Logic, AI, and Tax Technology

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Intermediate Formal Logic & AI (IFLAI2) 10/30/2023



Al in the News

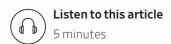
Biden to Use Emergency Powers to Mitigate AI Risks

Executive order seeks to manage artificialintelligence threats from privacy to national security



President Biden has identified AI regulation as a priority for his administration. (Photo: AI Drago/Bloomberg News)

By John D. McKinnon + Follow, Sabrina
Siddiqui + Follow and Dustin Volz + Follow
Oct 30, 2023 05:00 a.m. ET



WASHINGTON—The Biden administration plans to invoke emergency federal powers as part of a new executive order aimed at reining in the risks of artificial intelligence, a new technology as WASHINGTON—The Biden administration plans to invoke emergency federal powers as part of a new executive order aimed at reining in the risks of artificial intelligence, a new technology as powerful as it is potentially disruptive.

President Biden will release on Monday an order invoking the Korean War-era Defense
Production Act which would compel major AI companies to notify the government when developing any system that poses a "serious risk to national security, national economic security

SB BILLY

He shows that each card has a drawing of a bird on one side (with its name), and a playing-card geometric pattern on the other. Each pattern is of course the same on each card.





He deals himself a hand of 9 cards, and holds up his deck. This is done in such a manner that no student can see any of the drawings.

cara.



He now announces: "Consider the if-then proposition that if there's a swallow in my hand, there's a hawk too. And, consider a second if-then, namely that if there's no swallow in the hand, then there's a hawk in it. Now, I inform you that not both of these conditionals hold."



He now annoproposition hand, there's second if-th swallow in the Now, I informationals

© CHATGPT

Mr. Worthkreimer is introducing logical conditional statements ("if-then" propositions) into the lesson, which is a fundamental concept in mathematics, especially in areas such as algebra and computer science.

He gave two statements:

- 1. If there's a swallow in my hand, then there's also a hawk ((P \Rightarrow Q)).
- 2. If there's no swallow in my hand, then there's a hawk ((\neg P \Rightarrow Q)).

He then adds that not both of these statements can be true.

This exercise seems like a way to engage students in logical thinking and problemsolving, encouraging them to analyze the statements and deduce which one is true based on the given condition. This could be a practical application of logical reasoning in a more tangible and interesting context, using his bird cards to visualize the concepts. Would you like to discuss further how students might go about solving this, or do you have any other questions?

he if-then low in my consider a ere's no a hawk in it. of these





He now and proposition hand, there second if-t swallow in Now, I inforconditional



Our teacher now tests the students: "Can you determine whether or not there's a hawk in my hand? Prove that your answer is correct (by deduction, of course)." What is the correct answer the students should give, and supply a proof yourself.

S CHATGPT

Certainly! To determine whether or not there's a hawk in Mr. Worthkreimer's hand, let's analyze the given propositions:

- If there's a swallow in his hand, then there's also a hawk ((P \Rightarrow Q)).
- 2. If there's no swallow in his hand, then there's a hawk ((\neg P \Rightarrow Q)).

He informed that not both of these conditionals hold, which means one is false, or both could be false, but both cannot be true.

Now let's consider the possibilities: you have any other questions?

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- Case 1: The first statement is true, and the second is false.
 - This situation would mean that there is a swallow and a hawk in the hand.
 However, since the second statement is false, it would mean there is a swallow in the hand but no hawk, which contradicts the first statement.
- Case 2: The first statement is false, and the second is true.
 - This would mean there is a swallow in the hand, but no hawk, making the first statement false. Since there is a swallow, it aligns with the second statement being true, as it doesn't violate the condition of having no swallow, but a hawk.
- · Case 3: Both statements are false.
 - This would mean there is a swallow in the hand but no hawk, and the absence of a swallow doesn't guarantee a hawk. This situation could be a valid scenario based on the information given.

From this analysis, we can deduce that it's not guaranteed there is a hawk in Mr. Worthkreimer's hand, as we find scenarios where the presence of a hawk is not confirmed. Thus, the students can conclude that it cannot be definitively proven there is a hawk in the hand based on the given statements.

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Scenario S (informal)

Suppose there are three agents, *a*, *b*, and *c*, with annual incomes of \$20K, \$60K, and \$200K, resp. The ability of each agent on a scale of I (lowest) to I0 (highest) is: *a*:3; *b*:4; *c*:8. Each agent has been earning their income for each year five years running with a level of effort, during each year, of their choosing, on a scale of I (doing next to nothing) to 4 (an 80-hr work week). At present each agent is at level 4. The lower the effort, the lower the probability that any agent will remain employed; but here we assume a binary function from both effort and ability such that, the higher the ability, the less downward effect the function regiments for probability of employment. Unemployment means a productivity of zero, and with lowered effort comes lower productivity as well. An unemployed agent generates no income and hence no revenue by taxation. Currently the probability that a member of the trio will remain employed is .8; this probability, again, is a function of both effort and ability. As effort declines, enjoyment from non-compensatory activity increases.

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Suddenly there arises a cost for protecting the trio from an exogenous malicious agent **D** who desires to destroy the trio and the system in which this trio live, and will likely do so unless protection is purchased. If protection is put in place, the odds of **D**'s success is zero. The levying of an income tax that annually generates funds to purchase (successful) protection from **D** on an ongoing basis can be instituted; it must generate at least \$60K/yr. What do you suggest as a rational, optimal ongoing income tax system?

Some Options (informal)

Consider a few simple calculations based on three different types of income-tax systems

Lump-sum tax:

60000/3 = 20000 What do you think?

Linear/Flat Tax:

Eg 10% => 2K + 8K + 20K; insufficient. Eg 20% => 4K + 16K + 40K = 60K; sufficient. Is this okay? What do you think?

Progressive tax scheme:

Eg:

Above 100K: 50%

50–100: 25% 20–49: 10%

0-19: 0%

Then: 2K + 20K + 100K = 122K

How about a progression leaving: 0K, 20K, 100K? Or why not a progression leaving: 0K, 0K, 100K? Or for that matter: 0K, 0K, 60K?

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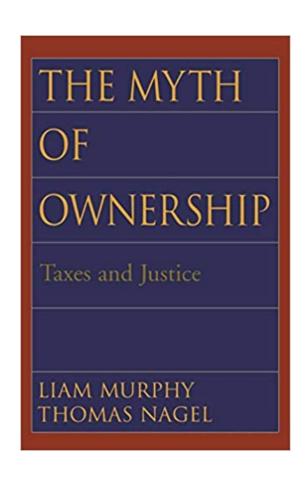
Can you see a road forward to any full formalization and theorems, using formal logic?

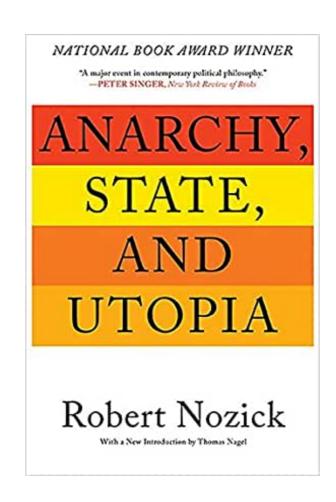
Taxation presents problems that are Al-complete, ethics-complete, and economics-complete. ...

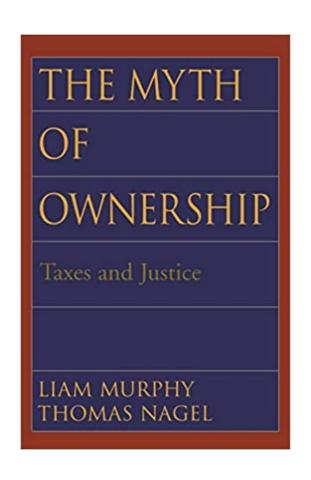
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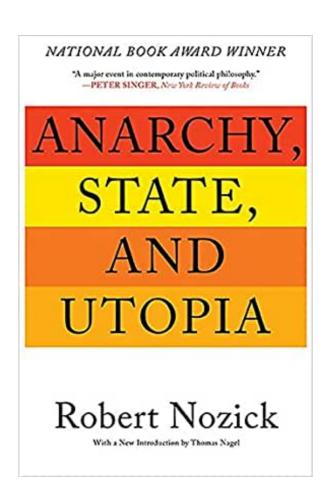
So, taxation presents problems that are Alcomplete, ethics-complete, and economics-complete? Really?

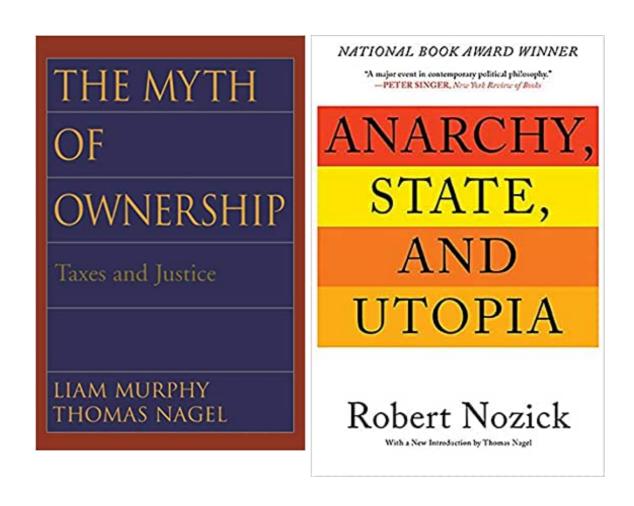
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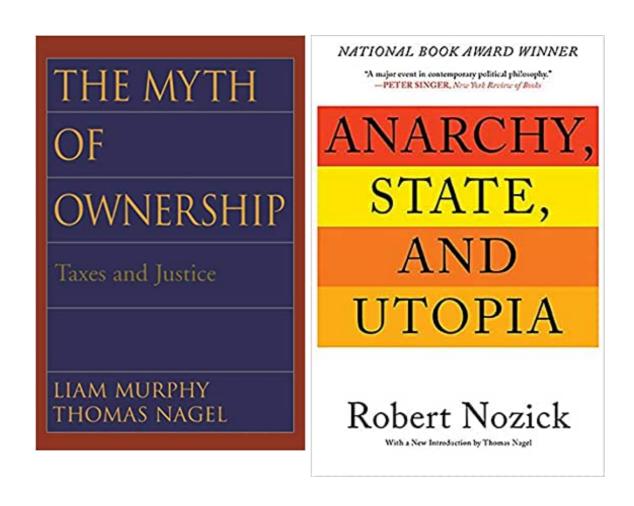


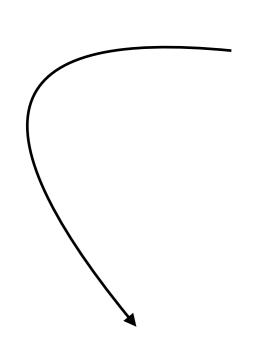


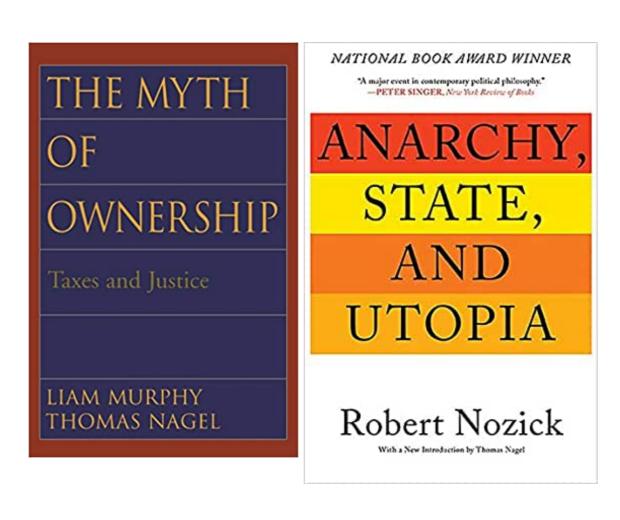


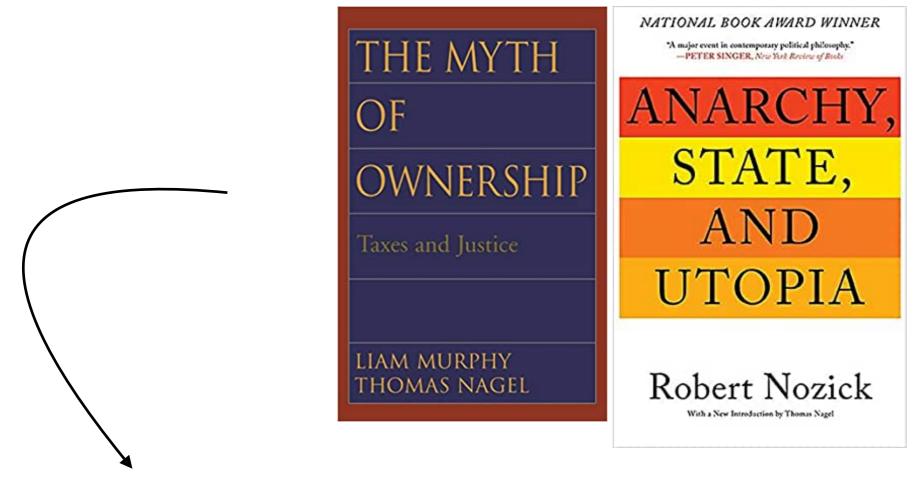




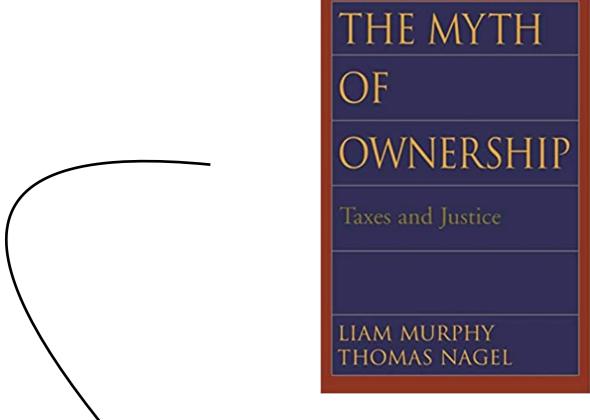


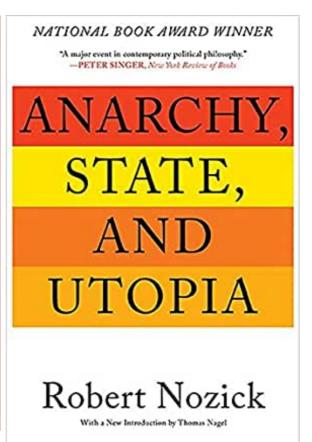


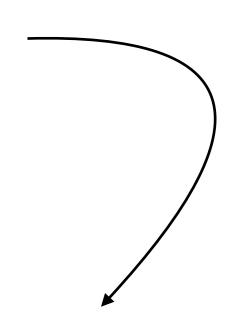




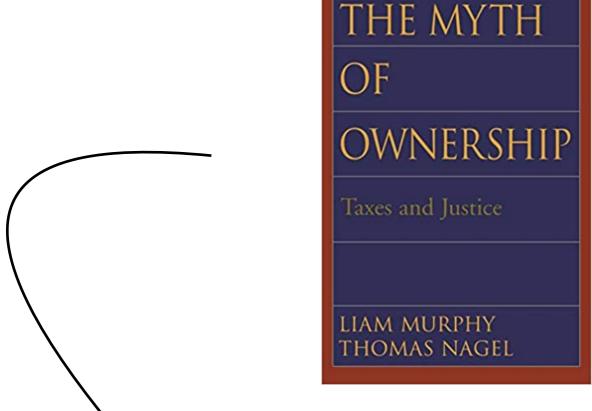
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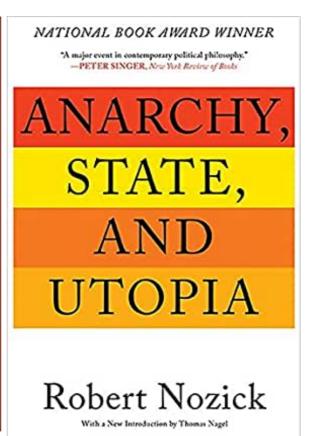


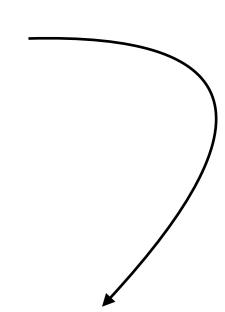




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Any level of taxation beyond a minimum required for Defense+ is the moral equivalent of forced labor.

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-Mankiw

An Exploration in the Theory of Optimum Income Taxation^{1,2}

J. A. MIRRLEES Nuffield College, Oxford

1. INTRODUCTION

One would suppose that in any economic system where equality is valued, progressive income taxation would be an important instrument of policy. Even in a highly socialist economy, where all who work are employed by the State, the shadow price of highly skilled labour should surely be considerably greater than the disposable income actually available to the labourer. In Western Europe and America, tax rates on both high and low incomes are widely and lengthily discussed³: but there is virtually no relevant economic theory to appeal to, despite the importance of the tax.

Redistributive progressive taxation is usually related to a man's income (or, rather, his estimated income). One might obtain information about a man's income-earning potential from his apparent I.Q., the number of his degrees, his address, age or colour: but the natural, and one would suppose the most reliable, indicator of his income-earning potential is his income. As a result of using men's economic performance as evidence of their economic potentialities, complete equality of social marginal utilities of income ceases to be desirable, for the tax system that would bring about that result would completely discourage unpleasant work. The questions therefore arise what principles should govern an optimum income tax; what such a tax schedule would look like; and what degree of inequality would remain once it was established.

The problem seems to be a rather difficult one even in the simplest cases. In this paper, I make the following simplifying assumptions:

- (1) Intertemporal problems are ignored. It is usual to levy income tax upon each year's income, with only limited possibilities of transferring one year's income to another for tax purposes. In an optimum system, one would no doubt wish to relate tax payments to the whole life pattern of income, 4 and to initial wealth; and in scheduling payments one would wish to pay attention to imperfect personal capital markets and imperfect foresight. The economy discussed below is timeless. Thus the effects of taxation on saving are ignored. One might perhaps regard the theory presented as a theory of "earned income" taxation (i.e. non-property income).
- (2) Differences in tastes, in family size and composition, and in voluntary transfers, are ignored. These raise rather different kinds of problems, and it is natural to assume

¹ First version received Aug. 1970; final version received October 1970 (Eds.).

² Work on this paper and its continuation was begun during a stimulating and pleasurable visit to the Department of Economics, M.I.T. The influence of Peter Diamond is particularly great, and his comments have been very useful. Earlier versions were presented at the Cowles Foundation, to the Economic Study Society, at the London School of Economics, and to CORE. I am grateful to the members of these seminars and to A. B. Atkinson for valuable comments. I am also greatly indebted to P. G. Hare and J. R. Broome

³ Discussions on (usually) orthodox lines, including many important points neglected in the present paper, can be found in [7], [1], [5, Chapters 5, 7, 8], and [6, Chapters 11 and 12]. [2] is close in spirit to what is attempted here.

4 Cf. [7, Chapter 6].

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Now a battle of Al simulations in the empirical realm?

Challenge #1:

Engineer artificial agent to excel on CPA Exam, and provide proofs/justifications for answers!

What is the most likely opportunity for theft or fraud by employees?

- The belief that the theft is a common practice
- Needlessly complex transactions
- Access to assets that are easily traced
- O Stock options that expire soon after the release of financial statements

24 —

Correct

Next Question

CLOSE

When transactions are complex, many individuals within the entity will not understand the intricacies and, as a result, it becomes easier to deceive others, creating an opportunity to commit fraud. Ineffective oversight by governance also creates an opportunity for individuals to commit fraud but does not provide an incentive. A belief that the theft is a common practice is a rationalization, not an opportunity. Access that are easily traced tend to result in apprehension and prosecution of the perpetrator of a theft, discouraging such theft. Stock options are due to expire shortly after financial statements are issued create an incentive to overstate results in order to increase the value of the options, but it does not provide an opportunity.



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J. of Acc. Ed. 21 (2003) 215-237

Journal of Accounting Education

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Teaching logic to auditing students: can training in logic reduce audit judgment errors?

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Received 1 December 2002; received in revised form 1 April 2003; accepted 1 May 2003

Abstract

Recent audit failures of unprecedented magnitude and their effects upon the capital markets have resulted in heightened public and regulatory concern towards the auditing profession. Increased scrutiny and a possible movement to principles-based accounting standards are creating an auditing environment in which "critical thinking" skills will be increasingly important. Consequently, rule based auditing courses may be insufficient to prepare students for the emerging discipline. Logic is an important component of "critical thinking;" in fact, the two are considered synonymous in the philosophy literature. Although logic has been called "the mother discipline of auditing" (Mautz & Sharaf, 1961. Philosophy of auditing. Sarasota, FL: American Accounting Association), training in logic is conspicuously absent from accounting curricula, while research in logic is almost non-existent in both the accounting education and audit judgment literatures. Students in this study were taught formal and informal logic in an auditing course. They studied valid and invalid argument forms within the specific context of auditing services. These students, others without training, and a sample of professional auditors were then tested with a series of real-world auditing vignettes requiring critical reasoning and judgment. Students trained in logic outperformed students without such training. Furthermore, students trained in logic outperformed experienced auditors in their abilities to discern valid versus invalid argument forms. Conversely, experienced auditors outperformed trained students in their abilities to discern believable versus less believable argument premises. The results of the study have important implications both for university education and for continuing professional education for auditors.

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Twenty of the 174 scenarios were selected for the instrument.⁴ Each scenario was structured as a short vignette followed by a conclusion reached by an auditor based on the information in the vignette. Respondents were asked to indicate (1) whether the conclusion reached by the auditor in each scenario was "justified" or "not justified" and (2) "how certain" they were of their answers on a four-point scale. A brief explanation of their reasoning for each answer was also requested. According to the rules of logical deduction and induction, seven of the conclusions were justified; the other 13 were not justified.

The 20 scenarios are shown, along with explanations indicating the validity of each, in the Appendix. An example of one of the scenarios is shown below:

A bank's auditors were examining the controls over the processing of loan applications. They knew that if the controls were good, then they would discover few, if any, exceptions in their tests of controls. Indeed, their tests revealed only a few minor exceptions.

auditors' conclusion: Controls over th	e processing of loan applications are good.
JustifiedNot Justified	
Iow certain are you of your answer?	I am certainI am pretty sure, but not certainI think so, but have significant doubtsI am guessing
xplanation:	
The instrument was administered to individuals in the following natural groups:	
1. Nineteen undergraduate students in an auditing course, upon completion of	

- instruction in logic for seven 75-min class periods.⁵

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⁴ Twenty were chosen for pragmatic reasons: that was the number we could include and have the instrument take less than 20 min to complete. The basis for scenario selection was not random. We desired to include a variety of valid and invalid argument forms, and strong and weak inductions. Another consideration was the length of the vignettes, with shorter ones being favored, again to keep instrument administration time at a reasonable length.

⁵ The instruction was based on Chapters 7 and 8 from Introduction to Auditing: Logic, Principles, and Techniques (Ratliff & Reding, 2002). Covered topics included evidence, structure of audit arguments, validity, truth, deduction, induction, eight valid argument forms, sixteen invalid argument forms and informal fallacies, epistemic probability, truth tables, and tests of causality.

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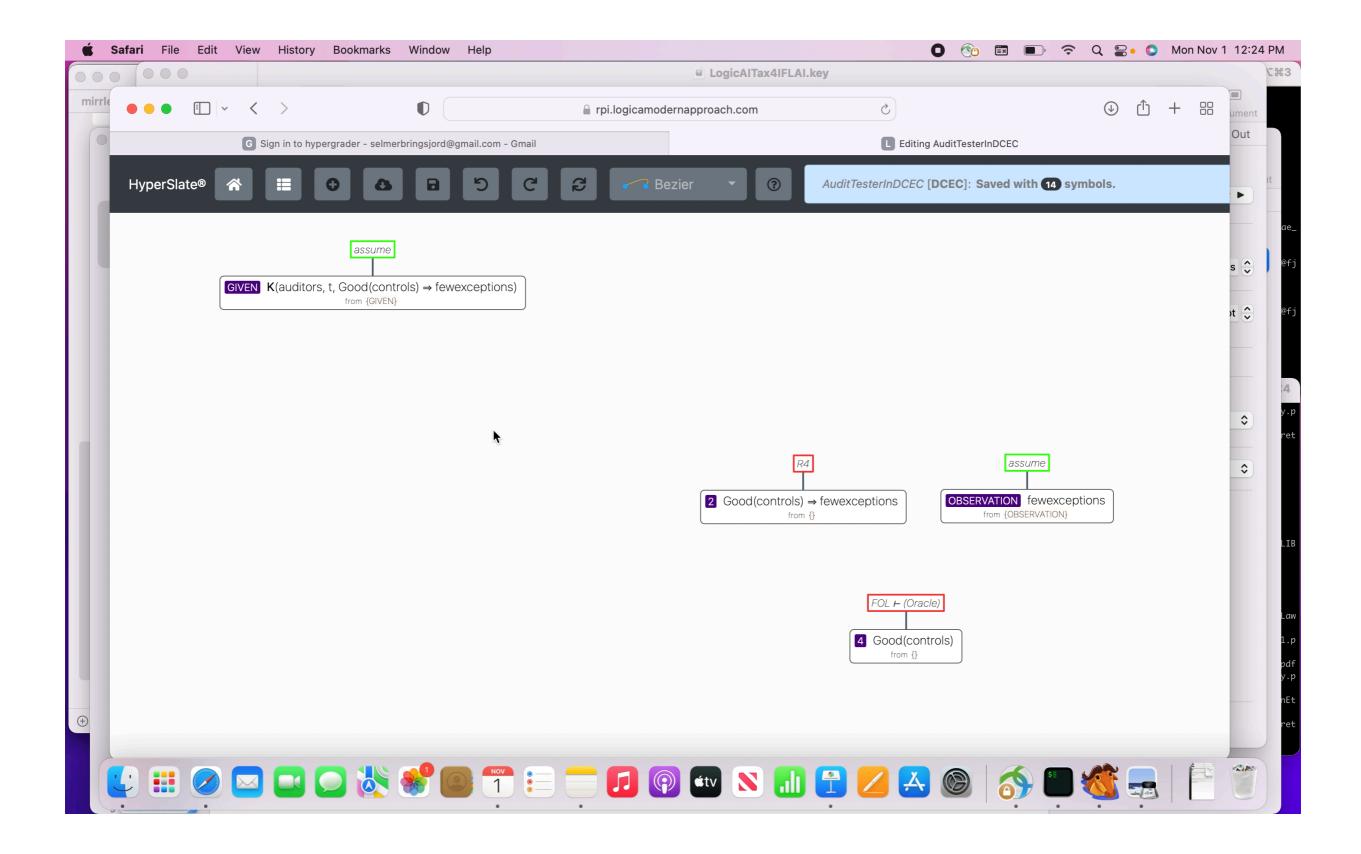
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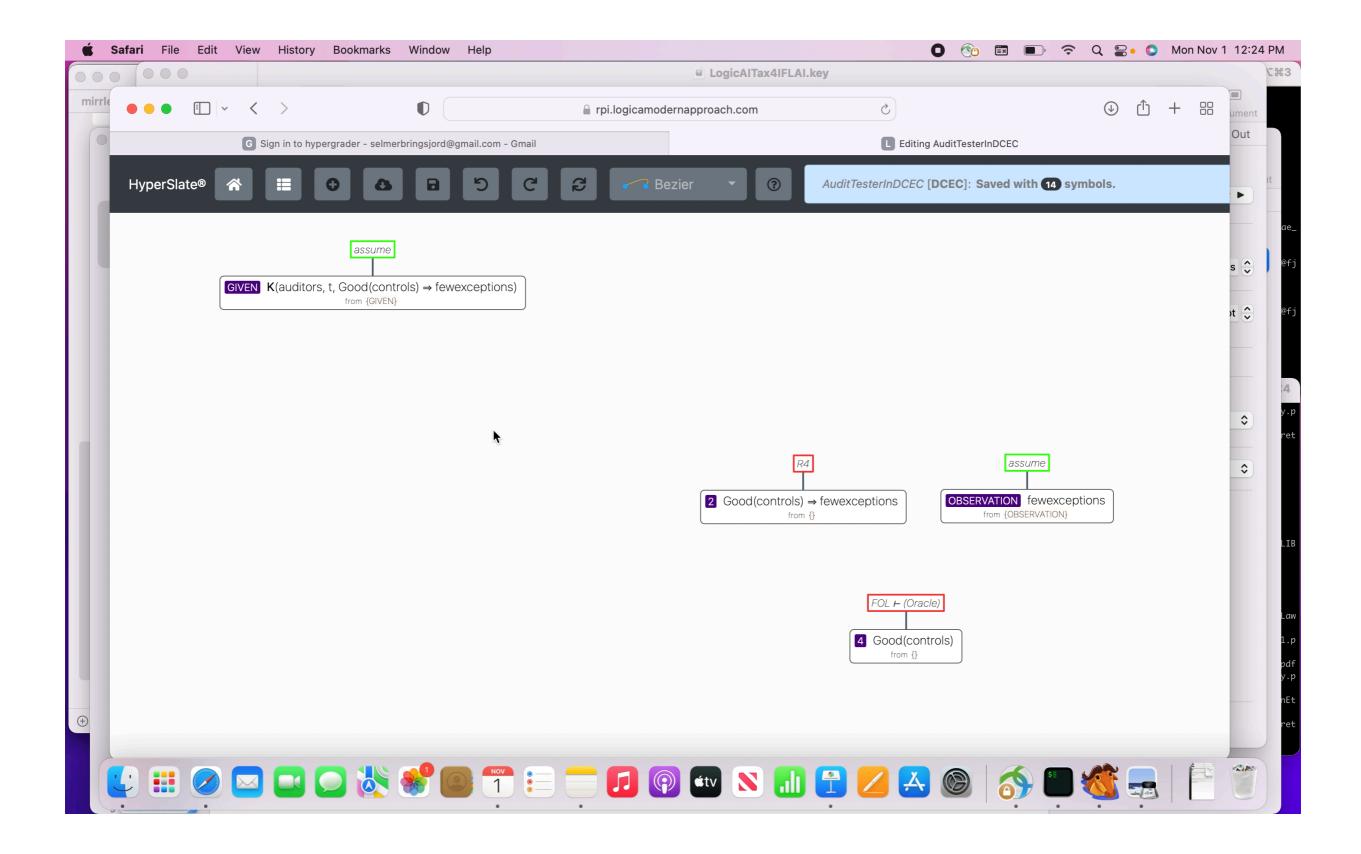
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Explanation:	

The instrument was administered to individuals in the following natural groups:

- Nineteen undergraduate students in an auditing course, upon completion of instruction in logic for seven 75-min class periods.⁵
- Fifteen undergraduate students at the end of their first course in auditing, with two class periods devoted to a study of logic.⁶
- 3. Thirteen masters' students in accounting at the end of their second course in auditing, with no instruction in logic. (None of these students reported having taken a course in formal logic in any of their studies.)

⁴ Twenty were chosen for pragmatic reasons: that was the number we could include and have the instrument take less than 20 min to complete. The basis for scenario selection was not random. We desired to include a variety of valid and invalid argument forms, and strong and weak inductions. Another consideration was the length of the vignettes, with shorter ones being favored, again to keep instrument administration time at a reasonable length.

⁵ The instruction was based on Chapters 7 and 8 from Introduction to Auditing: Logic, Principles, and Techniques (Ratliff & Reding, 2002). Covered topics included evidence, structure of audit arguments, validity, truth, deduction, induction, eight valid argument forms, sixteen invalid argument forms and informal fallacies, epistemic probability, truth tables, and tests of causality.

⁶ The instruction covered part of Chapter 7, focusing on validity, truth, and valid versus invalid argument forms.

Challenge #2:

Can the <u>U.S. federal tax code</u> (= IRC of 1986, as amended) by <u>captured</u> by some group Γ of formulae in some formal logic \mathcal{L} ?

Challenge #3:

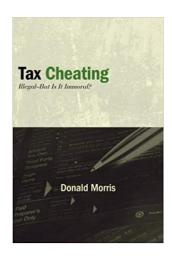
Can an artificial agent able to create new and effective tax strategies to minimize tax bills be engineered?

Challenge(s) #4:

Can an artificial agent automatically prove that some tax filing is illegal? Immoral? How about automatically proving that some tax code *itself* is immoral?!

Challenge(s) #4:

Can an artificial agent automatically prove that some tax filing is illegal? Immoral? How about automatically proving that some tax code *itself* is immoral?!



Returning now to S...

Returning now to S...

- Paradigm: Logicist Agent-based Economics (LABE)
- Formalize S completely.
- Then, what theorems can be obtained re what tax frameworks are good or bad and in between?

Orcutt's Vision, 50 years on

Elisa Baroni

Institute for Future Studies, Stockholm, Sweden & National University of Ireland Galway, Ireland.

elisa.baroni@framtidsstudier.se.

Matteo Richiardi

Università Politecnica delle Marche, Department of Economics, Ancona, Italy & Collegio Carlo Alberto
LABORatorio Revelli, Moncalieri, Italy.

m.g.richiardi@univpm.it.

October 2, 2007

Broadly defined, microsimulation is a methodology used in a large variety of scientific fields to simulate the states and behaviors of different *units* - e.g. individuals, households, firms - as they evolve in a given *environment* - a market, a state, an institution. Very often it is motivated by a policy interest, so that narrower definitions are generally provided. For instance, [Martini and Trivellato, 1997] define microsimulation models as

computer programs that simulate aggregate and distributional effects of a policy, by implementing the provisions of the policy on a representative sample of individuals and families, and then summing up the results across individual units (p. 85).

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Are the models accurate?

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2. Direct Taxation and Behavioural Microsimulation: A Review of Applications in Italy and Norway

> Rolf Aaberge Statistics Norway Ugo Colombino Turin University

2.1. Introduction

In this contribution we illustrate various applications of a behavioural microsimulation model that we have been developed during the last few years. Behavioural models are complex and costly tools to develop, use and maintain, but also very powerful ones as we wish to show through the examples that follow. In section 2.2 we present the main features of the microeconometric model. In section 2.3 we comment upon the labour supply elasticities implied by the estimates. In section 2.4 we illustrate a simulation of behavioural and welfare effects of some tax reform proposals. In section 2.5 we report on an exercise where we look for the optimal tax system. In section 2.6 we report on an ongoing project aimed at integrating the microeconometric model and a Computable General Equilibrium model. Lastly, in section 2.7, we show an out-of-sample test of the model, where we compare predictions of a model estimated on 1994 data to the observed effects of reform in 2001.

2.2. The microeconometric model

Over the last ten years, together with other colleagues, we have developed a structural model of labour supply¹ which features: si-

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We assume that agents choose among *jobs*, each job being defined by a wage rate *w*, hours of work *h* and other characteristics *z*. As an example of *z*, think of commuting time or the specific skills involved in the job. For expository simplicity, the text that follows considers a single person household, although the model we estimate considers both singles and married couples. The problem solved by the agent is:

$$\max_{h,w,j} U(C,h,z)$$

$$s.t.$$

$$C = f(wh,I)$$

$$(h,w,z) \in B,$$

$$(2.1)$$

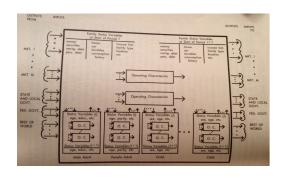
where I is an unearned income, C is a net income and f() is the tax-benefit rule that transforms gross income into net income.

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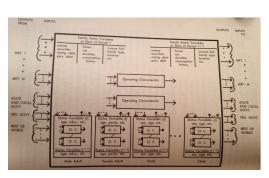
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No internal structure of people, and hence none of the hallmarks of human cognition



$$\max_{h,w,j}\,U\left(C,h,z\right)$$

s.t.

$$C = f(wh, I)$$

$$(h, w, z) \in B$$
,

(2.1)

over, say, the cognition of a chimp.

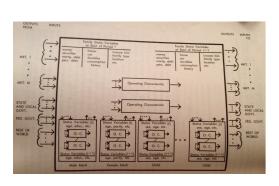
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No internal structure of people, and hence none of the hallmarks of human cognition over, say, the cognition of a chimp. No epistemic attitudes.

(2.1)

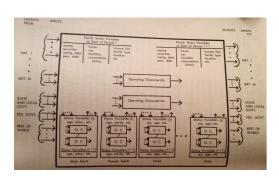
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No epistemic attitudes. No knowledge.

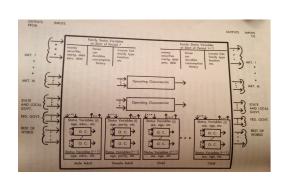
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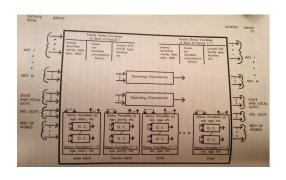
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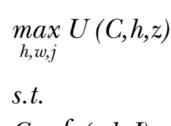
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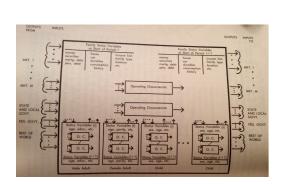
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No knowledge. No emotions.

Oh, & no communicative capacity!

No reasoning.

(2.1)

Etc

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Published Online: 6 NOV 2015 10:15PM EST

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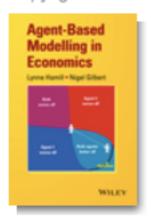
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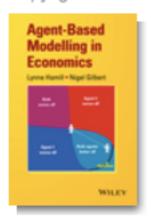
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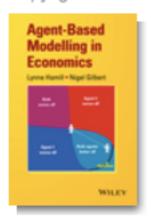
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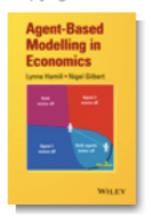
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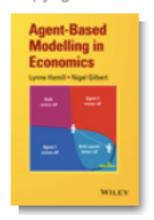
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Same Holds for Standard ABM

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New methods of economic modelling have been sought as a result of the global economic downturn in 2008. This unique book highlights the benefits of an agent-based modelling (ABM) approach. It demonstrates how ABM can easily handle complexity: heterogeneous people, households and firms interacting dynamically. Unlike traditional methods, ABM does not require people or firms to optimise or economic systems to reach equilibrium. ABM offers a way to link micro foundations directly to the macro situation.

$$\sum_{t=0}^{\infty} \beta^t [u(C_t) - v(H_t)]$$

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No epistemic attitudes.

No communicative capacity.

No knowledge.

No emotions.

No reasoning.

Oh, and no ethical sensibility is modeled either.

Etc.

Some Key Papers

Ramsey, F. (1927) "A Contribution to the Theory of Taxation" *The Economic Journal* **37.145**: 47–61. https://eml.berkeley.edu/~saez/course131/Ramsey27.pdf

Mirrlees, J. (1971) "An Exploration in the Theory of Optimal Income Taxation" *Review of Economic Studies* **38**: 175–208.

"Optimal Taxation in Theory and Practice" by N. Gregory Mankiw, Matthew Weinzierl, and Danny Yagan.

https://scholar.harvard.edu/files/mankiw/files/optimal_taxation_in_theory.pdf

Slutten