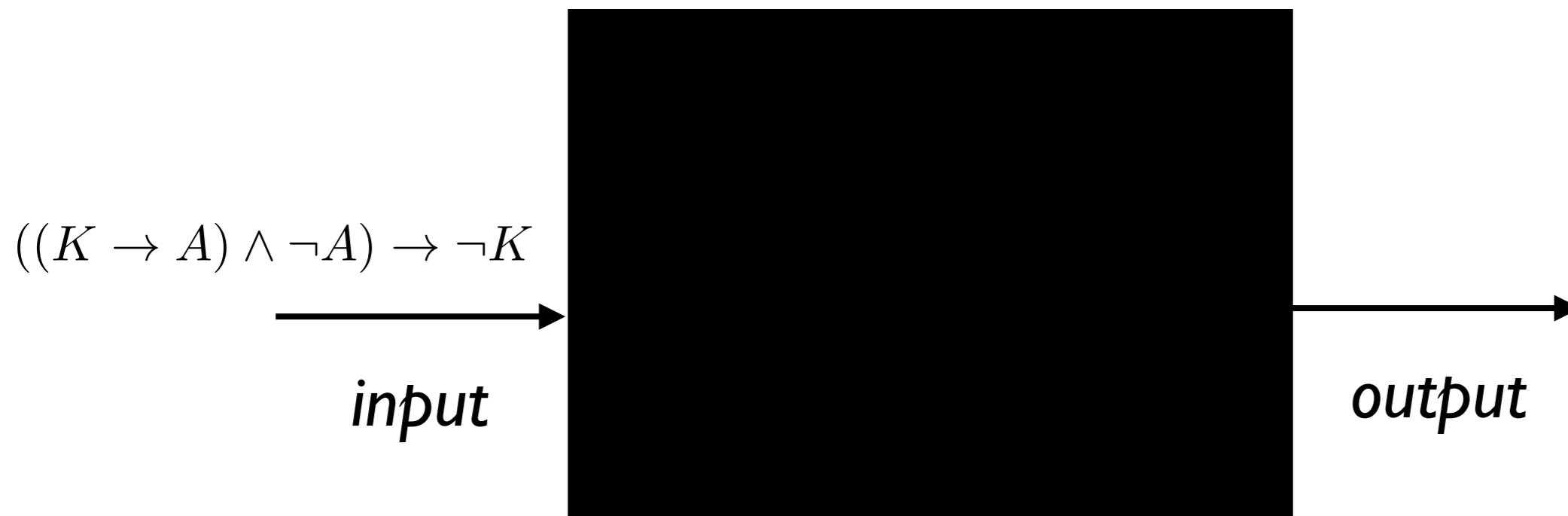
**Hard!! — for apparently no polynomial-time algorithm for this!**

First, the Theoremhood Decision Problem  
( $\text{THEOREM}_{\text{PC}}$ )  
for the Propositional Calculus



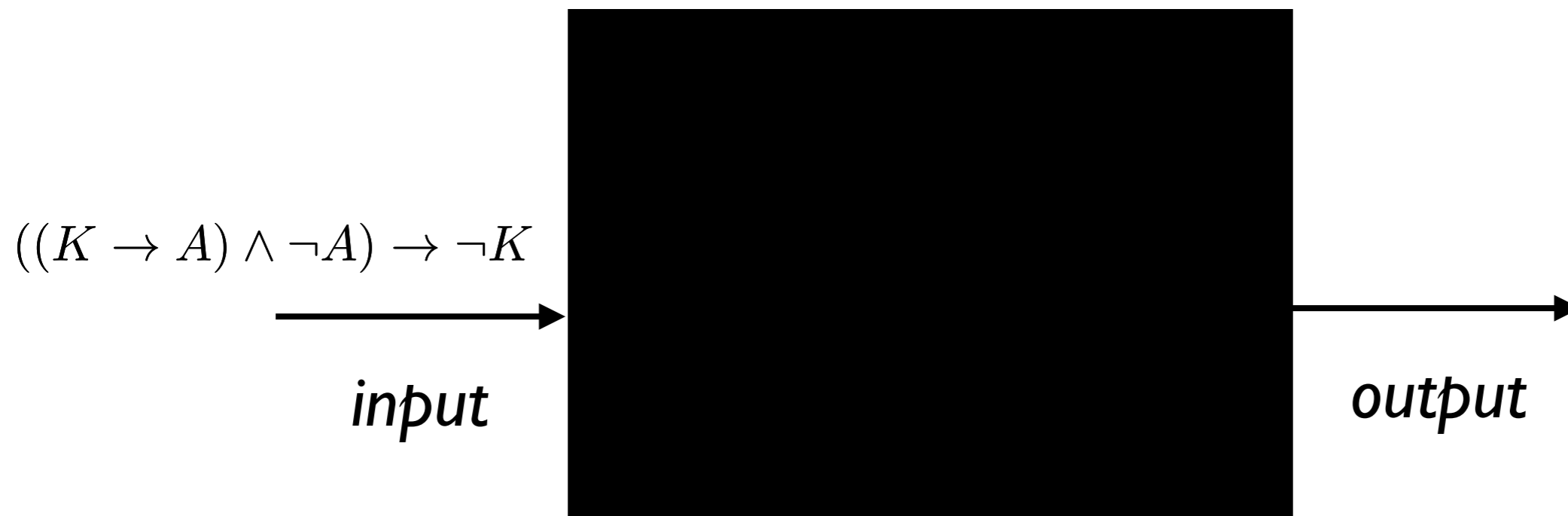
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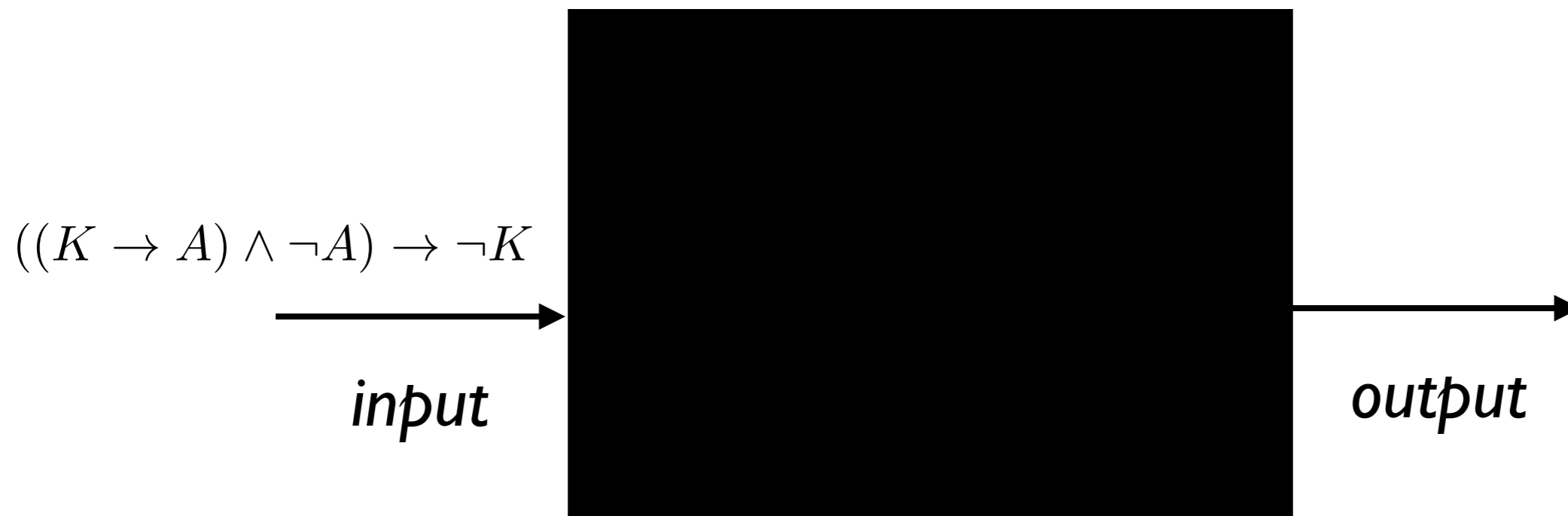
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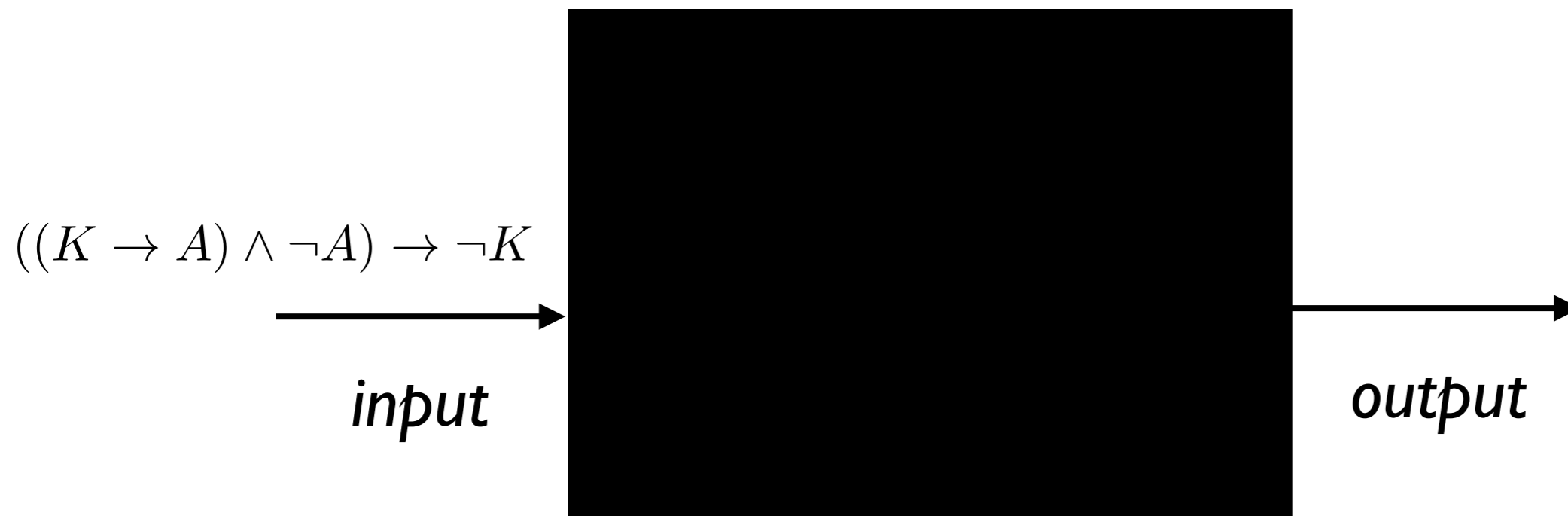


First, the Theoremhood Decision Problem  
( $\text{THEOREM}_{\text{PC}}$ )  
for the Propositional Calculus



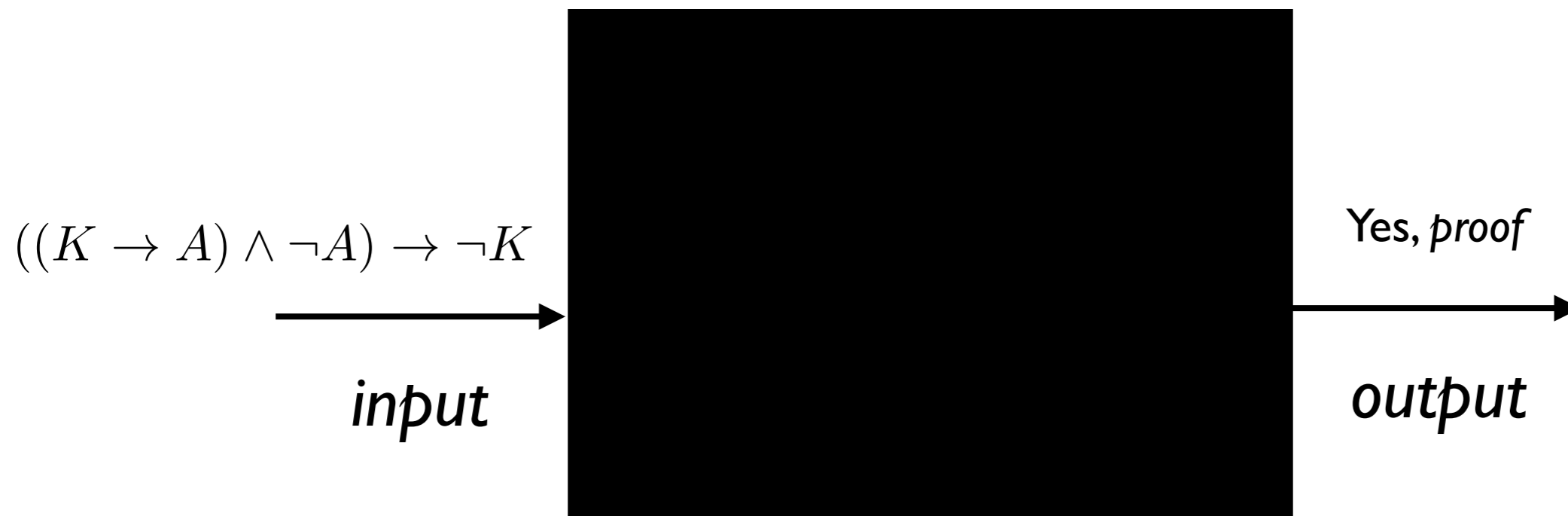
**Hard!! — for apparently no polynomial-time algorithm for this!**

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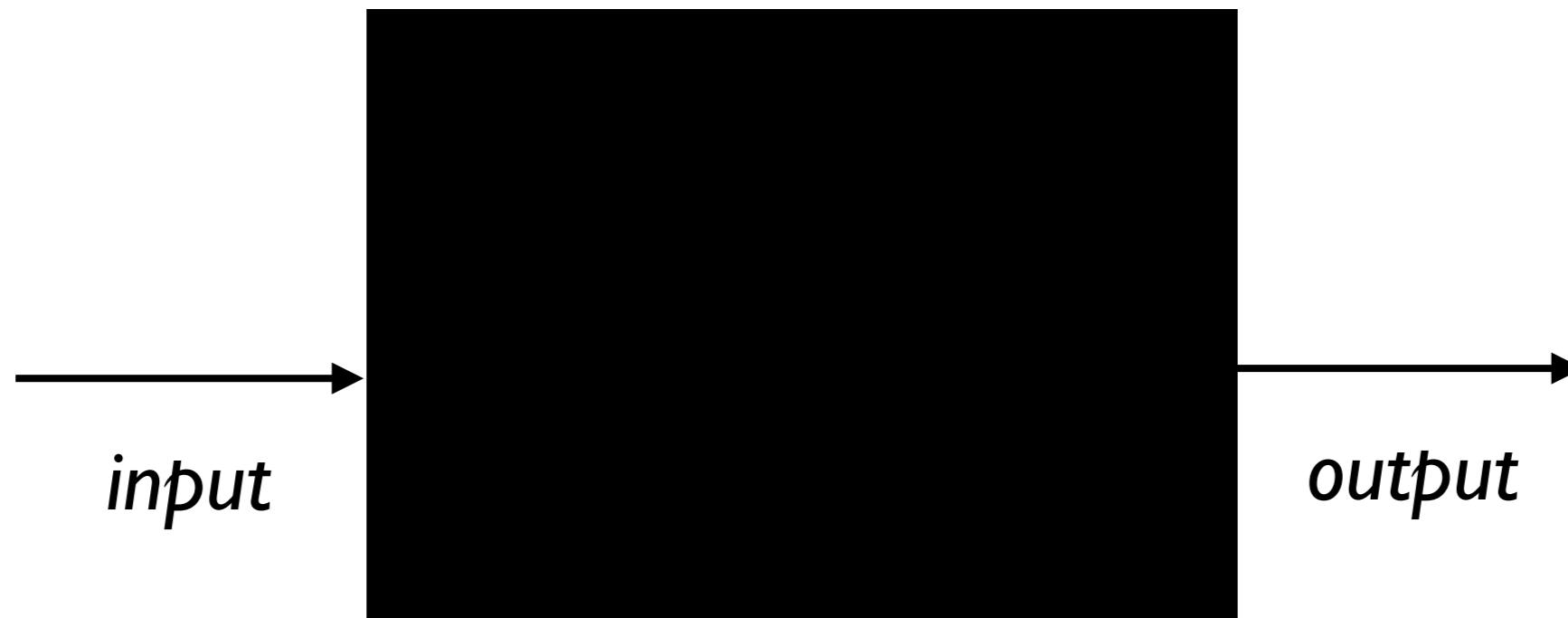
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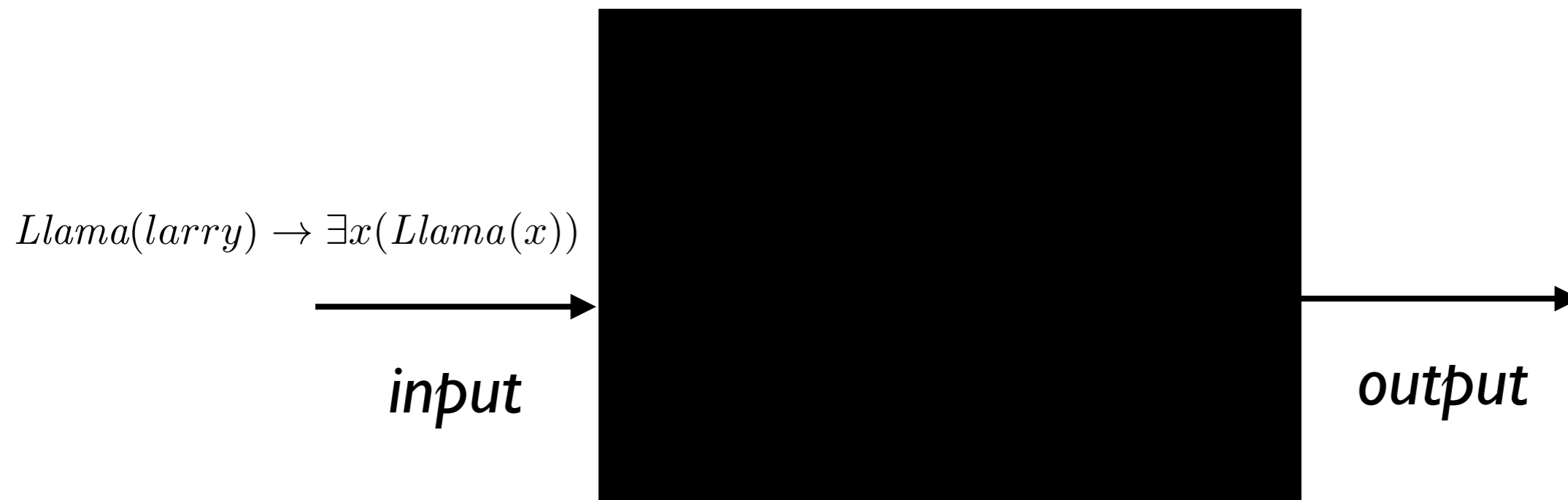


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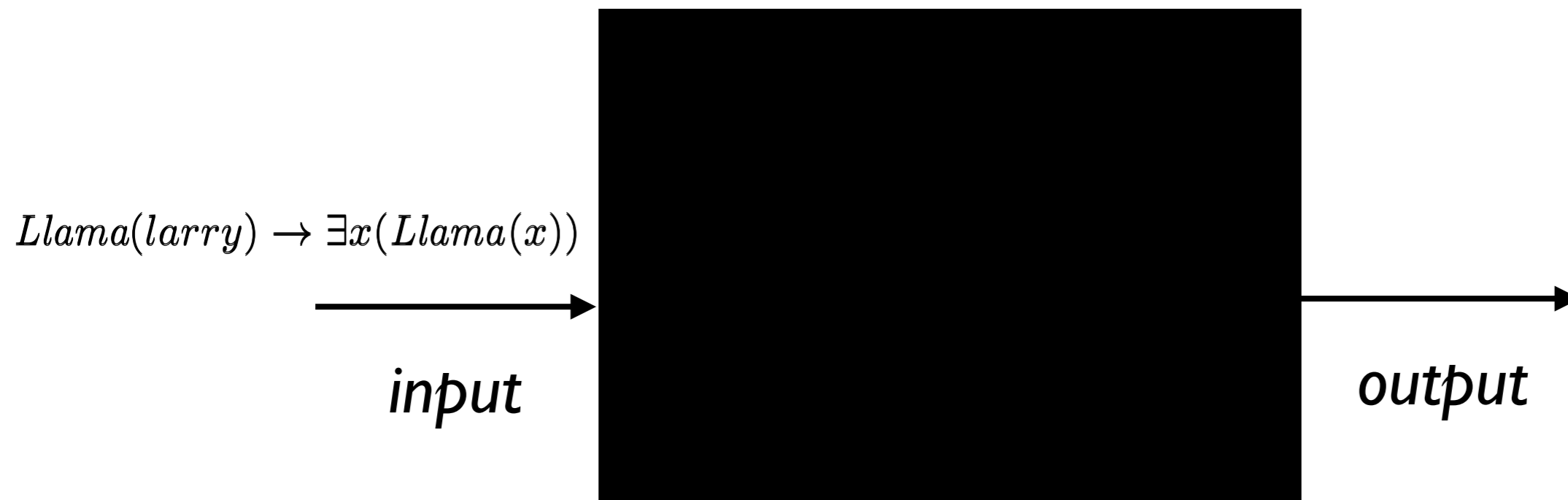
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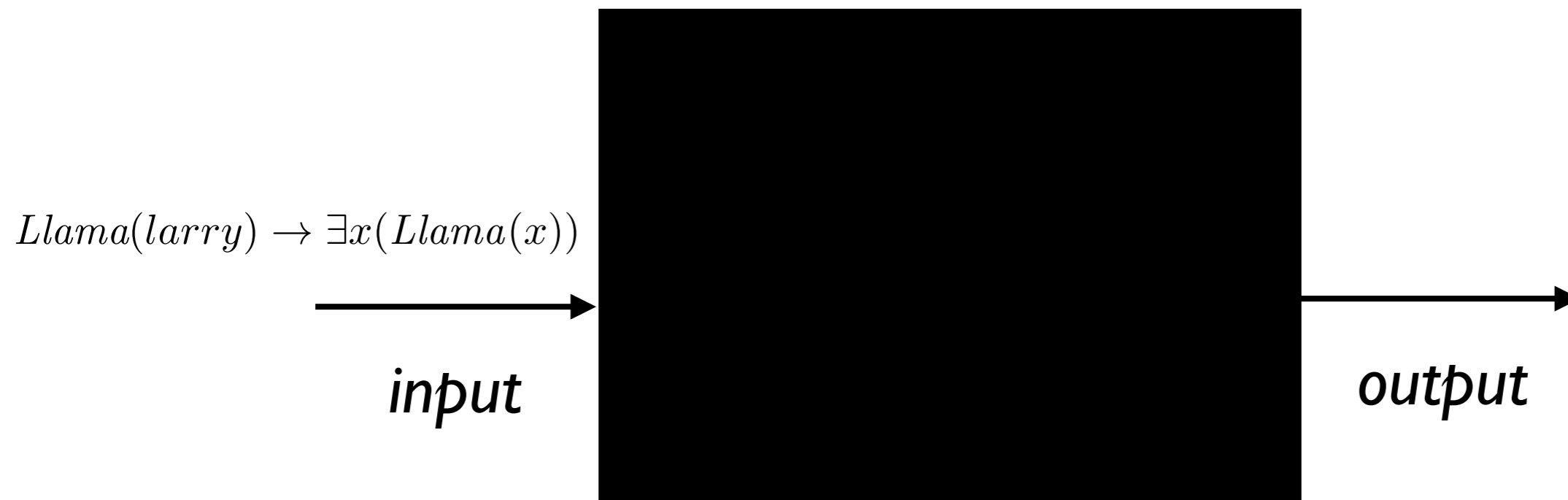
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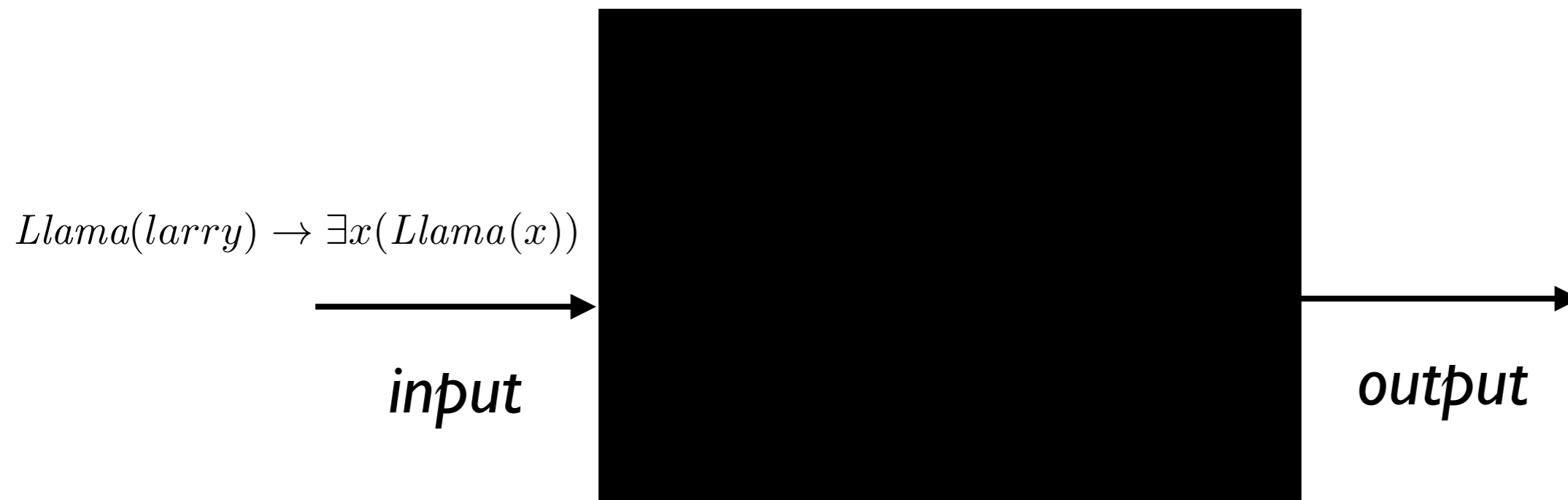
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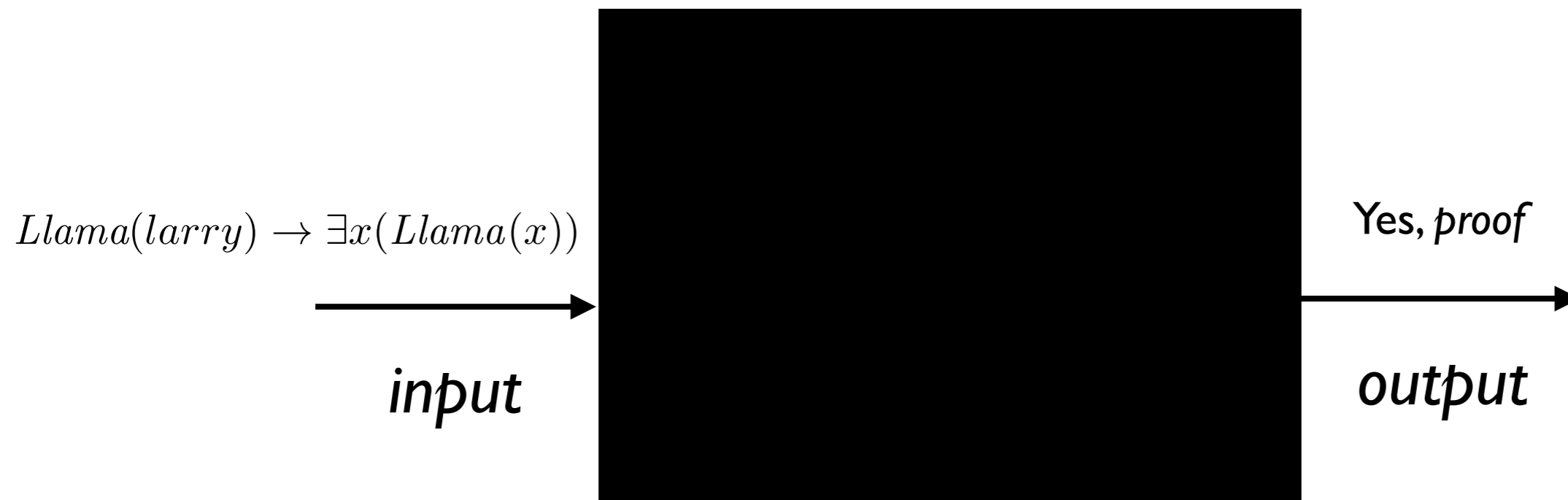


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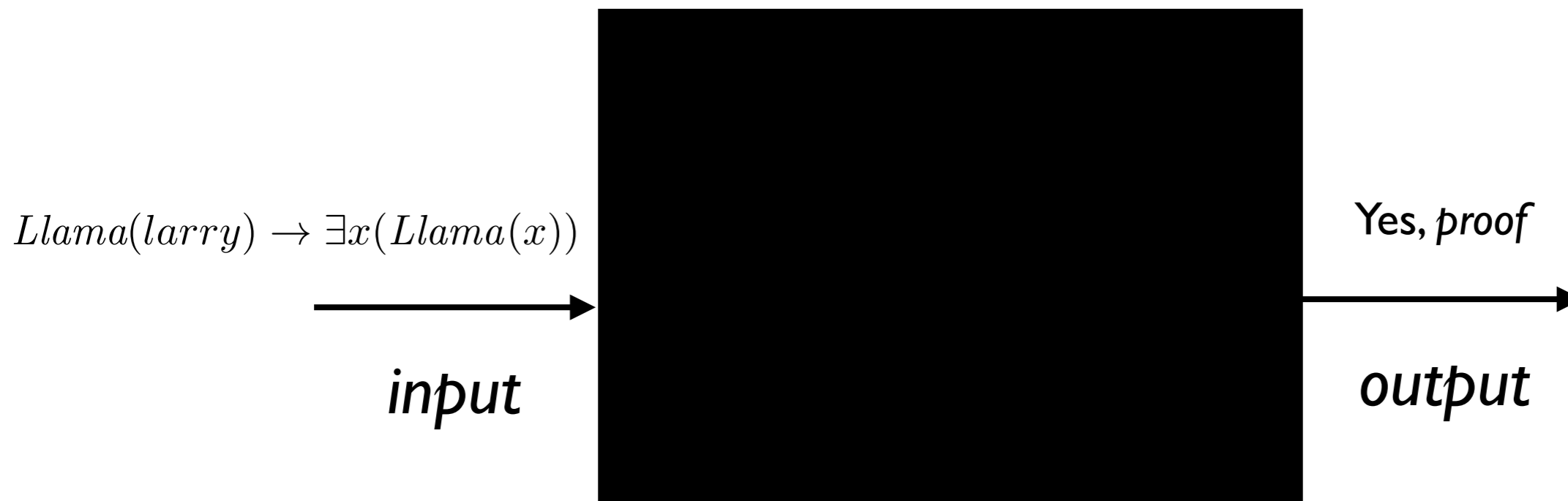




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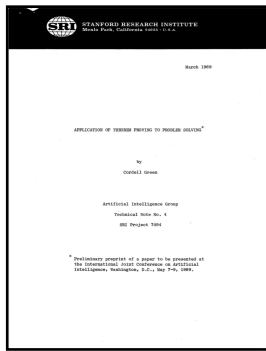


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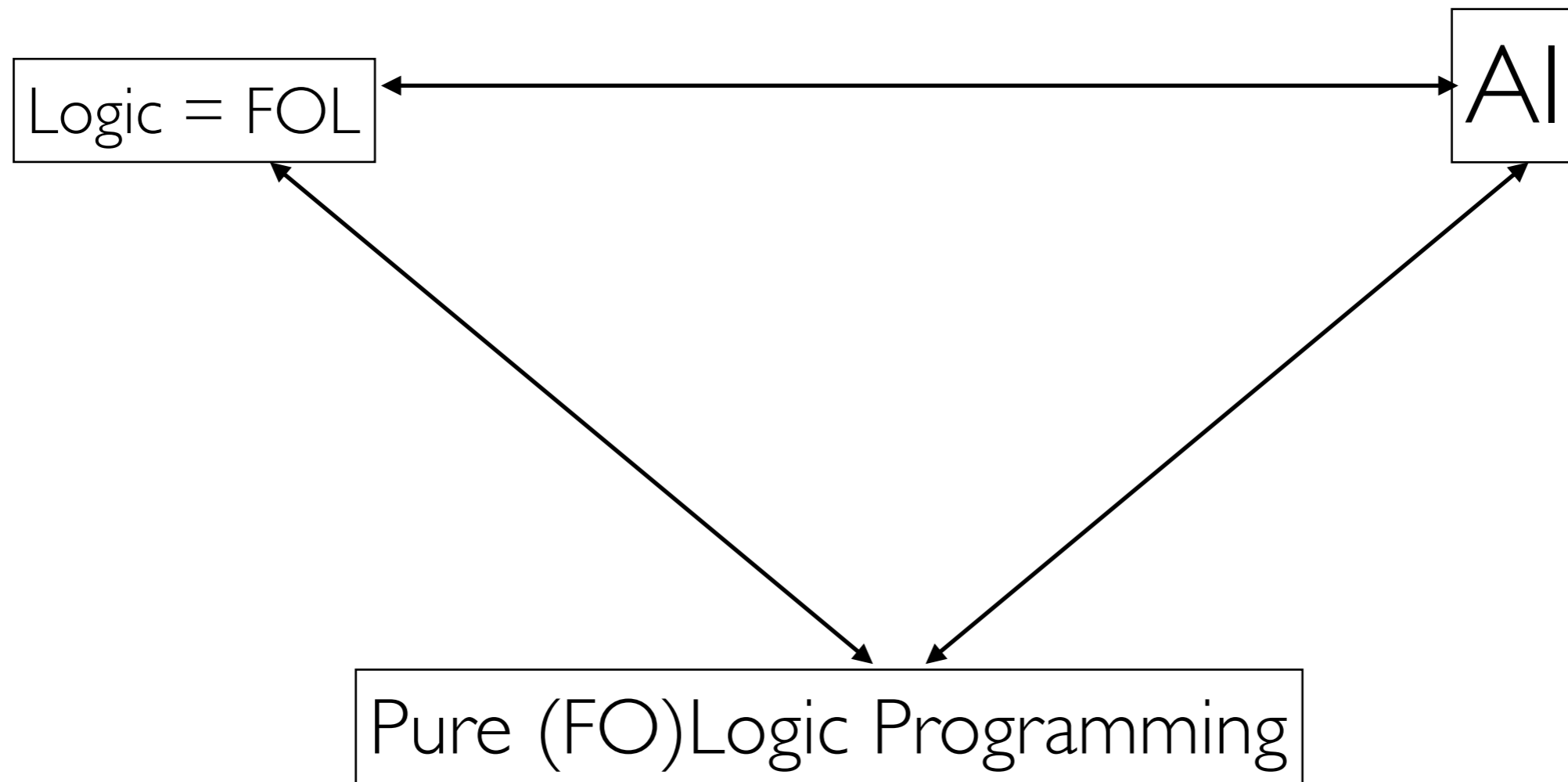


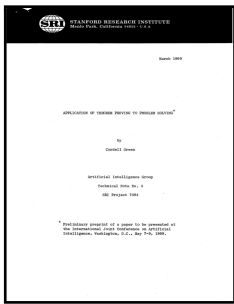
**Not just hard: *impossible* for a (and this needed to be *invented* in the course of clarifying and solving the problem) standard computing machine.**

# On Logic & AI, Specifically ...

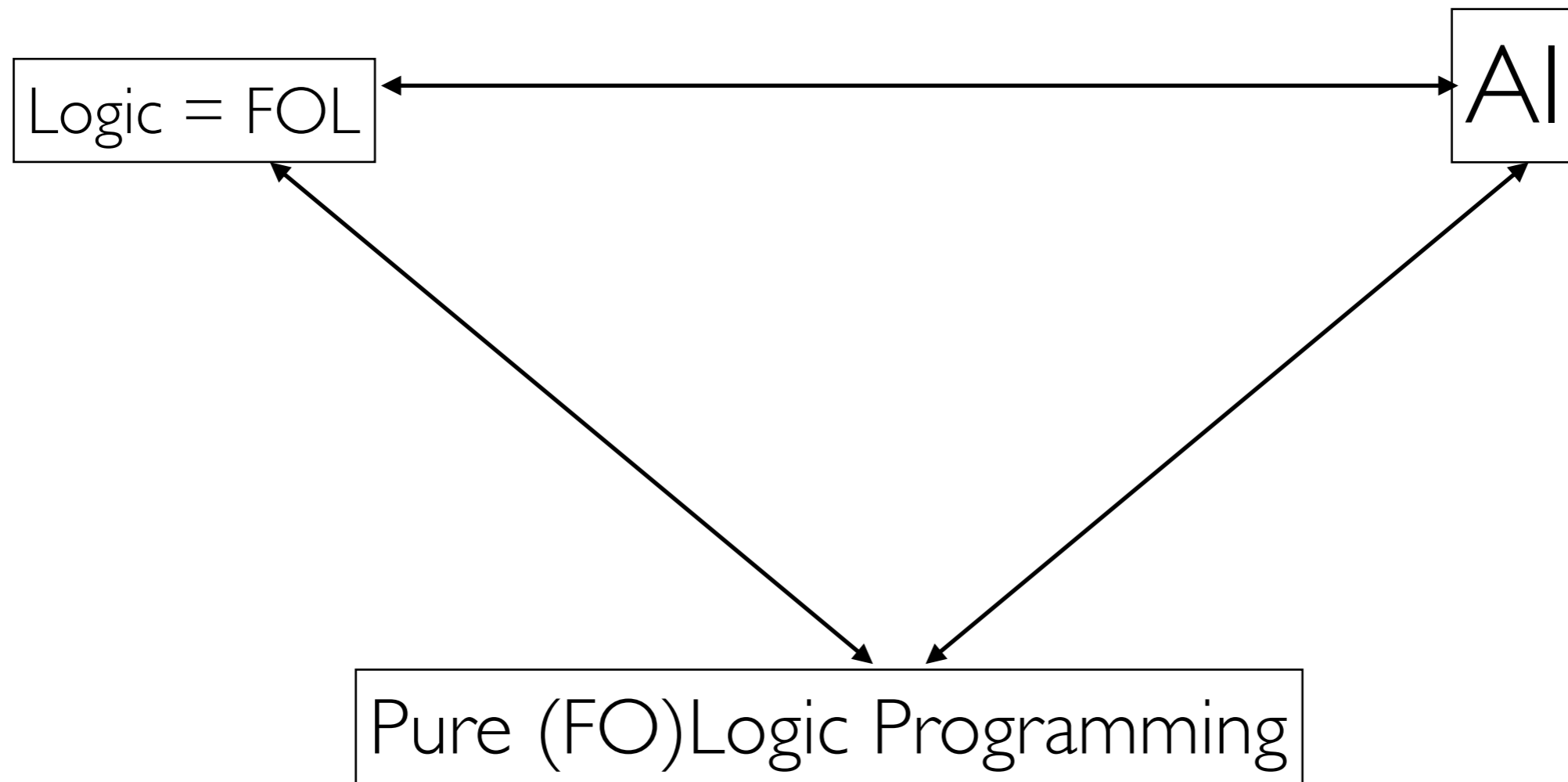


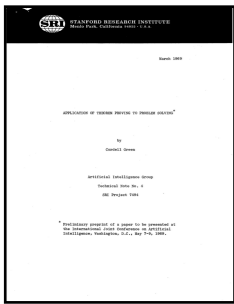
# The Terrific Triad circa 1965



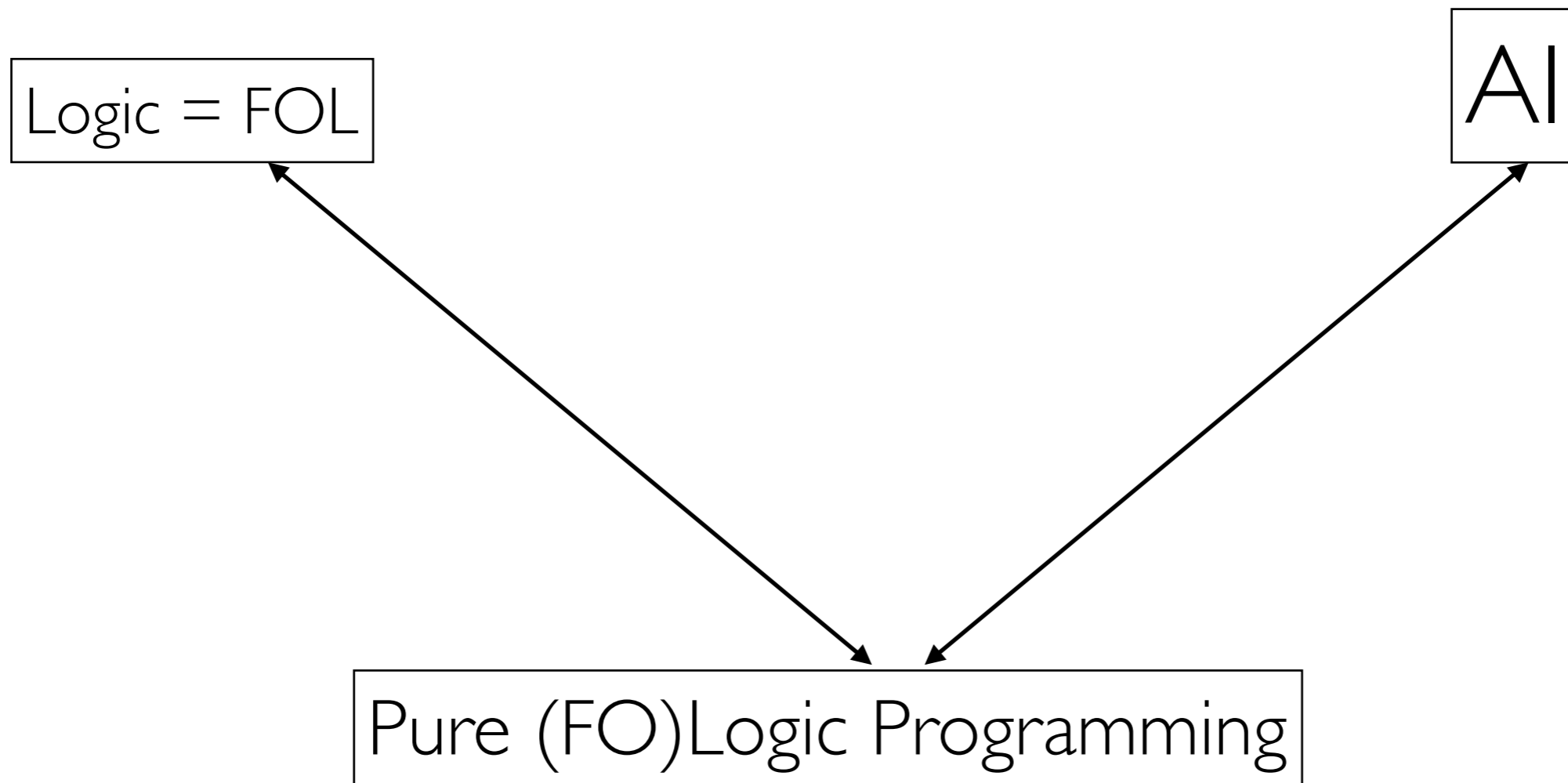


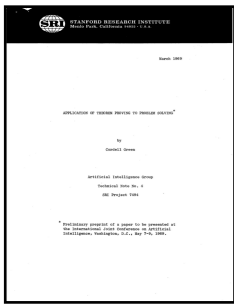
# The Disastrous Disunion





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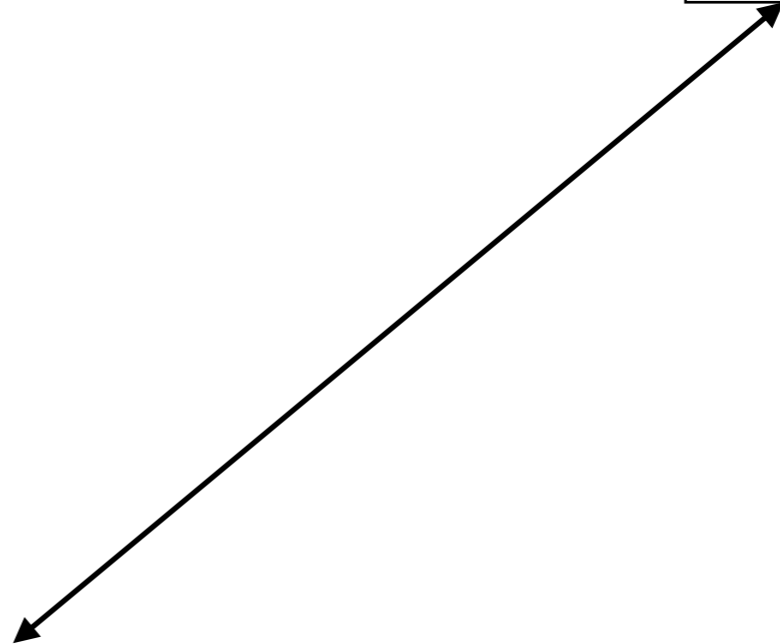


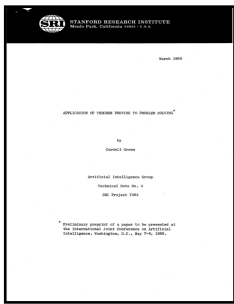
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Logic = FOL

AI

Pure (FO)Logic Programming





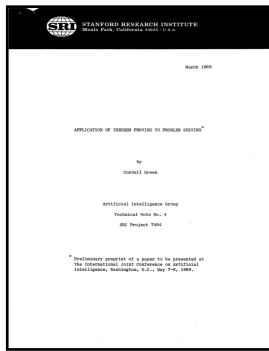
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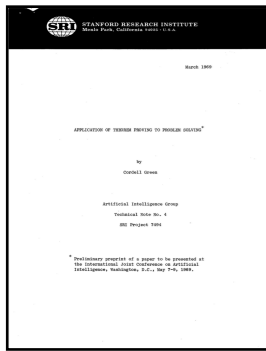


# The Disastrous Disunion

AI

Logic = FOL

Pure (FO)Logic Programming



# The Disastrous Disunion

ML

Logic = FOL

Pure (FO)Logic Programming

# The Disastrous Disunion

ML

**Some Disastrous Consequences ...**

**Disastrous Consequence #1:  
Mindless Procedure is Venerated & Pushed**

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COMMUNICATIONS OF THE ACM March 2006/Vol. 49, No. 3 33

ingrained in everyone's lives when words like algo-  
rithm and precondition are part of everyone's vocab-

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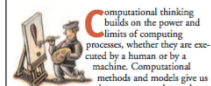
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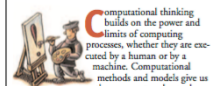
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what problems can be solved,  
 what tasks can be accomplished,  
 and what features of the world can be understood ...

... *computationally*, that is, using a language with only:

2 nouns ('0', '1'),  
 3 verbs ('move', 'print', 'halt'),  
 3 grammar rules (sequence, selection, repetition),  
 and nothing else,

and then to provide algorithms to show how this can be done:

efficiently,  
 practically,  
 physically,  
 and ethically.

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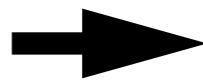
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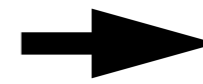
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Computational thinking is using abstraction and decomposition when attacking a large complex task or designing a large complex system. It is separation of concerns. It is choosing an appropriate representation for a problem or modeling the relevant aspects of a problem to make it tractable. It is using invariants to describe a system's behavior succinctly and declaratively. It is having the confidence we can safely use, modify, and influence a large complex system without understanding its every detail. It is

COMMUNICATIONS OF THE ACM March 2006/Vol. 49, No. 3 33



Teach computer programming!  
**(procedural, o-o, functional)**



Computer science is the scientific (or STEM) study of:

what problems can be solved,  
 what tasks can be accomplished,  
 and what features of the world can be understood ...

... *computationally*, that is, using a language with only:

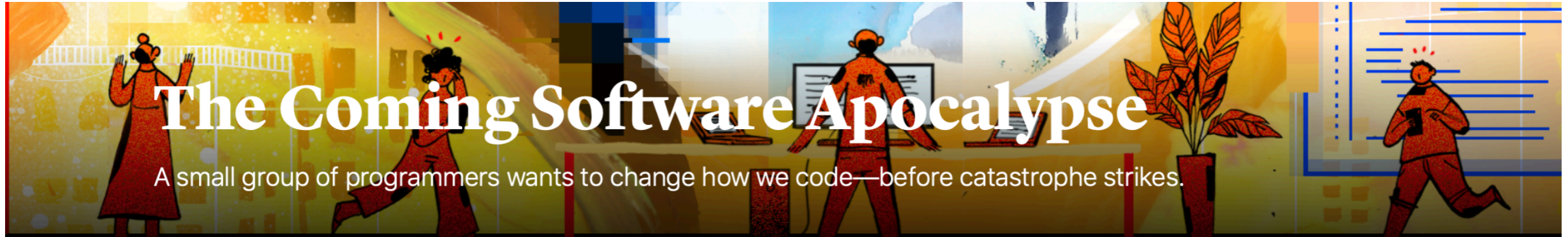
2 nouns ('0', '1'),  
 3 verbs ('move', 'print', 'halt'),  
 3 grammar rules (sequence, selection, repetition),  
 and nothing else,

and then to provide algorithms to show how this can be done:

efficiently,  
 practically,  
 physically,  
 and ethically.

– Rapaport, "phics" book

**Disastrous Consequence #2:  
Impenetrable, Dangerous Code**



# The Coming Software Apocalypse

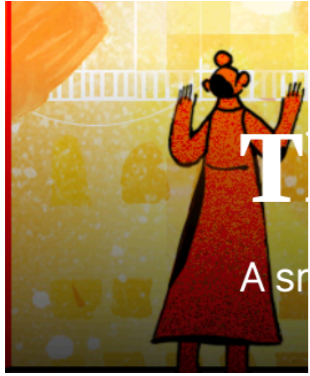
A small group of programmers wants to change how we code—before catastrophe strikes.

In September 2007, Jean Bookout was driving on the highway with her best friend in a Toyota Camry when the accelerator seemed to get stuck. When she took her foot off the pedal, the car didn't slow down. She tried the brakes but they seemed to have lost their power. As she swerved toward an off-ramp going 50 miles per hour, she pulled the emergency brake. The car left a skid mark 150 feet long before running into an embankment by the side of the road. The passenger was killed. Bookout woke up in a hospital a month later.

The incident was one of many in a nearly decade-long investigation into claims of so-called unintended acceleration in Toyota cars. Toyota blamed the incidents on poorly designed floor mats, “sticky” pedals, and driver error, but outsiders suspected that faulty software might be responsible. The National Highway Traffic Safety Administration enlisted software experts from NASA to perform an intensive review of Toyota's code. After nearly 10 months, the NASA team hadn't found evidence that software was the cause—but said they couldn't prove it wasn't.

It was during litigation of the Bookout accident that someone finally found a convincing connection. Michael Barr, an expert witness for the plaintiff, had a team of software experts spend 18 months with the Toyota code, picking up where NASA left off. Barr described what they found as “spaghetti code,” programmer lingo for software that has become a tangled mess. Code turns to spaghetti when it accretes over many years, with feature after feature piling on top of, and being woven around, what's already there; eventually the code becomes impossible to follow, let alone to test exhaustively for flaws.

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**Disastrous Consequence #3:  
Black-Box Machine-Learning  
Machines that Don't Learn  
Anything At All**

Since Plato:

*Knowledge is justified, true belief — where justifications (arguments and proofs) are necessarily based on logic.*

# But Plato has been trampled.

## Do Machine-Learning Machines Learn?

Selmer Bringsjord and Naveen Sundar Govindarajulu and Shreya Banerjee and John Hummel

**Abstract** We answer the present paper's title in the negative. We begin by introducing and characterizing "real learning" ( $\mathcal{RL}$ ) in the formal sciences, a phenomenon that has been firmly in place in homes and schools since at least Euclid. The defense of our negative answer pivots on an integration of *reductio* and proof by cases, and constitutes a general method for showing that any contemporary form of machine learning (ML) isn't real learning. Along the way, we canvass the many different conceptions of "learning" in not only AI, but psychology and its allied disciplines; none of these conceptions (with one exception arising from the view of cognitive development espoused by Piaget), aligns with real learning. We explain in this context by four steps how to broadly characterize and arrive at a focus on  $\mathcal{RL}$ .

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Naveen Sundar Govindarajulu  
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Shreya Banerjee  
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John Hummel  
901 West Illinois Street, Urbana, IL 61801, e-mail: jehummel@illinois.edu

## 8 Appendix: The Formal Method

The following deduction uses fonts in an obvious and standard way to sort between functions ( $f$ ), agents ( $\alpha$ ), and computing machines ( $m$ ) in the Arithmetical Hierarchy. Ordinary italicized Roman is used for particulars under these sorts (e.g.  $f$  is a particular function). In addition, ' $\mathcal{C}$ ' denotes any collection of conditions constituting jointly necessary-and-sufficient conditions for a form of current ML, which can come from relevant textbooks (e.g. Luger, 2008; Russell and Norvig, 2009) or papers; we leave this quite up to the reader, as no effect upon the validity of the deductive inference chain will be produced by the preferred instantiation of ' $\mathcal{C}$ .' It will perhaps be helpful to the reader to point out that the deduction eventuates in the proposition that no machine in the ML fold that in this style learns a relevant function  $f$  thereby also real-learns  $f$ . We encode this target as follows:

$$(\star) \neg \exists m \exists f [\phi := MLlearns(m, f) \wedge \psi := RLearns(m, f) \wedge \mathcal{C}_\phi(m, f) \vdash^* (ci')\text{--}(ciii)_\psi(m, f)]$$

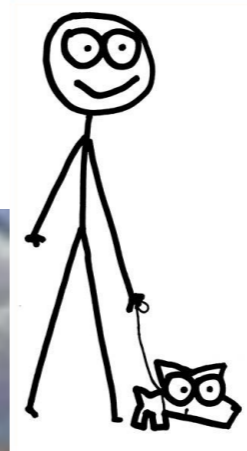
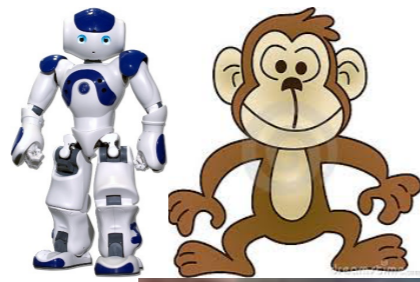
Note that  $(\star)$  employs meta-logical machinery to refer to particular instantiations of  $\mathcal{C}$  for a particular, arbitrary case of ML ( $\phi$  is the atomic sub-formula that can be instantiated to make the particular case), and particular instantiations of the triad  $(ci')\text{--}(ciii)$  for a particular, arbitrary case of  $\mathcal{RL}$  ( $\psi$  is the atomic sub-formula that can be instantiated to make the particular case). Meta-logical machinery also allows us to use a provability predicate to formalize the notion that real learning is produced by the relevant instance of ML. If we "pop"  $\phi/\psi$  to yield  $\phi'/\psi'$  we are dealing with the particular instantiation of the atomic sub-formula.

The deduction, as noted in earlier when the informal argument was given, is indirect proof by cases; accordingly, we first assume  $\neg(\star)$ , and then proceed as follows under this supposition.

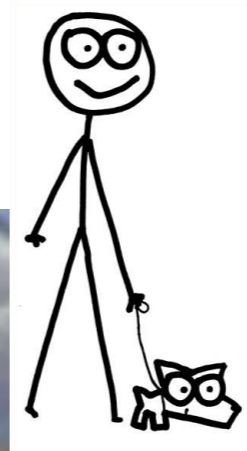
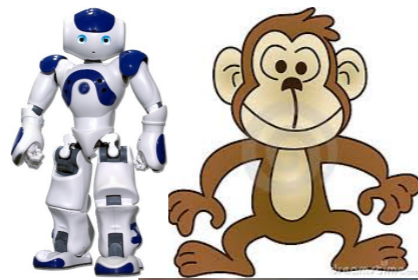
(1)	$\forall f, \alpha [f : \mathbb{N} \mapsto \mathbb{N} \rightarrow (RLearns(\alpha, f) \rightarrow (i)\text{--}(iii))]$	Def of Real Learning
(2)	$MLlearns(m, f) \wedge RLearns(m, f) \wedge f : \mathbb{N} \mapsto \mathbb{N}$	supp (for $\exists$ elim on $(\star)$ )
(3)	$\forall m, f [f : \mathbb{N} \mapsto \mathbb{N} \rightarrow (MLlearns(m, f) \leftrightarrow \mathcal{C}(m, f))]$	Def of ML
(4)	$\forall f [f : \mathbb{N} \mapsto \mathbb{N} \rightarrow (TurComp(f) \vee TurUncomp(f))]$	theorem
(5)	$TurUncomp(f)$	supp; Case 1
(6)	$\neg \exists m \exists f [(f : \mathbb{N} \mapsto \mathbb{N} \wedge TurUncomp(f) \wedge \mathcal{C}(m, f))]$	theorem
$\therefore$ (7)	$\neg \exists m MLlearns(m, f)$	(6), (3)
$\therefore$ (8)	$\perp$	(7), (2)
(9)	$TurComp(f)$	supp; Case 2
$\therefore$ (10)	$\mathcal{C}_{\phi'}(m, f)$	(2), (3)
$\therefore$ (11)	$(ci')\text{--}(ciii)_{\psi'}(m, f)$	from supp for $\exists$ elim on $(\star)$ and provability
$\therefore$ (12)	$\neg (ci')\text{--}(ciii)_{\psi'}(m, f)$	inspection: proofs wholly absent from $\mathcal{C}$
$\therefore$ (13)	$\perp$	(11), (12)
$\therefore$ (14)	$\perp$	<i>reductio</i> ; proof by cases

**Disastrous Consequence #4:  
Animal-level AI; AI Chained to Earth**

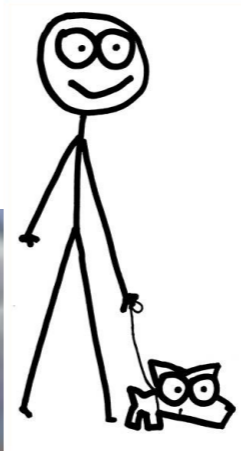
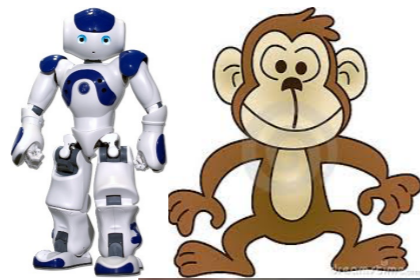
# The Canyon of Discontinuity (or Darwin's Dread)



# The Canyon of Discontinuity (or Darwin's Dread)

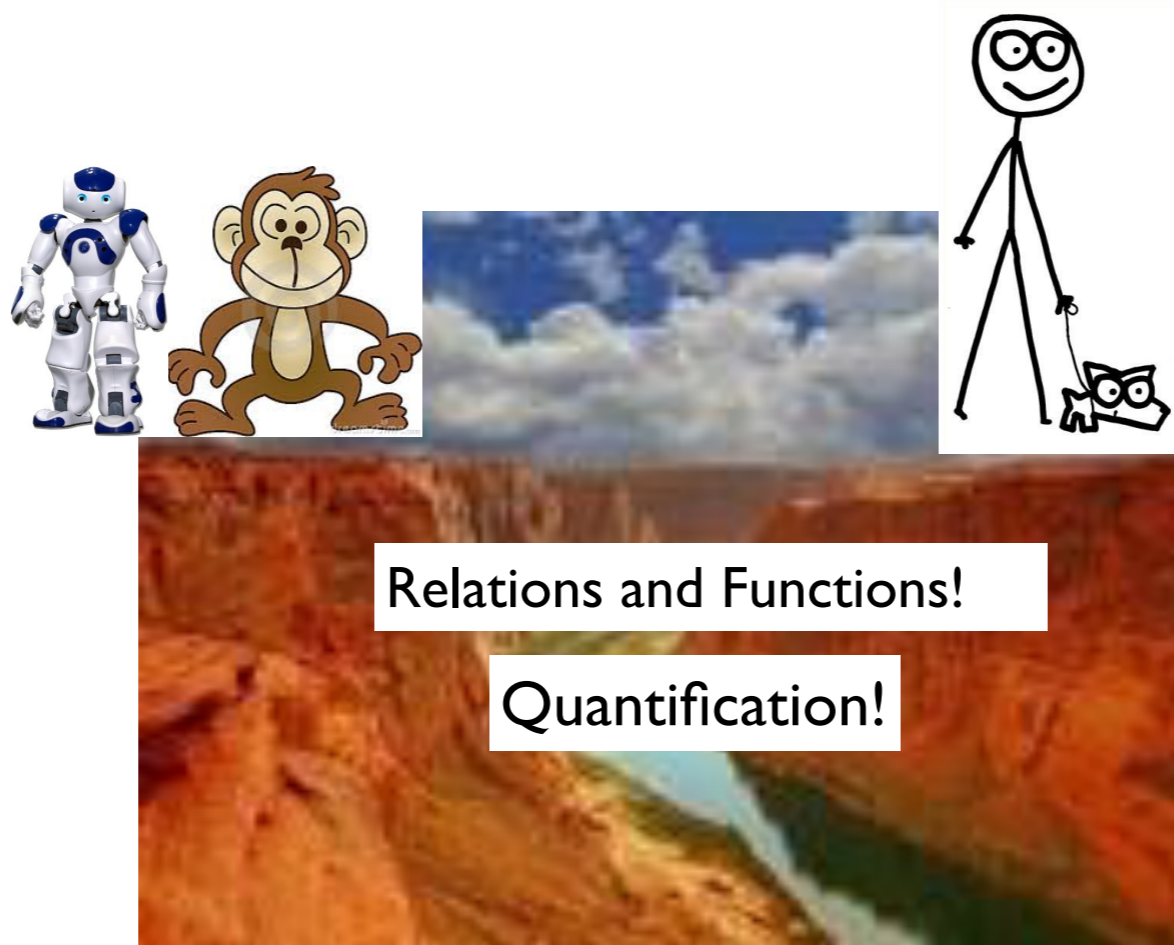


# The Canyon of Discontinuity (or Darwin's Dread)



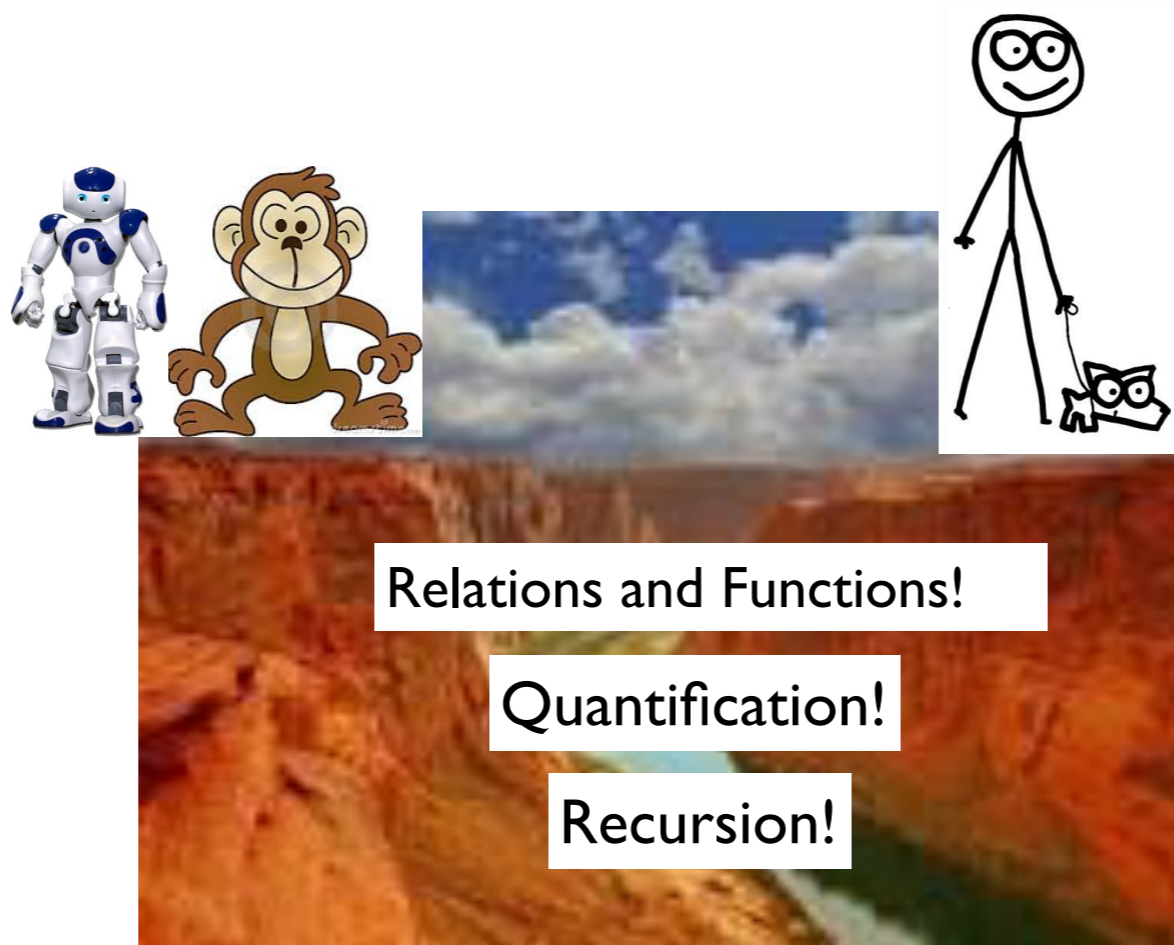
Relations and Functions!

# The Canyon of Discontinuity (or Darwin's Dread)

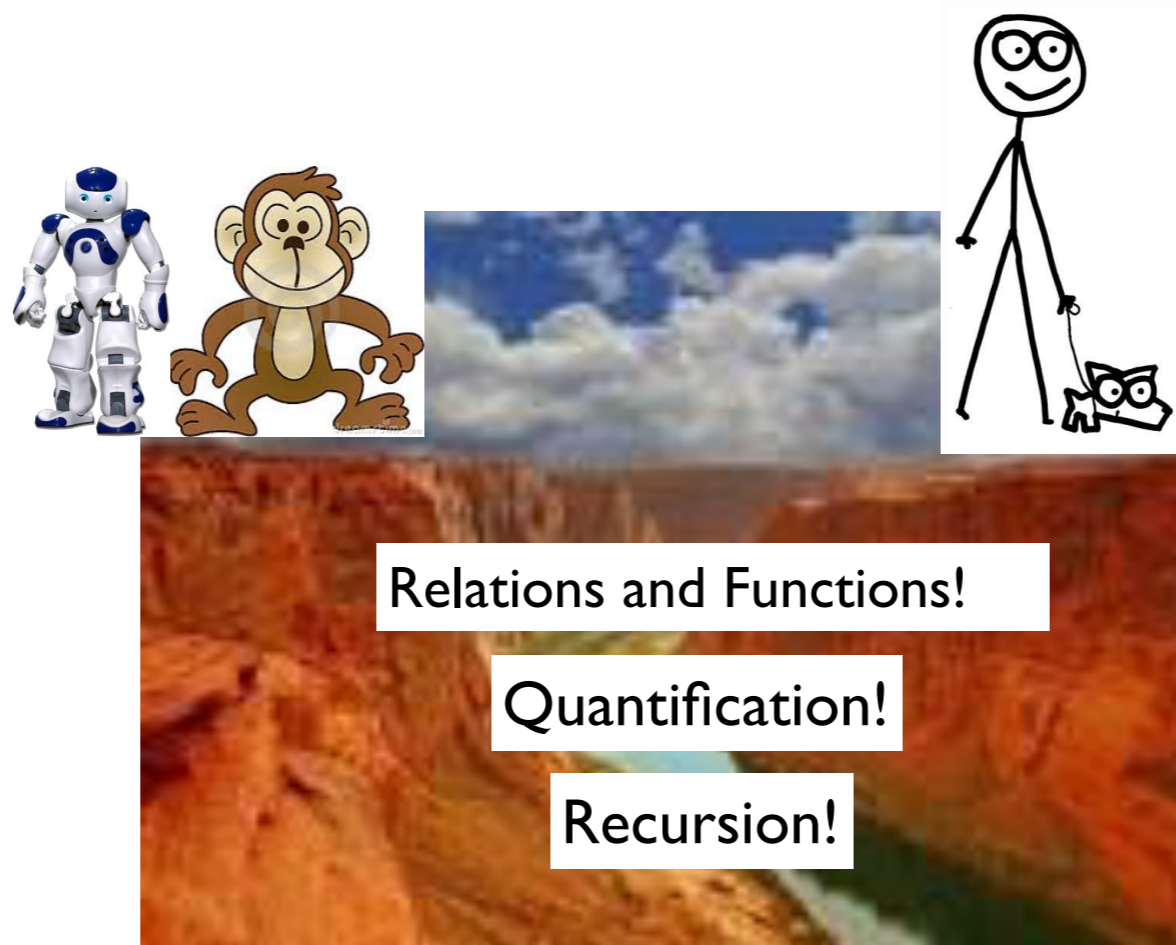




# The Canyon of Discontinuity (or Darwin's Dread)



# The Canyon of Discontinuity (or Darwin's Dread)



(Interesting paper:  
[http://idiom.ucsd.edu/~ivano/SemBabble\\_old/LogicSeminar\\_15W/Material/Partee\\_2013\\_History-of-Quantifiers.pdf](http://idiom.ucsd.edu/~ivano/SemBabble_old/LogicSeminar_15W/Material/Partee_2013_History-of-Quantifiers.pdf).)

# The Canyon of Discontinuity (or Darwin's Dread)



# Quantification!



(Interesting paper:

[http://idiom.ucsd.edu/~ivano/SemBabble\\_old/LogicSeminar\\_15W/Material/Partee\\_2013\\_History-of-Quantifiers.pdf](http://idiom.ucsd.edu/~ivano/SemBabble_old/LogicSeminar_15W/Material/Partee_2013_History-of-Quantifiers.pdf).)

# Karkooking Problem ...

Everyone karkooks anyone who karkooks someone.

Alvin karkooks Bill.

Can you infer that everyone karkooks Bill?

ANSWER:

JUSTIFICATION:

# Karkooking Problem ...

Everyone karkooks anyone who karkooks someone.

**Relations and Functions!**

Alvin karkooks Bill.

**Quantification!**

Can you infer that everyone karkooks Bill?

ANSWER: **Recursion!**

JUSTIFICATION:

# Animal-Level AI

*Super-Serious Human Cognitive Power*

*Serious Human Cognitive Power*

Mere Calculative Cognitive Power

**Entscheidungsproblem**

# Animal-Level AI

Analytical Hierarchy

*Serious Human Cognitive Power*

Mere Calculative Cognitive Power

**Entscheidungsproblem**

# Animal-Level AI

Analytical Hierarchy

Arithmetical Hierarchy

**Entscheidungsproblem**

Mere Calculative Cognitive Power



# Animal-Level AI

Analytical Hierarchy

Arithmetical Hierarchy

Polynomial Hierarchy

**Entscheidungsproblem**

# Animal-Level AI

Analytical Hierarchy

Arithmetical Hierarchy

**Entscheidungsproblem**

Polynomial Hierarchy

$P \subseteq NP \subseteq PSPACE = NPSpace \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$

# Animal-Level AI

## Analytical Hierarchy

### Arithmetical Hierarchy

$\vdots$   
 $\Pi_2$   
 $\Sigma_2$   
 $\Pi_1$   
 $\Sigma_1$   
 $\Sigma_0$

**Entscheidungsproblem**

### Polynomial Hierarchy

$P \subseteq NP \subseteq PSPACE = NPSpace \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$

# Animal-Level AI

## Analytical Hierarchy

### Arithmetical Hierarchy

Go:AlphaGo



⋮  
 $\Pi_2$   
 $\Sigma_2$   
 $\Pi_1$   
 $\Sigma_1$   
 $\Sigma_0$

**Entscheidungsproblem**

### Polynomial Hierarchy

$P \subseteq NP \subseteq PSPACE = NPSpace \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$

# Animal-Level AI

## Analytical Hierarchy

### Arithmetical Hierarchy

*Jeopardy!:* **Watson**

Go: AlphaGo



⋮  
 $\Pi_2$   
 $\Sigma_2$   
 $\Pi_1$   
 $\Sigma_1$   
 $\Sigma_0$

**Entscheidungsproblem**

### Polynomial Hierarchy

$P \subseteq NP \subseteq PSPACE = NPSpace \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$

# Animal-Level AI

## Analytical Hierarchy

### Arithmetical Hierarchy

Chess: Deep Blue



Jeopardy!: **Watson**



Go: AlphaGo



⋮  
 $\Pi_2$   
 $\Sigma_2$   
 $\Pi_1$   
 $\Sigma_1$   
 $\Sigma_0$

**Entscheidungsproblem**

### Polynomial Hierarchy

$P \subseteq NP \subseteq PSPACE = NPSpace \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$

# Animal-Level AI

## Analytical Hierarchy

### Arithmetical Hierarchy

Checkers: Chinook



Chess: Deep Blue



Jeopardy!: **Watson**



Go: AlphaGo



⋮  
 $\Pi_2$   
 $\Sigma_2$   
 $\Pi_1$   
 $\Sigma_1$   
 $\Sigma_0$

**Entscheidungsproblem**

### Polynomial Hierarchy

$P \subseteq NP \subseteq PSPACE = NPSpace \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$

# Animal-Level AI

## Analytical Hierarchy

### Arithmetical Hierarchy

⋮  
 $\Pi_2$   
 $\Sigma_2$   
 $\Pi_1$   
 $\Sigma_1$   
 $\Sigma_0$

**Entscheidungsproblem**

### Polynomial Hierarchy

Jeopardy!: **Watson**

Chess: Deep Blue  
Checkers: Chinook  
Go: AlphaGo

$P \subseteq NP \subseteq PSPACE = NPSPACE \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$



# Animal-Level AI

## Analytical Hierarchy

### Arithmetical Hierarchy

⋮  
 $\Pi_2$   
 $\Sigma_2$   
 $\Pi_1$   
 $\Sigma_1$   
 $\Sigma_0$

**Entscheidungsproblem**

### Polynomial Hierarchy

Jeopardy!: **Watson**

Chess: Deep Blue  
Go: AlphaGo  
Checkers: Chinook



$P \subseteq NP \subseteq PSPACE = NPSpace \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$

# Animal-Level AI

## Analytical Hierarchy

### Arithmetical Hierarchy



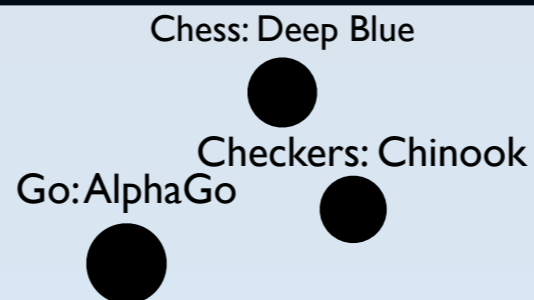
Church

⋮  
 $\Pi_2$   
 $\Sigma_2$   
 $\Pi_1$   
 $\Sigma_1$   
 $\Sigma_0$

**Entscheidungsproblem**

### Polynomial Hierarchy

Jeopardy!: **Watson**



$P \subseteq NP \subseteq PSPACE = NPSPACE \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$

# Animal-Level AI

## Analytical Hierarchy

### Arithmetical Hierarchy



Church



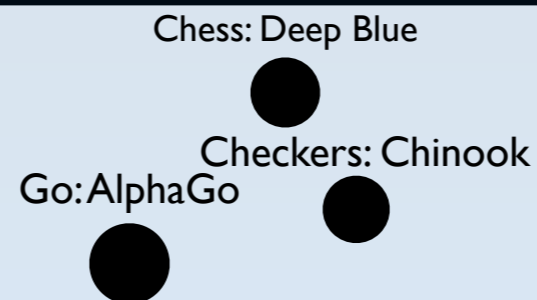
Turing

⋮  
 $\Pi_2$   
 $\Sigma_2$   
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 $\Sigma_0$

**Entscheidungsproblem**

### Polynomial Hierarchy

Jeopardy!: **Watson**

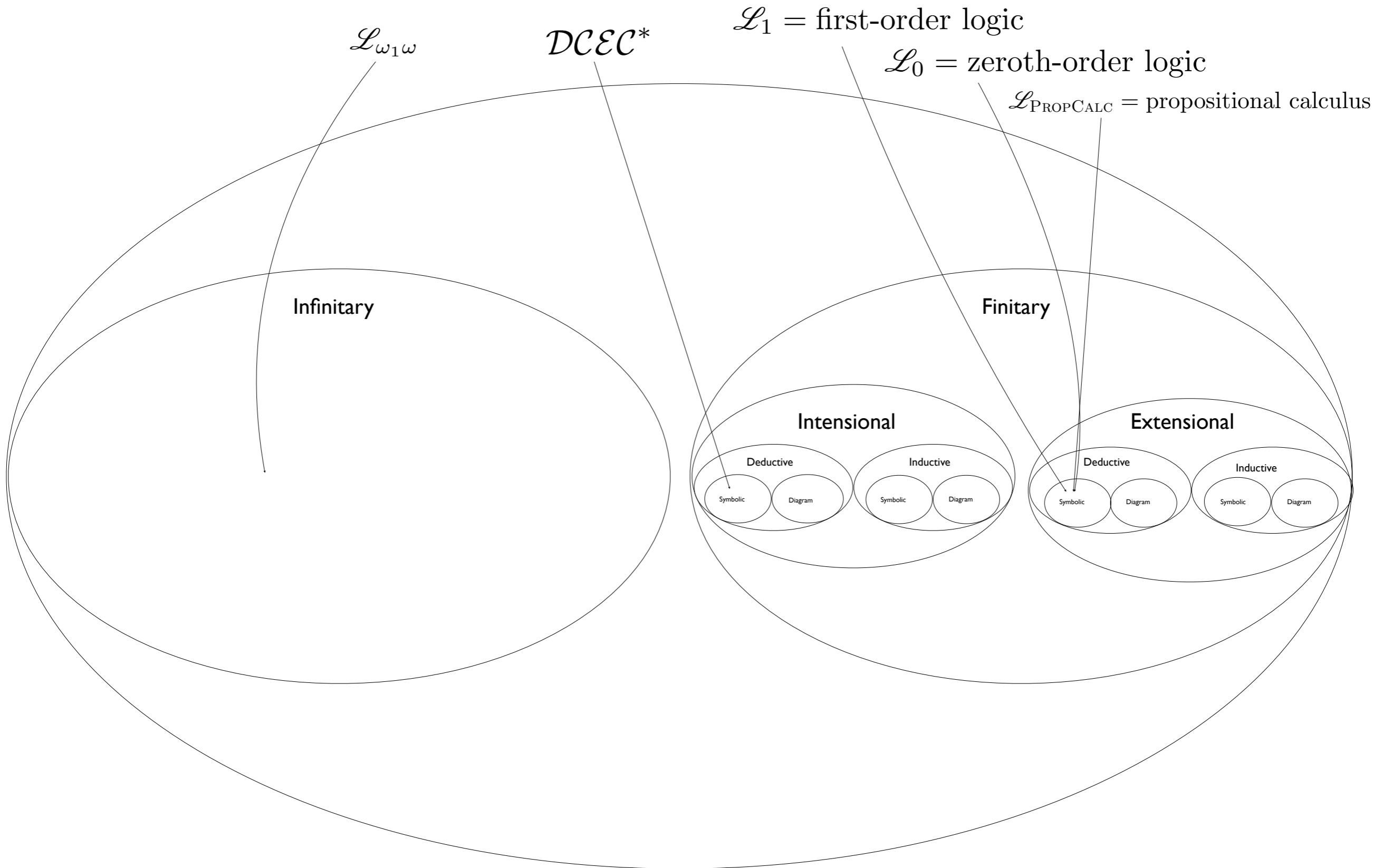


$P \subseteq NP \subseteq PSPACE = NPSPACE \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$

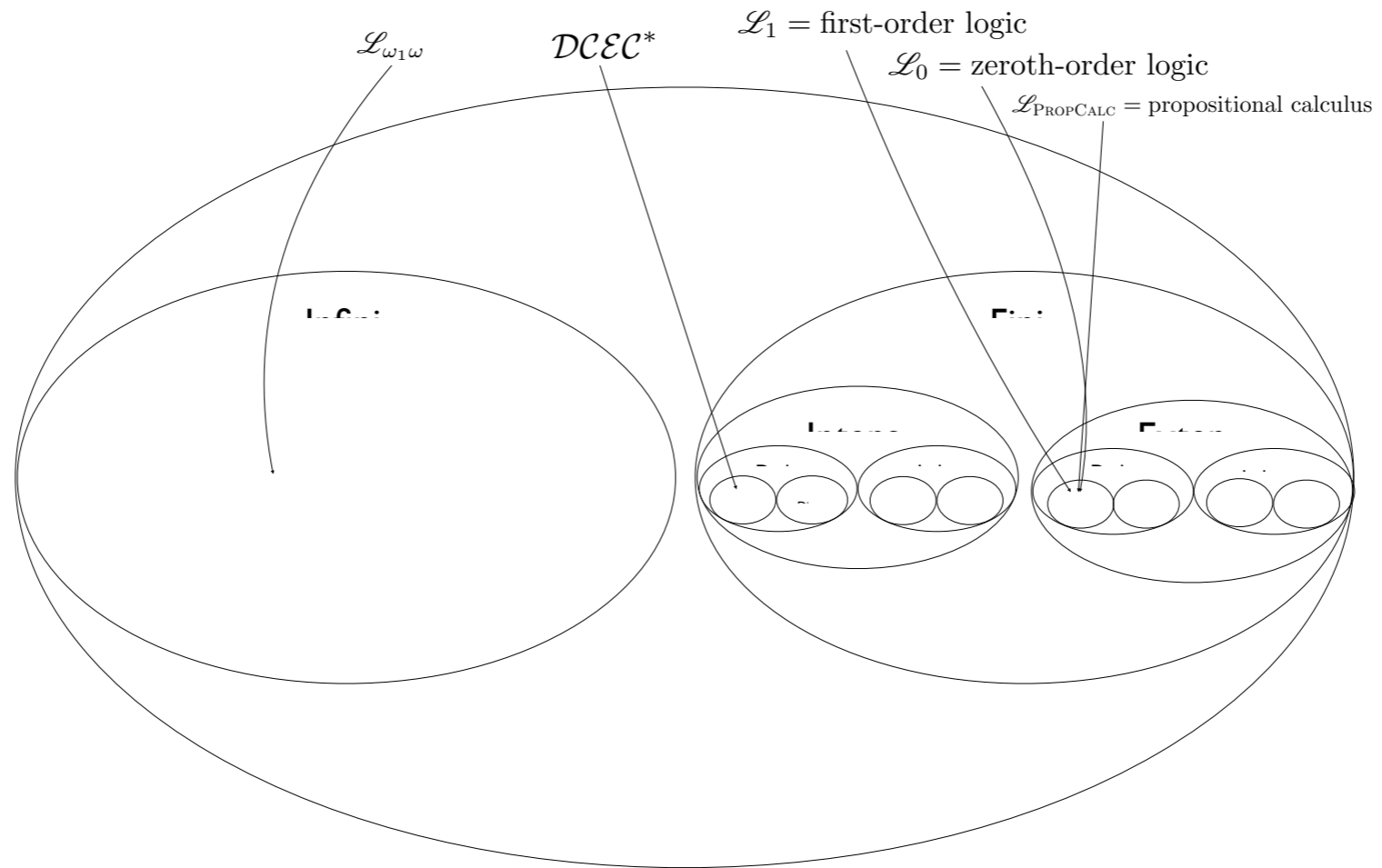
**But what are the three things, in  
The Terrific Triad, exactly?**

**Logic ...**

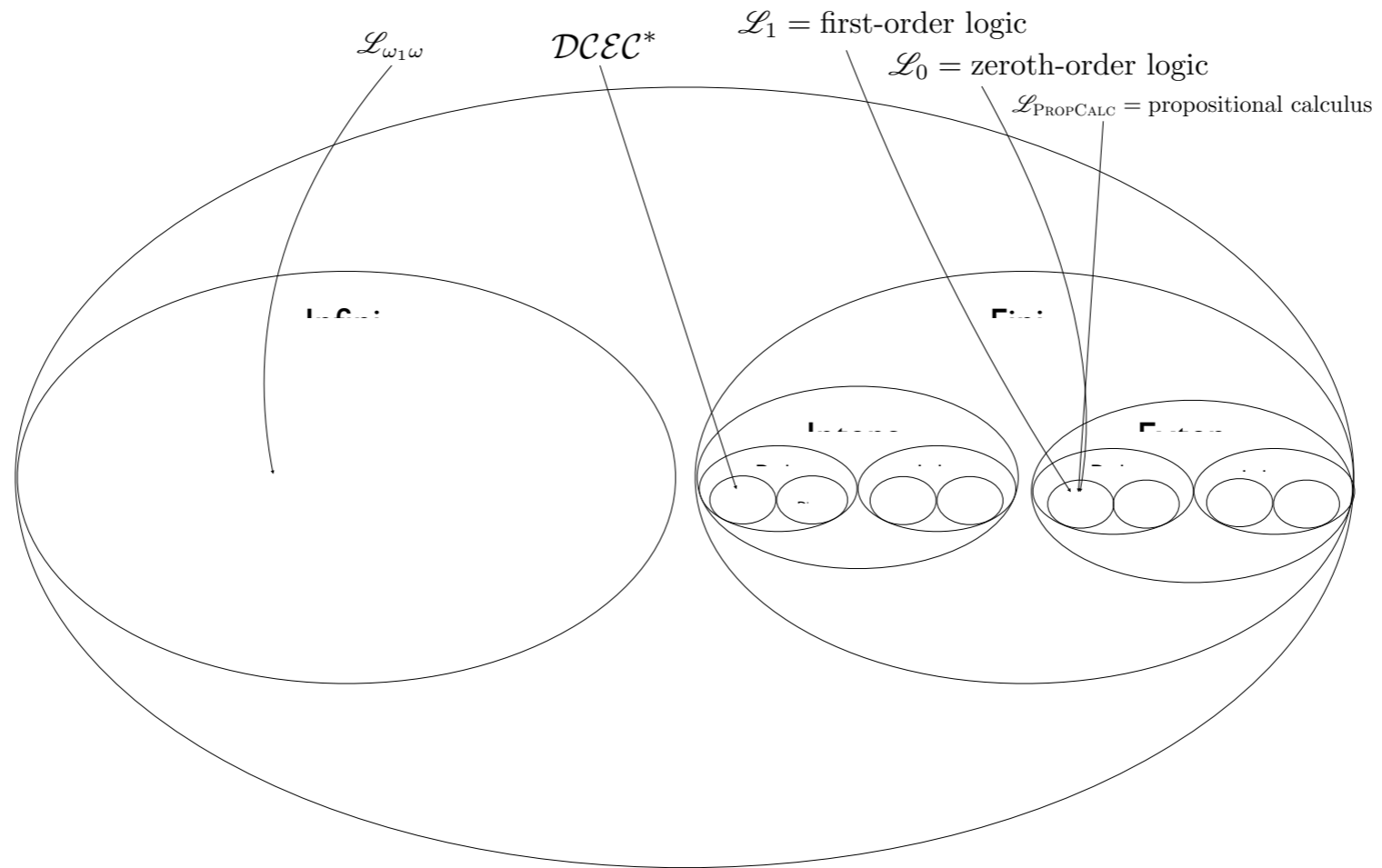
# The Universe of Logics



# The Universe of Logics



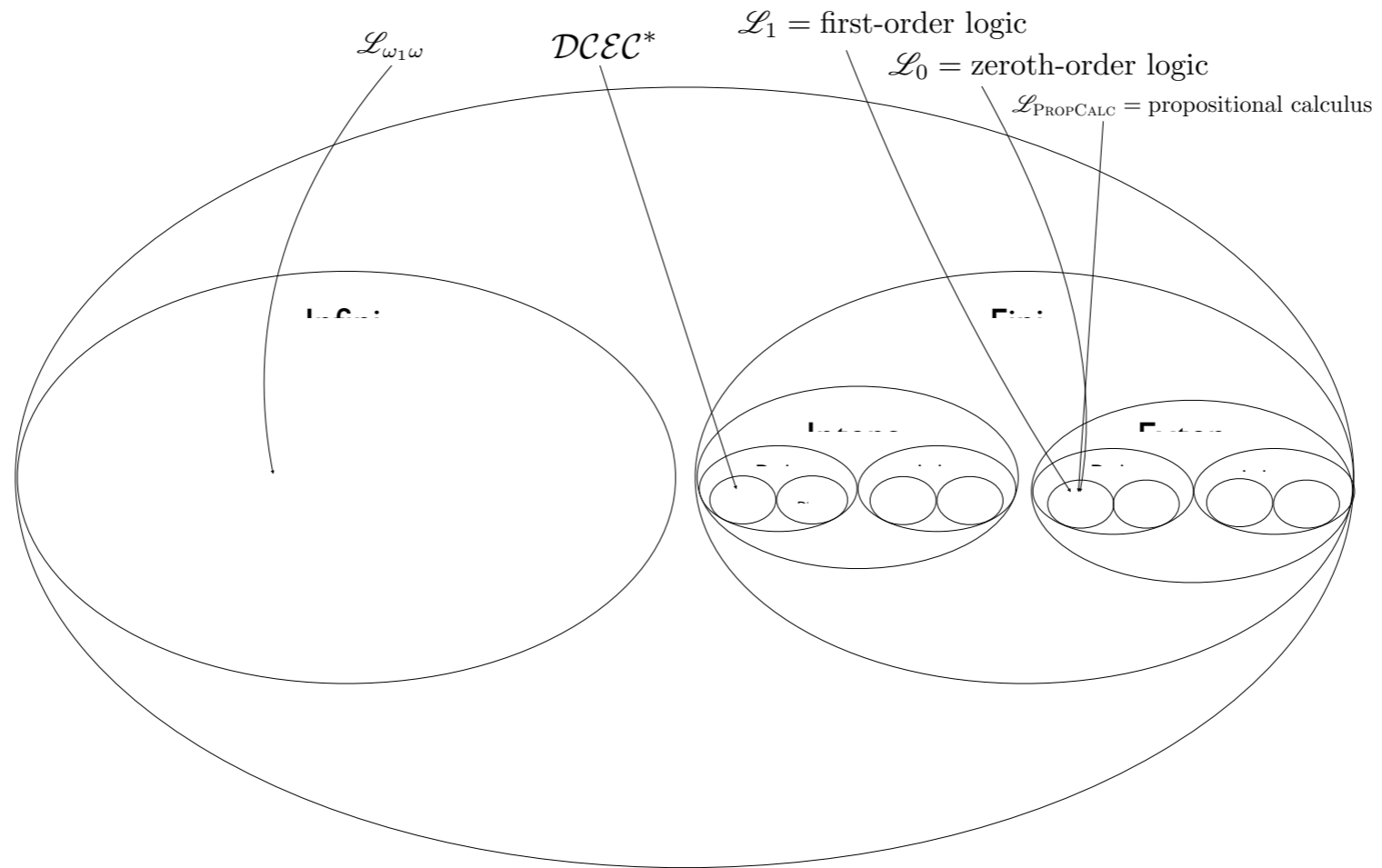
# The Universe of Logics



$$\mathcal{L} := \langle L, I, S \rangle$$



# The Universe of Logics



$$\mathcal{L} := \langle L, I, S \rangle$$

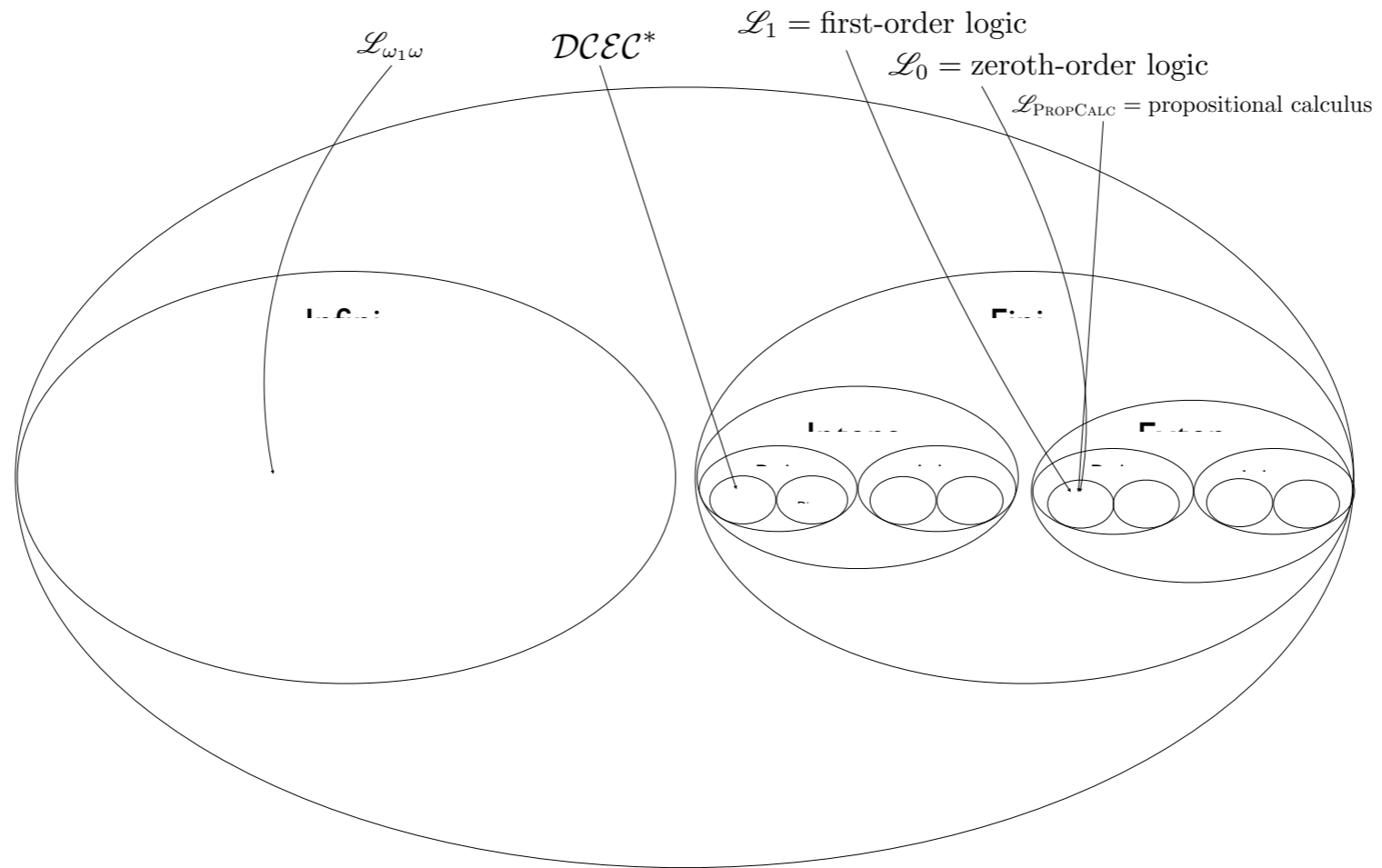
the logic

formal language

inference schemata

semantics

# The Universe of Logics



$$\mathcal{L} := \langle L, I, \rangle$$

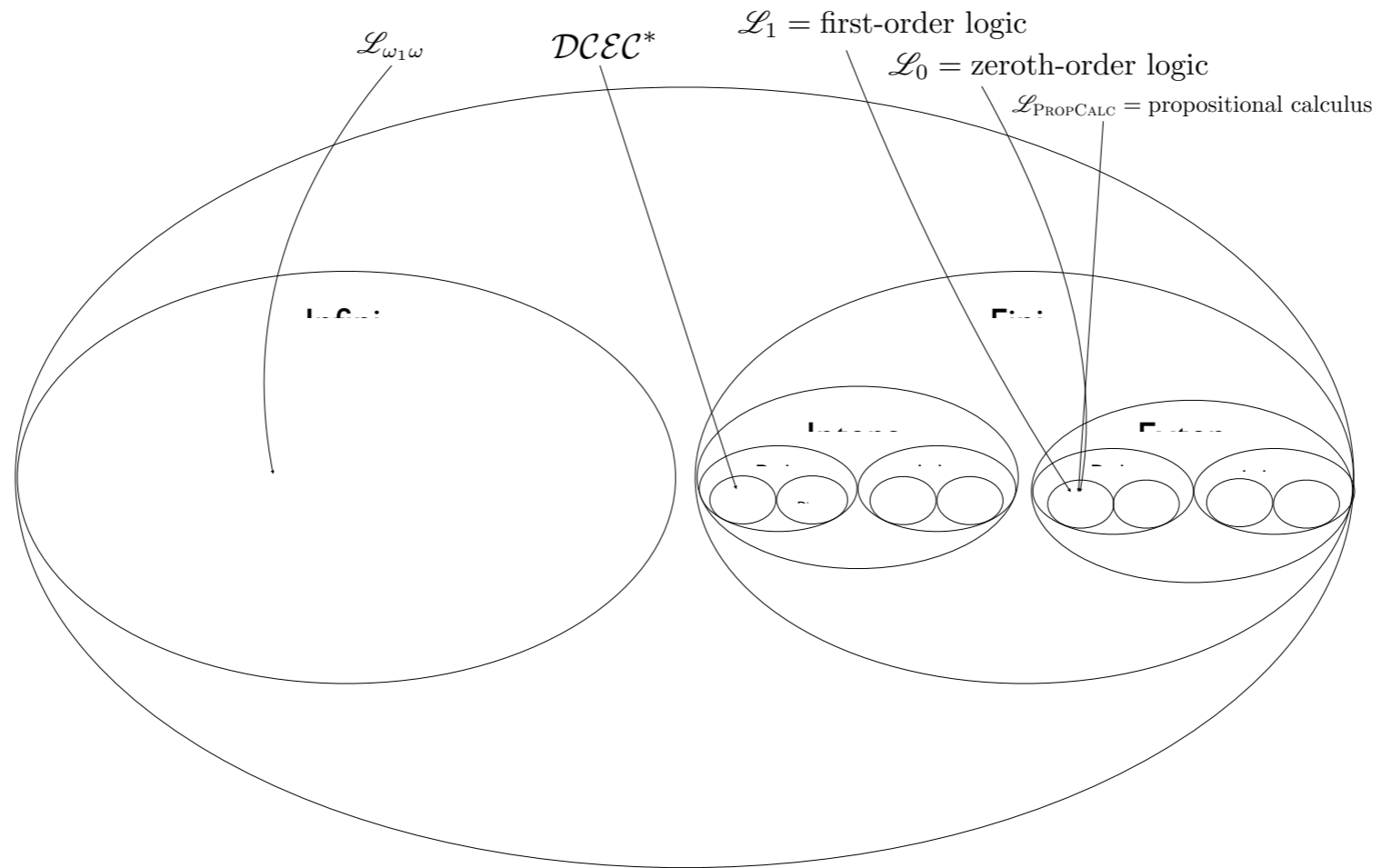
the logic

formal language

inference schemata

semantics

# The Universe of Logics



$$\mathcal{L} := \langle L, I, \rangle$$

the logic

formal language

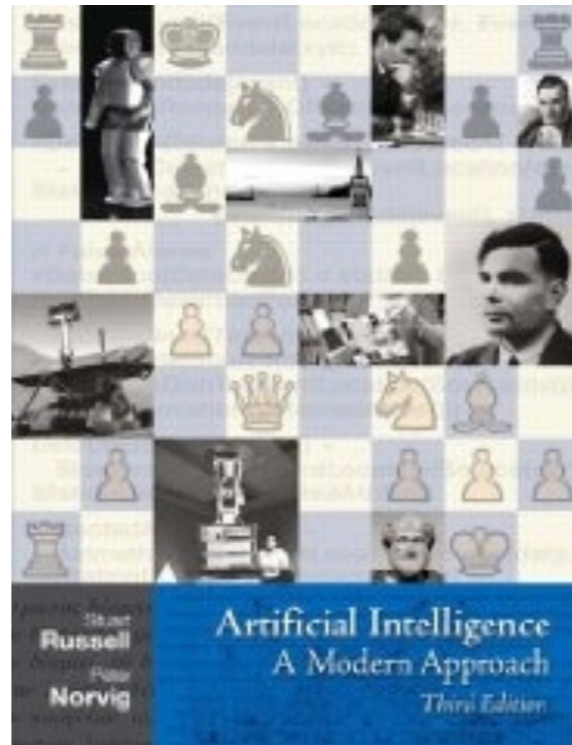
inference schemata

semantics

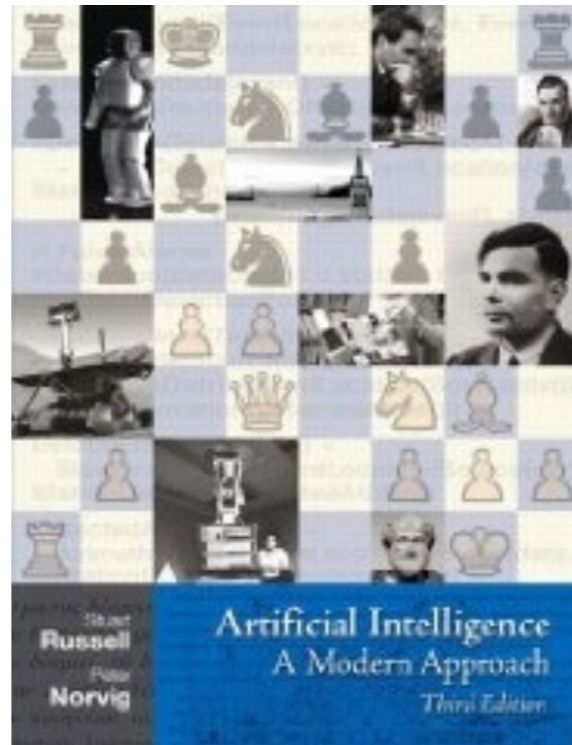
AI ...

Al:

# AI:



# AI:



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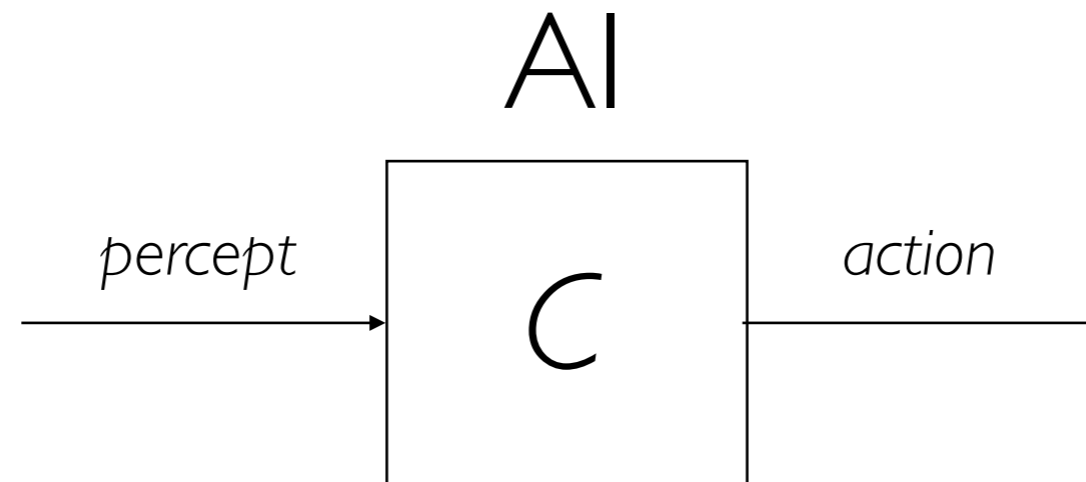
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## Artificial Intelligence

*First published Thu Jul 12, 2018*

Artificial intelligence (AI) is the field devoted to building artificial animals (or at least artificial creatures that – in suitable contexts – *appear* to be animals) and, for many, artificial persons (or at least artificial creatures that – in suitable contexts – *appear* to be persons).<sup>[1]</sup> Such goals immediately ensure that AI is a discipline of considerable interest to many philosophers, and this has been confirmed (e.g.) by the energetic attempt, on the part of numerous philosophers, to show that these goals are in fact un/attainable. On the constructive side, many of the core formalisms and techniques used in AI come out of, and are indeed still much used and refined in, philosophy: first-order logic and its extensions; intensional logics suitable for the modeling of doxastic attitudes and deontic reasoning; inductive logic, probability theory, and probabilistic reasoning; practical reasoning and planning, and so on. In light of this, some philosophers conduct AI research and development *as* philosophy.

# AI:



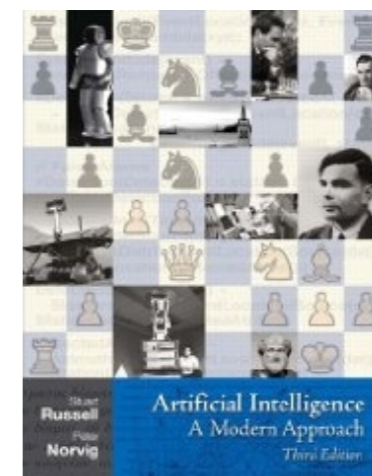
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### Artificial Intelligence

First published Thu Jul 12, 2018

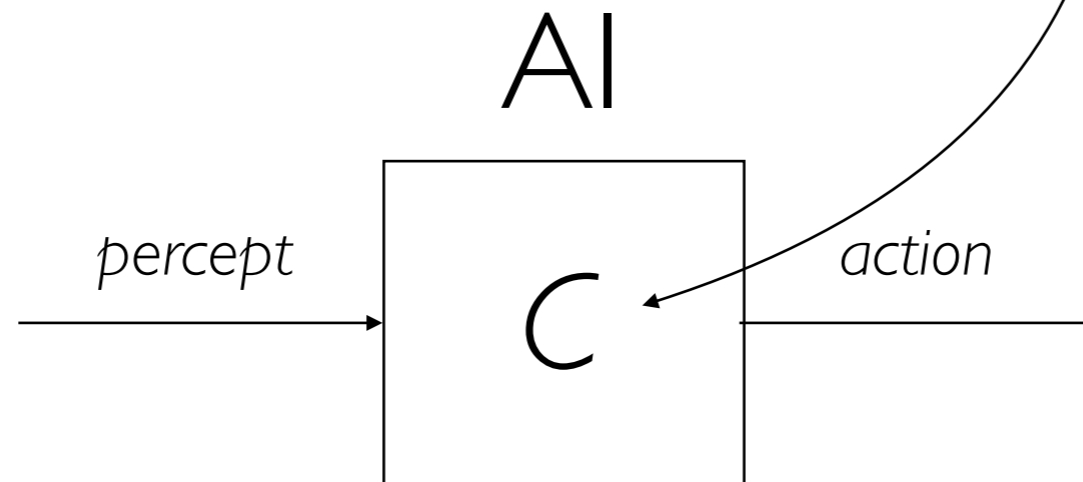
Artificial intelligence (AI) is the field devoted to building artificial animals (or at least artificial creatures that – in suitable contexts – *appear* to be animals) and, for many, artificial persons (or at least artificial creatures that – in suitable contexts – *appear* to be persons).<sup>[1]</sup> Such goals immediately ensure that AI is a discipline of considerable interest to many philosophers, and this has been confirmed (e.g.) by the energetic attempt, on the part of numerous philosophers, to show that these goals are in fact unattainable. On the constructive side, many of the core formalisms and techniques used in AI come out of, and are indeed still much used and refined in, philosophy: first-order logic and its extensions; intensional logics suitable for the modeling of doxastic attitudes and deontic reasoning; inductive logic, probability theory, and probabilistic reasoning; practical reasoning and planning, and so on. In light of this, some philosophers conduct AI research and development *as* philosophy.





# AI:

A (Turing-level) entity that computes.



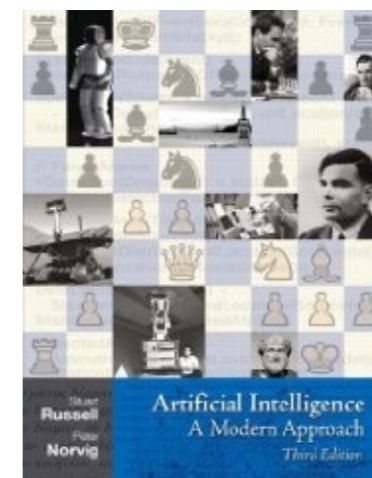
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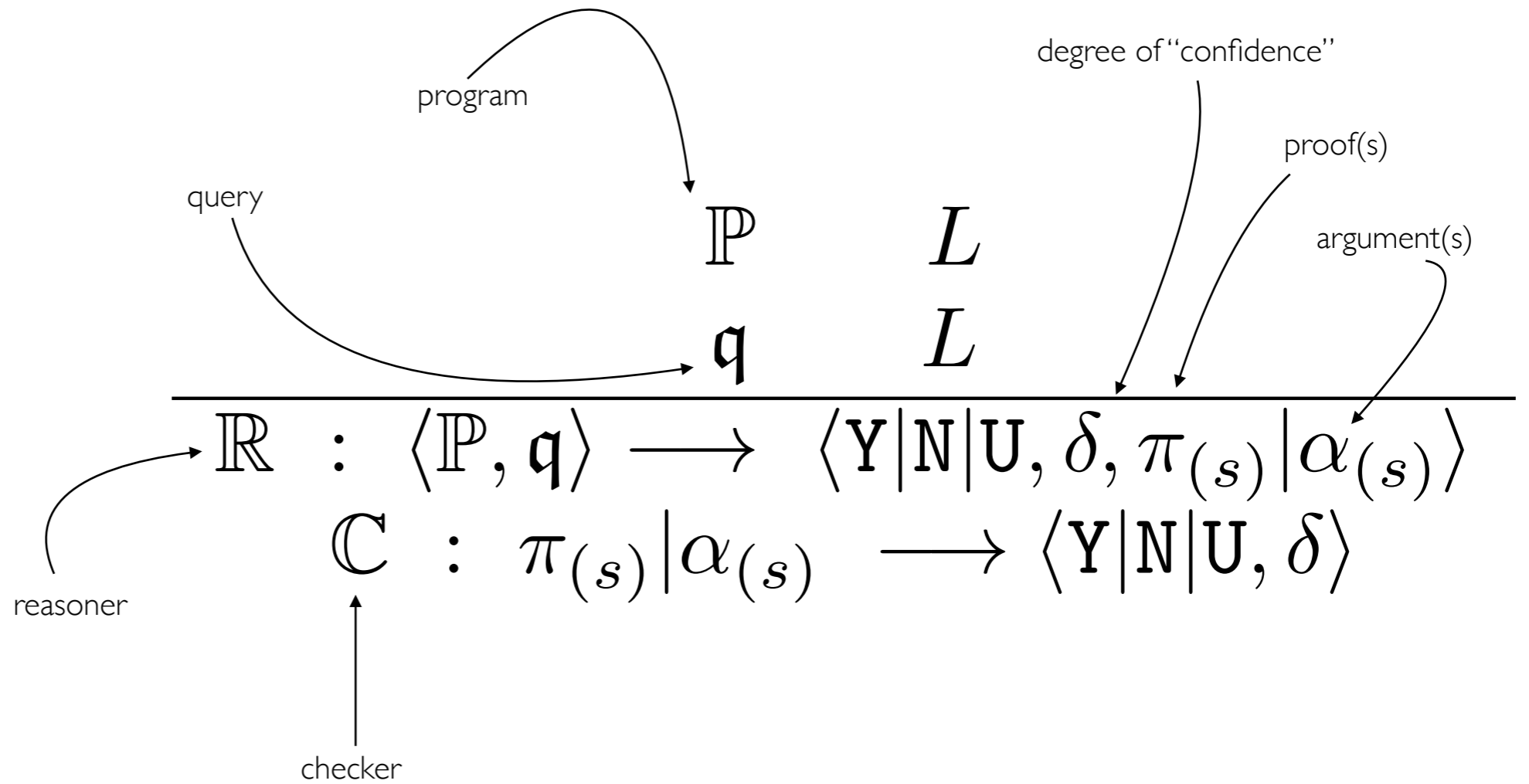


**(Pure General) Logic Programming ...**

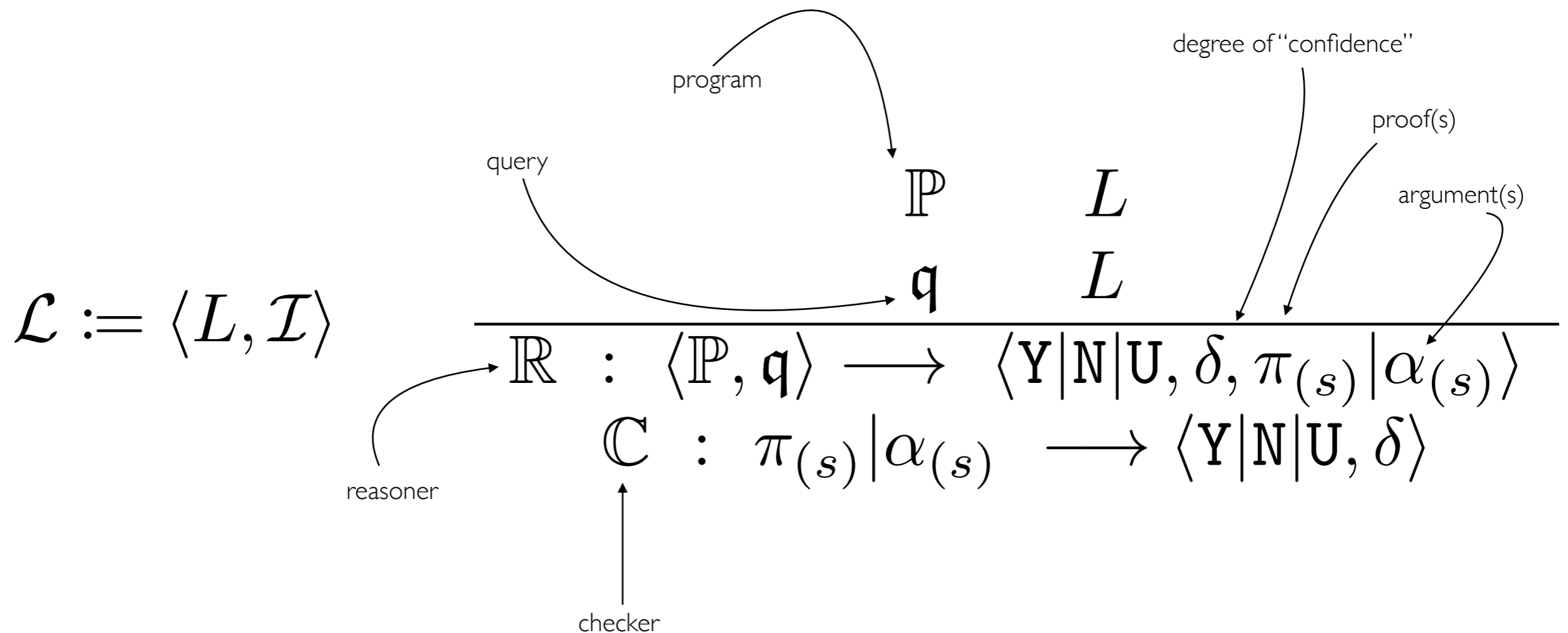
$$\mathcal{L} := \langle L, \mathcal{I} \rangle$$

$$\begin{array}{ccc}
 & \mathbb{P} & L \\
 & \mathfrak{q} & L \\
 \hline
 \mathbb{R} & : \langle \mathbb{P}, \mathfrak{q} \rangle \longrightarrow & \langle Y|N|U, \delta, \pi_{(s)} | \alpha_{(s)} \rangle \\
 \mathbb{C} & : \pi_{(s)} | \alpha_{(s)} \longrightarrow & \langle Y|N|U, \delta \rangle
 \end{array}$$

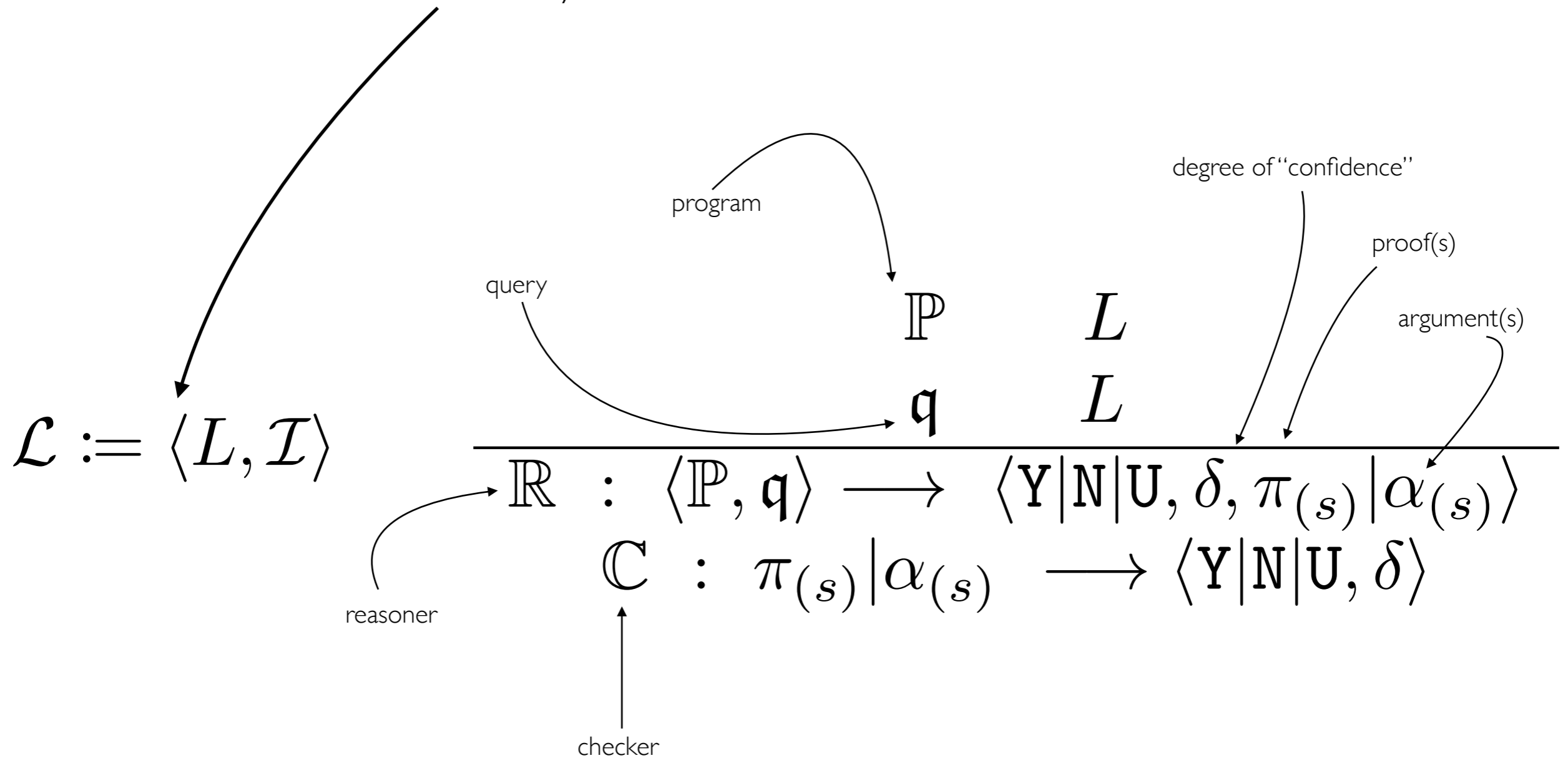
$$\mathcal{L} := \langle L, \mathcal{I} \rangle$$



For just “logic programming,” and a vintage approach that goes back to circa 1970, restrict this to a FOL or a fragment thereof, and use resolution as the only inference schema.



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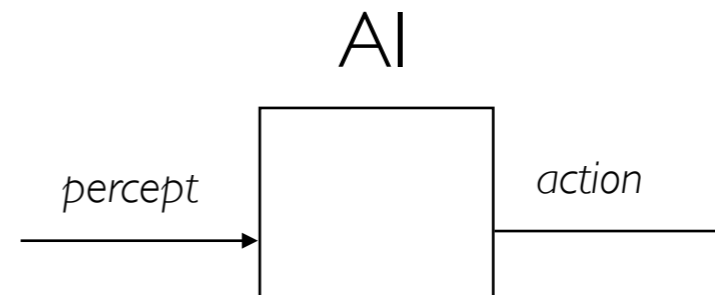


# Resurrection of The Terrific Triad

...

# The Triad Resurrected & Rebuilt, & Better

Logic  
 $\mathcal{L}$



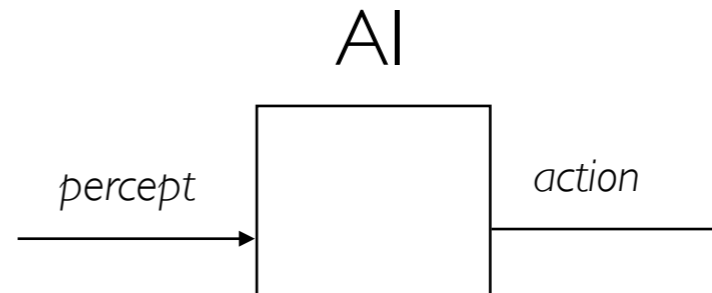
$$\mathcal{L} := \langle L, \mathcal{I} \rangle \quad \frac{\begin{array}{c} \mathbb{P} \quad L \\ \mathbf{q} \quad L \end{array}}{\begin{array}{l} \mathbb{R} : \langle \mathbb{P}, \mathbf{q} \rangle \longrightarrow \langle \mathbf{Y}|\mathbf{N}|\mathbf{U}, \delta, \pi_{(s)}|\alpha_{(s)} \rangle \\ \mathbb{C} : \pi_{(s)}|\alpha_{(s)} \longrightarrow \langle \mathbf{Y}|\mathbf{N}|\mathbf{U}, \delta \rangle \end{array}}$$

Pure General Logic Programming



# The Triad Resurrected & Rebuilt, & Better

Logic  
 $\mathcal{L}$

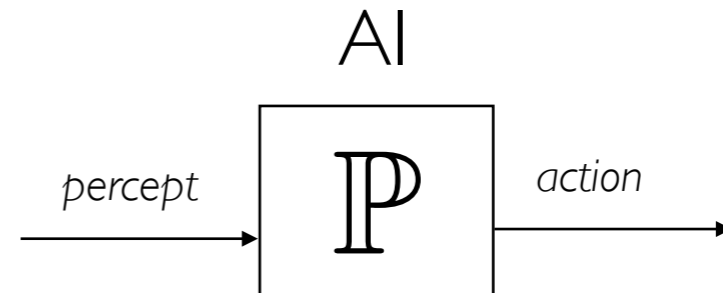


$$\mathcal{L} := \langle L, \mathcal{I} \rangle \quad \frac{\begin{array}{c} \mathbb{P} \quad L \\ \mathbf{q} \quad L \end{array}}{\begin{array}{l} \mathbb{R} : \langle \mathbb{P}, \mathbf{q} \rangle \longrightarrow \langle \mathbf{Y}|\mathbf{N}|\mathbf{U}, \delta, \pi_{(s)}|\alpha_{(s)} \rangle \\ \mathbb{C} : \pi_{(s)}|\alpha_{(s)} \longrightarrow \langle \mathbf{Y}|\mathbf{N}|\mathbf{U}, \delta \rangle \end{array}}$$

Pure General Logic Programming

# The Triad Resurrected & Rebuilt, & Better

Logic  
 $\mathcal{L}$



$$\mathcal{L} := \langle L, \mathcal{I} \rangle \quad \frac{\begin{array}{cc} \mathbb{P} & L \\ \mathbf{q} & L \end{array}}{\begin{array}{l} \mathbb{R} : \langle \mathbb{P}, \mathbf{q} \rangle \longrightarrow \langle \mathbf{Y}|\mathbf{N}|\mathbf{U}, \delta, \pi_{(s)}|\alpha_{(s)} \rangle \\ \mathbb{C} : \pi_{(s)}|\alpha_{(s)} \longrightarrow \langle \mathbf{Y}|\mathbf{N}|\mathbf{U}, \delta \rangle \end{array}}$$

Pure General Logic Programming



*Og med det .. er vårt klasse møte ferdig!*