

Review of Extensional Logics (contrasted with intensional ones)

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Troy, New York 12180 USA

Intermediate Formal Logic & AI (IFLAI2)
9/7/2021



Mechanics ...

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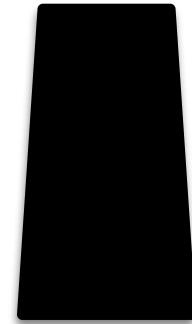
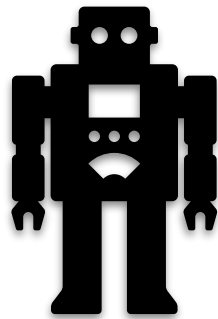
Mechanics ...

Any questions? ...

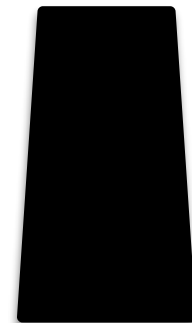
Extensional vs Intensional Logics in a Nutshell Example

...

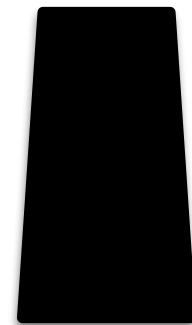
Blinky



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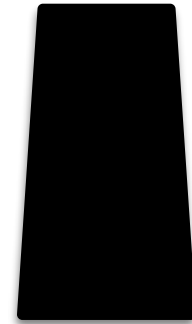
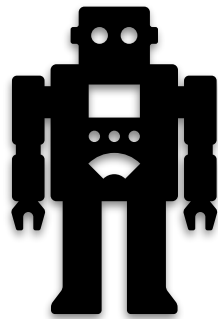


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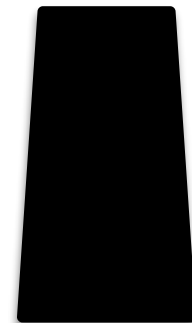


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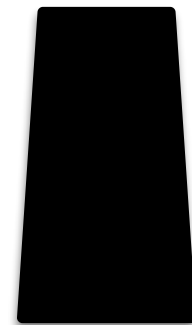
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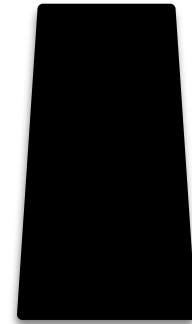
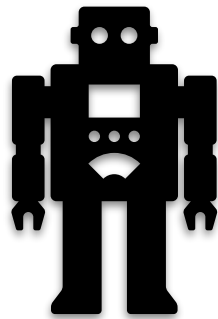
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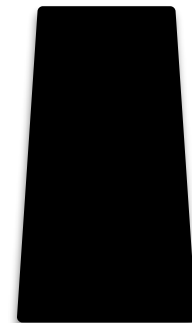
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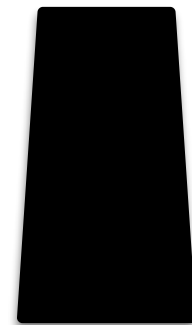
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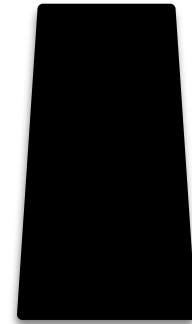
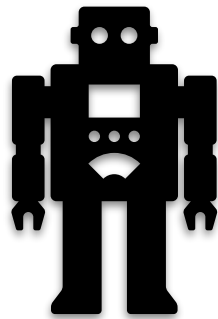


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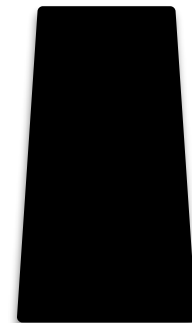


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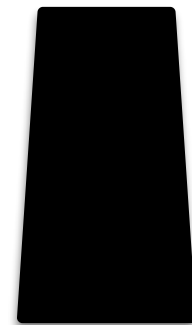
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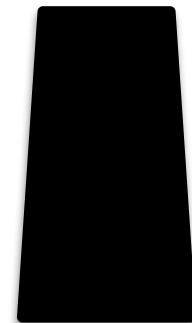
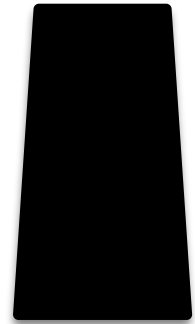
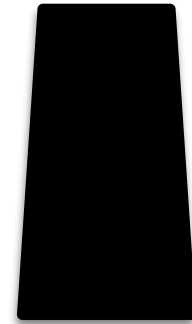
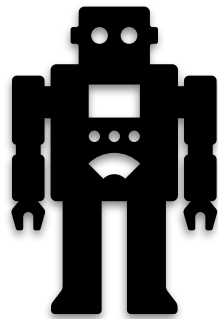


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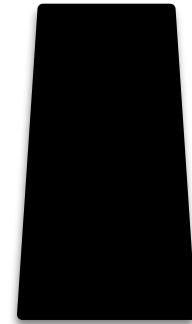
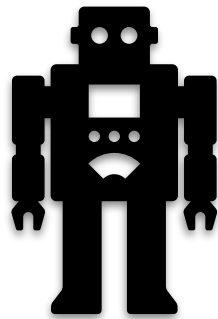
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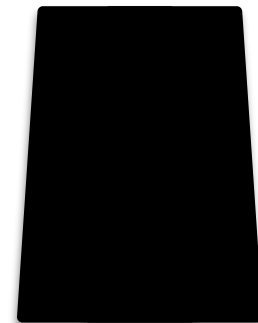
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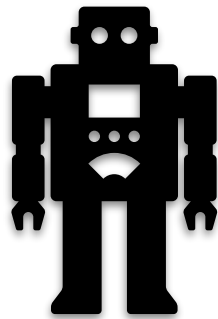
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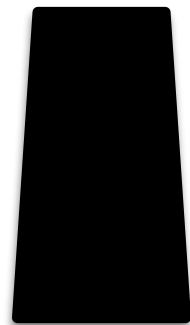
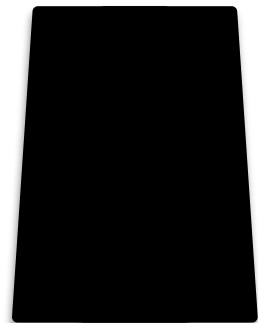
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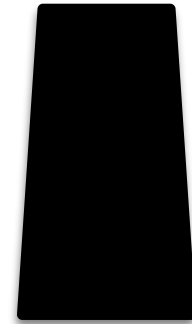
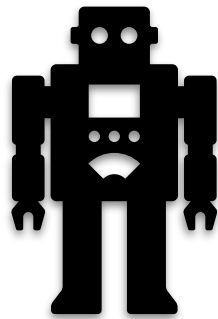
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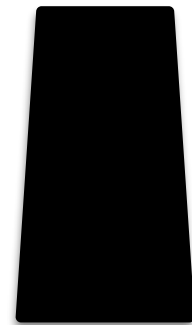
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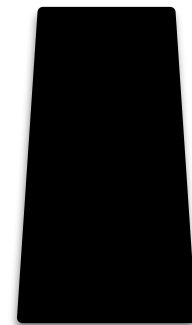
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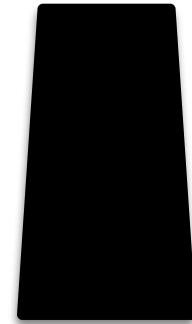
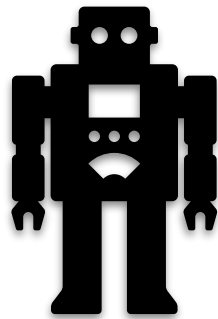


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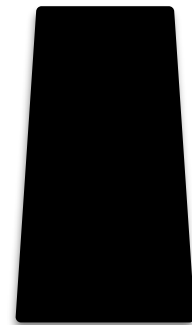


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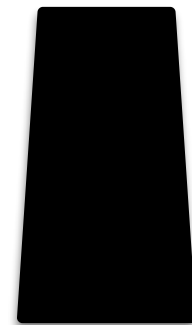
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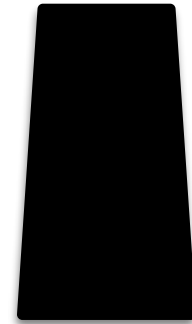
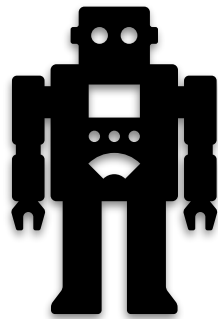


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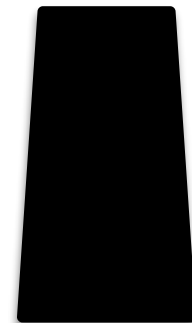


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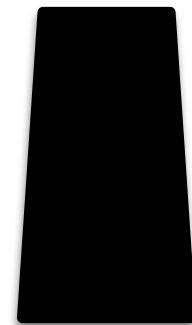
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1



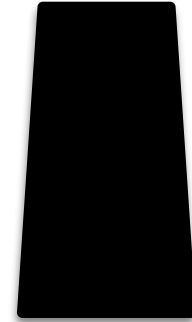
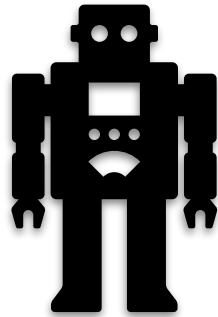
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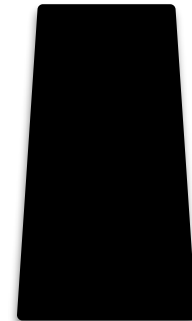
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The ball is in the cup at location #1.

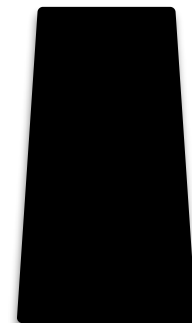
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1



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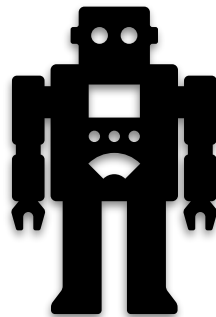


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The ball is in the cup at location #1.

Loc(ball,1)

Blinky



1



2



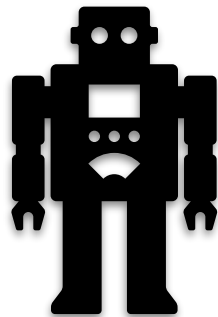
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The ball is in the cup at location #1.

Loc(ball,1)

(Loc ball 1)

Blinky



1



2



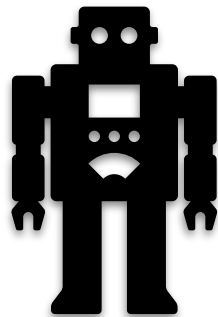
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The ball is in the cup at location #1.

FALSE Loc(ball,1)

(Loc ball 1)

Blinky



1



2

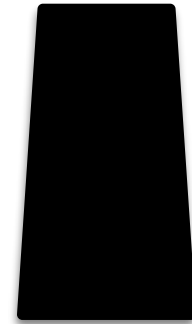
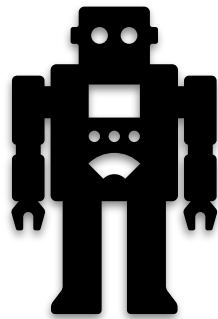


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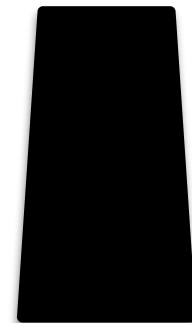
FALSE Loc(ball,1)

(Loc ball 1)

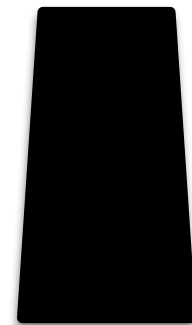
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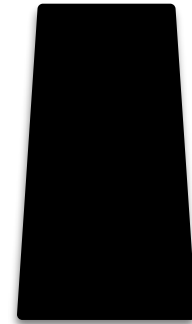
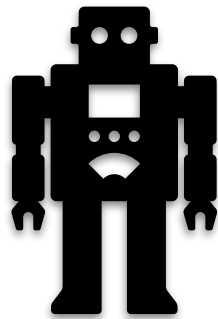


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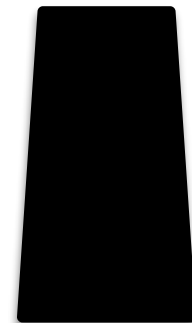
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(Loc ball 1)

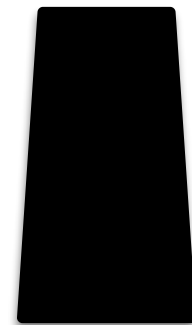
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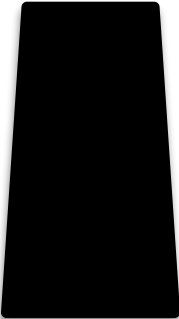


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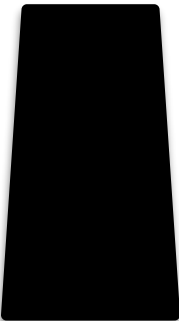


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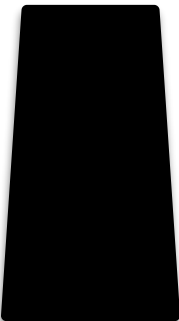
(Loc ball 1)



1

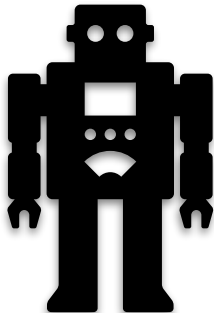


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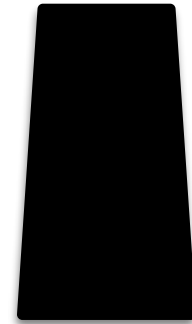
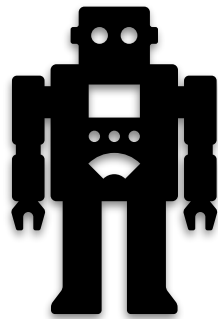


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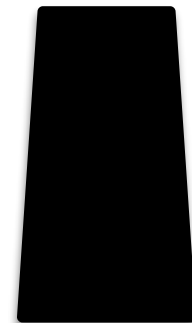
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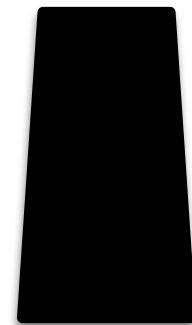
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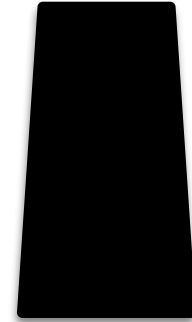
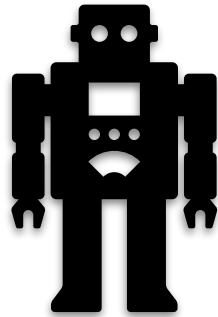
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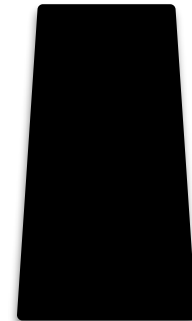
3

The ball is in the cup at location #1 or the ball is at location #3.

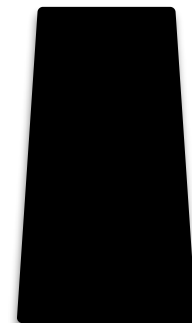
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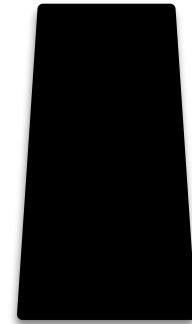
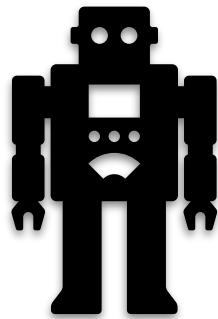


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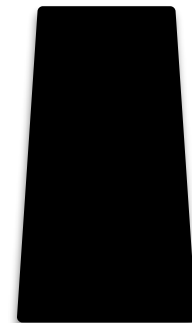
The ball is in the cup at location #1 or the ball is at location #3.

$\text{Loc}(\text{ball}, 1) \vee \text{Loc}(\text{ball}, 3)$

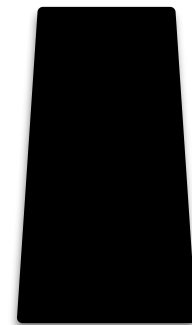
Blinky



1



2



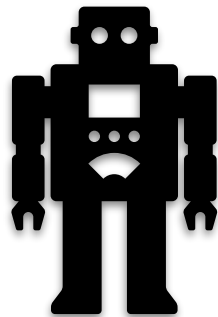
3

The ball is in the cup at location #1 or the ball is at location #3.

$\text{Loc}(\text{ball}, 1) \vee \text{Loc}(\text{ball}, 3)$

(or (Loc ball 1) (Loc ball 3))

Blinky



1



2



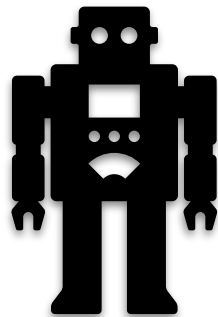
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(or (Loc ball 1) (Loc ball 3))

Blinky



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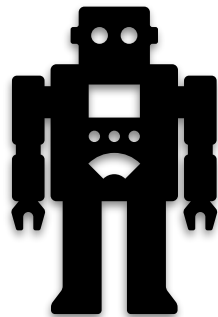


3

FALSE $\text{Loc}(\text{ball}, 1) \vee \text{Loc}(\text{ball}, 3)$

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Blinky



1



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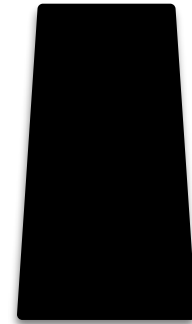
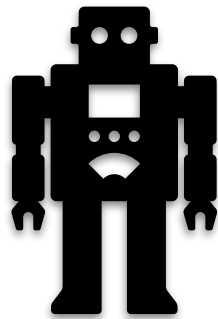


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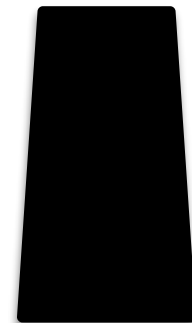
FALSE

(or (Loc ball 1) (Loc ball 3))

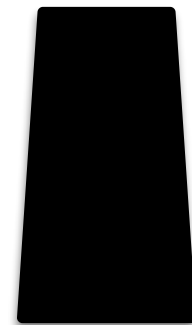
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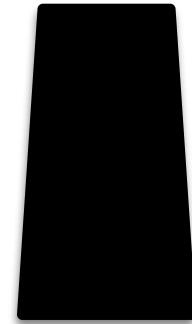
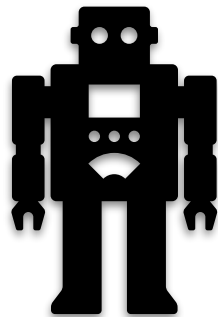
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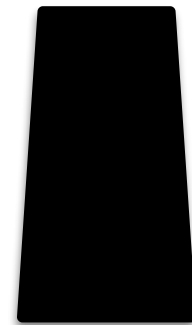
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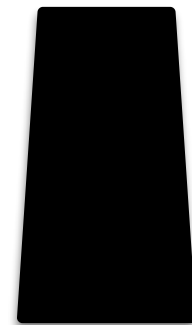
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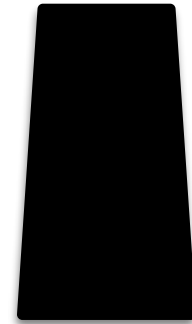
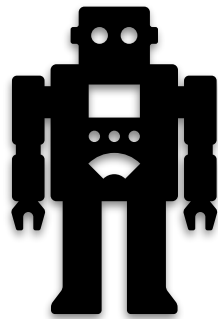


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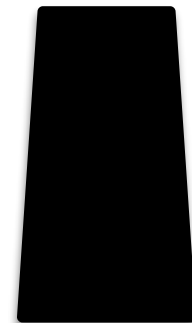


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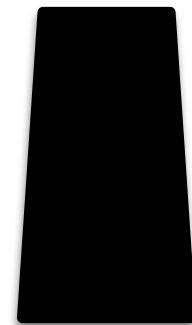
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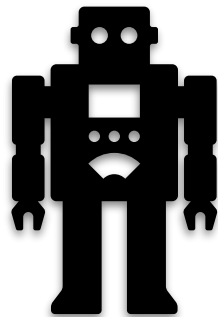
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3

Blinky believes that the ball is in the cup at location #1.

Blinky



1



2

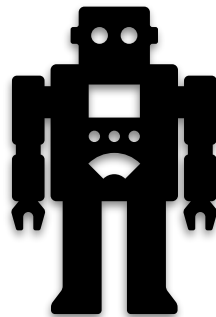


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Blinky believes that the ball is in the cup at location #1.

$B(\text{blinky}, \text{Loc}(\text{ball}, 1))$

Blinky



1



2



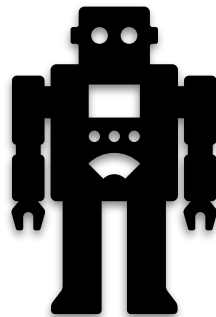
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Blinky believes that the ball is in the cup at location #1.

$B(\text{blinky}, \text{Loc}(\text{ball}, 1))$

`(bel Blinky (Loc ball 1))`

Blinky



1



2



3

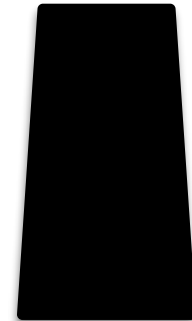
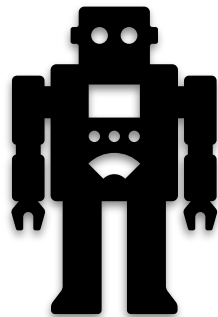
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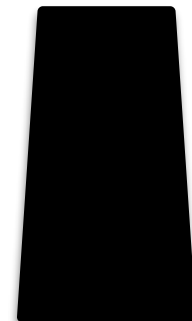
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(bel Blinky (Loc ball 1))

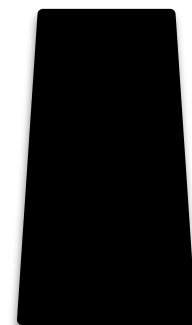
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1



2



3

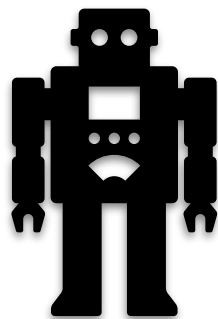
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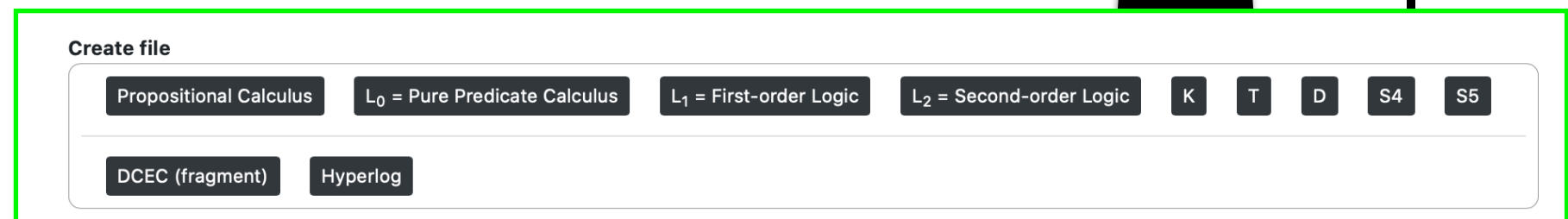
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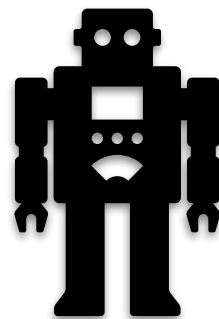
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$B(\text{blinky}, \text{Loc}(\text{ball}, 1))$

$(\text{bel Blinky } (\text{Loc ball } 1))$



Blinky



2

3

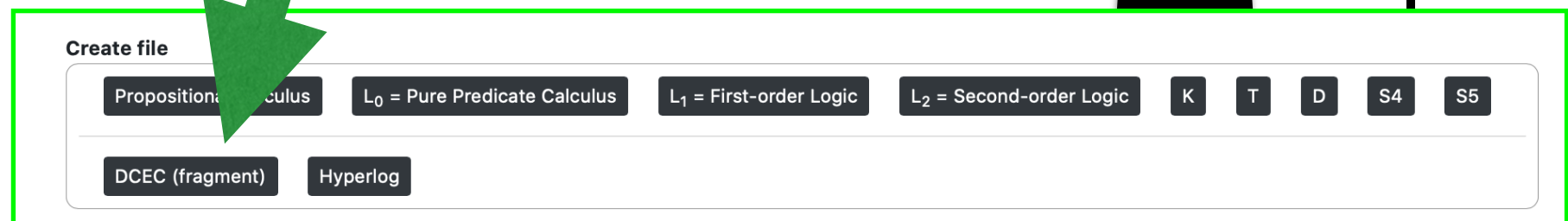
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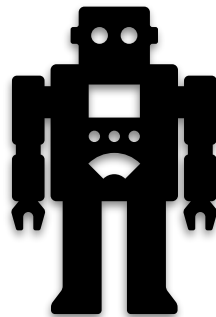
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2

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Layman Allen Committee Problem ...

“Well, if your AI is so smart, let me see it do my taxes for me, and for a company too.”

THE UNIVERSITY OF CHICAGO LAW REVIEW

VOLUME 25

AUTUMN 1957

NUMBER 1

TOWARD A MORE SYSTEMATIC DRAFTING AND INTERPRETING OF THE INTERNAL REVENUE CODE: EXPENSES, LOSSES AND BAD DEBTS

LAYMAN E. ALLEN* AND GABRIEL ORECHKOFF†

SUPPOSE that you, as a reasonable man, are asked whether the following two sets of rules mean exactly the same thing. If they do and if you intend to communicate your message as effectively as possible, which of the two sets would you choose to state the organizational rules of your law school?

Set 1

- A. The financial committee shall be chosen from among the general committee.
- B. No one shall be a member of both the general and library committees unless he is also on the financial committee.
- C. No member of the library committee shall be on the financial committee.¹

Set 2

- A. The financial committee shall be chosen from among the general committee.
- B. No member of the general committee shall be on the library committee.

We suspect that most readers will have little difficulty in deciding the second question; but even after careful reading of the two sets of rules, they will remain a little puzzled as to whether both sets say the same thing. We further suspect that lawyers waste a great deal of their mental energy by using inadequate and inappropriate intellectual tools to figure out similar logical problems in their everyday work. A symbolic logician could quickly ascertain that the two sets of rules are equivalent and relieve his mind to focus on the more important problem of deciding which is the more appropriate choice. Since law

* Social Science Research Council Fellow, Yale Law School. Member Connecticut Bar.

† Member, New York Bar.

¹ This example is given in Berkeley, *The Algebra of States and Events*, 78 *Scientific Monthly* 232 (1954).

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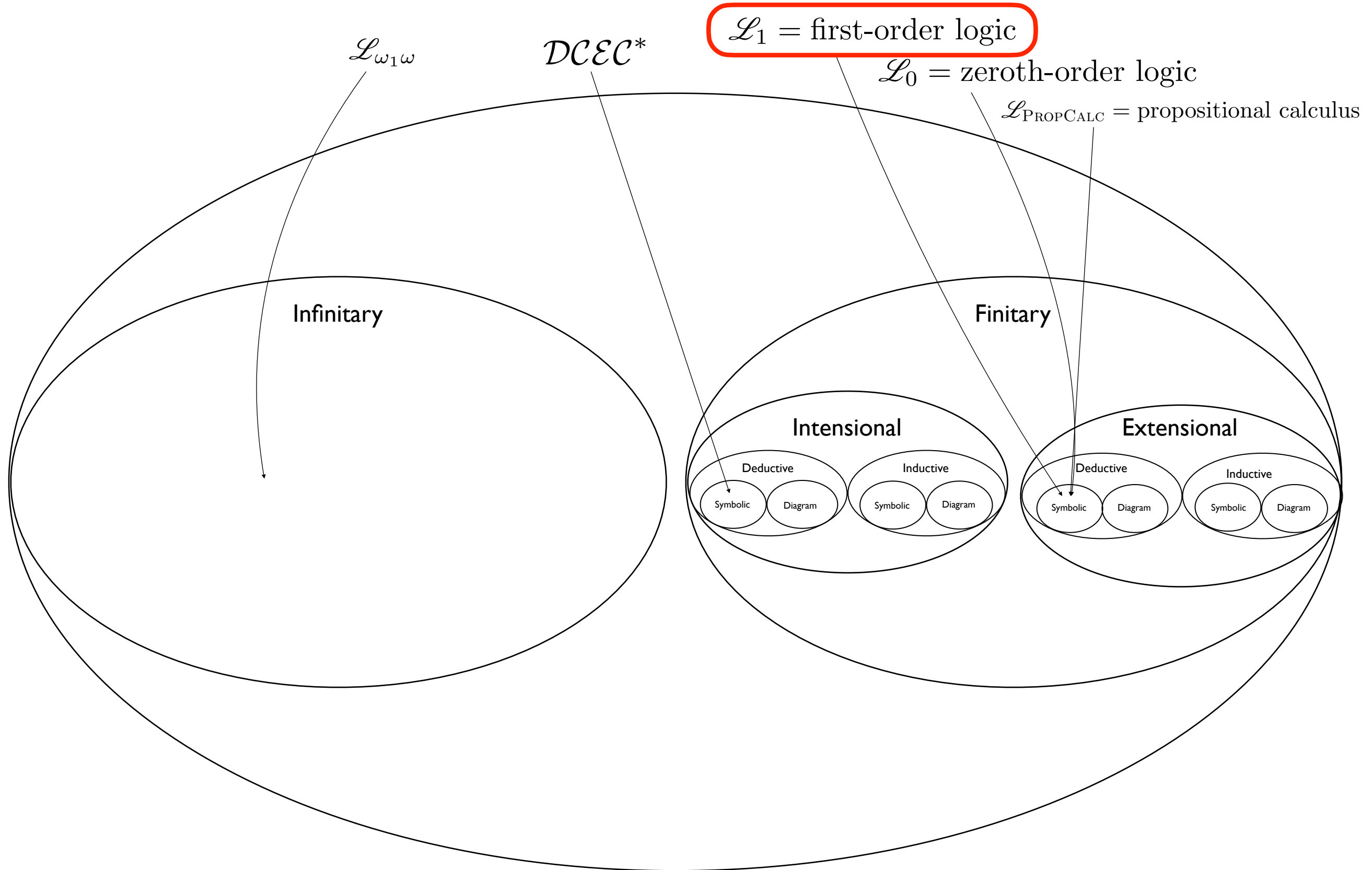
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SpecialLlamasDisjunction

...

The Universe of Logics



Special Llamas Disjunction

There's a thing such that it's both a llama and a non-llama;
or
there's a thing such that if it's a llama, everything is a llama;
or
there's a thing such that every llama is a non-llama.

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Is this disjunction TRUE, FALSE, or UNKNOWN?

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Second-Order Logic and the k -Order Ladder ...

FOL

✓ FOL

✓ FOL

Epistemic + FOL

$B_d B_v B_d V v$

✓ FOL

Epistemic + FOL (for coverage of “killer” robots, later)
 $B_d B_v B_d V v$

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$B_d B_v B_d V v$

TOL

$\exists X[X(j) \wedge \neg X(m) \wedge S(X)]$

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Double-Minded Man

The Contemporary Craft of Creating Characters Meets Today's Cognitive Architectures: A Case Study in Expressivity*

Selmer Bringsjord • John Licato • Alexander Bringsjord

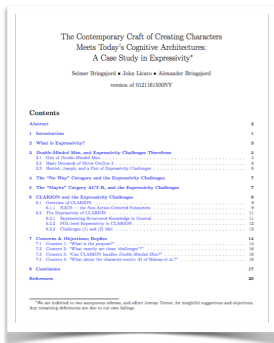
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*We are indebted to two anonymous referees, and editor Jeremy Turner, for insightful suggestions and objections. Any remaining deficiencies are due to our own failings.

Double-Minded Man



Movie Outline - Double-Minded_Man_010316.mvo

Outline Script Notes Characters FeelFactor Reference Library PowerView Step Cards Story Tasks

1. TWIRL - DAY

68-year-old Harriet Smith sits with two wrinkled hands firmly on the wheel of her rust-eaten Subaru wagon, staring straight ahead through the top level of bifocals as she waits serenely at a red light.

Harriet is alone in the car. To her right is another vehicle, also waiting, in this case to make a right turn; it's a sleek, low-slung, black Camaro.

We are inside the cabin with Harriet. The Subaru's sound system softly plays choral music. Harriet's lips move slightly as she internally sings along, mouthing a slow aria. Her head weaves slightly side to side, in the rhythm with the music.

Things are calm as can be here inside the car with Harriet. There are a pair of well-worn Bibles on the empty passenger seat beside her, one with a gold-lettered 'Harriet' on its leather front cover, the other with a matching 'Joseph' on its front cover.

Harriet's eyes swivel up to the light: still red. We wait with her.

Suddenly there is a piercing SCREECH outside. Harriet jerks her head to the right and we follow her line of sight.

A sleek motorcycle has swerved out of its lane and is now streaking straight for the right side of the Camaro beside Harriet's car.

The bike slams with CLANG into the side of the Camaro. Its rider is flung up and forward into the air, twirling passed Harriet's windshield.

We now watch from Harriet's POV, in slow motion. The black-leather-clad motorcyclist sails by Harriet's windshield, airborne. We see a man's face, clearly: His elephant-hide skin tells us that he is well beyond middle-age. Yet thick, black curls of youthful hair emerge from under his helmet. The rider has only one half of a black, bushy, swept-out, waxed mustache. His eyes are weary and grey, and appear to lock with Harriet's for an instant.

We return to normal speed. The body is now lying on the incoming lane to the left of Harriet's Subaru, perfectly still on the blacktop, the head twisted into an impossible angle. Blood seeps from a nostril. Beside the lifeless head, a BMW medallion lies on the pavement, glinting in the sunlight.

1. TWIRL - DAY

2. YES, THAT'S HIM - LATER

3. SECOND HOME - LATER

Step 1 of 3

The Contemporary Craft of Creating Characters
Meets Today's Cognitive Architecture:
A Case Study in Expressivity*

Selmer Bringsjord • John Lewis • Alexander Bringsjord
version of 022161000V

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Double-Minded Man

Double-Minded Man
by
S Bringsjord & A Bringsjord

DRAFT #5
© June 30 2016

Selmer.Bringsjord@gmail.com

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Double-Minded Man

1. TWIRL - DAY

68-year-old Harriet Smith sits with two wrinkled hands firmly on the wheel of her rust-eaten Subaru wagon, staring straight ahead through the top level of bifocals as she waits serenely at a red light.

Harriet is alone in the car. To her right is another vehicle, also waiting, in this case to make a right turn; it's a sleek, low-slung, black Camaro.

We are inside the cabin with Harriet. The Subaru's sound system softly plays choral music. Harriet's lips move slightly as she internally sings along, mouthing a slow aria. Her head weaves slightly side to side, in the rhythm with the music.

Things are calm as can be here inside the car with Harriet. There are a pair of well-worn Bibles on the empty passenger seat beside her, one with a gold-lettered 'Harriet' on its leather front cover, the other with a matching 'Joseph' on its front cover.

Harriet's eyes swivel up to the light: still red. We wait with her.

Suddenly there is a piercing SCREECH outside. Harriet jerks her head to the right and we follow her line of sight.

A sleek motorcycle has swerved out of its lane and is now streaking straight for the right side of the Camaro beside Harriet's car.

The bike slams with CLANG into the side of the Camaro. Its rider is flung up and forward into the air, twirling passed Harriet's windshield.

We now watch from Harriet's POV, in slow motion. The black-leather-clad motorcyclist sails by Harriet's windshield, airborne. We see a man's face, clearly: His elephant-hide skin tells us that he is well beyond middle-age. Yet thick, black curls of youthful hair emerge from under his helmet. The rider has only one half of a black, bushy, swept-out, waxed mustache. His eyes are weary and grey, and appear to lock with Harriet's for an instant.

We return to normal speed. The body is now lying on the incoming lane to the left of Harriet's Subaru, perfectly still on the blacktop, the head twisted into an impossible angle. Blood seeps from a nostril. Beside the lifeless head, a BMW medallion lies on the pavement, glinting in the sunlight.

The Contemporary Craft of Creating Characters

Memo Today's Cognitive Architecture:

A Case Study in Expressivity*

Silver Stripling • John Linn • Alexander Stripling

version of 02/16/2020

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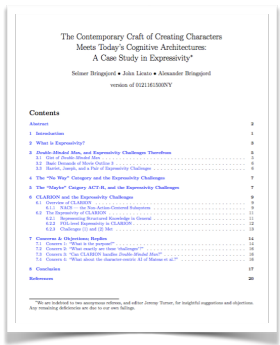
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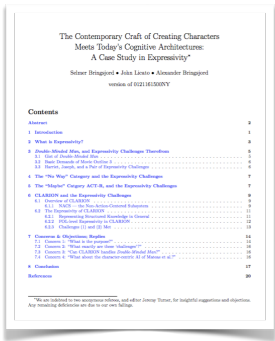
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Climbing the k -order Ladder

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a is a llama, as is b , a likes b , and the father of a is a llama as well.

Climbing the k -order Ladder

$Llama(a) \wedge Llama(b) \wedge Likes(a, b) \wedge Llama(fatherOf(a))$

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Climbing the k -order Ladder

ZOL $Llama(a) \wedge Llama(b) \wedge Likes(a, b) \wedge Llama(fatherOf(a))$

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Climbing the k -order Ladder

There's some thing which is a llama and likes b (which is also a llama), and whose father is a llama too.

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Things x and y , along with the father of x ,
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$$\exists x \exists y \exists R [R(x) \wedge R(y) \wedge Likes(x, y) \wedge R(fatherOf(x))]$$

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FOL $\exists x [Llama(x) \wedge Llama(b) \wedge Likes(x, b) \wedge Llama(fatherOf(x))]$

There's some thing which is a llama and likes b (which is also a llama), and whose father is a llama too.

ZOL $Llama(a) \wedge Llama(b) \wedge Likes(a, b) \wedge Llama(fatherOf(a))$

a is a llama, as is b , a likes b , and the father of a is a llama as well.

Climbing the k -order Ladder

$$\exists x, y \exists R, R^2 [R(x) \wedge R(y) \wedge R^2(x, y) \wedge \textit{Positive}(R^2) \wedge R(\textit{fatherOf}(x))]$$

Things x and y , along with the father of x , share a certain property; and, x R^2 s y , where R^2 is a positive property.

SOL $\exists x \exists y \exists R [R(x) \wedge R(y) \wedge \textit{Likes}(x, y) \wedge R(\textit{fatherOf}(x))]$

Things x and y , along with the father of x , share a certain property (and x likes y).

FOL $\exists x [Llama(x) \wedge Llama(b) \wedge \textit{Likes}(x, b) \wedge Llama(\textit{fatherOf}(x))]$

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Climbing the k -order Ladder

TOL $\exists x, y \exists R, R^2 [R(x) \wedge R(y) \wedge R^2(x, y) \wedge \textit{Positive}(R^2) \wedge R(\textit{fatherOf}(x))]$

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Climbing the k -order Ladder

TOL $\exists x, y \exists R, R^2 [R(x) \wedge R(y) \wedge R^2(x, y) \wedge \textit{Positive}(R^2) \wedge R(\textit{fatherOf}(x))]$

$\mathcal{L}_3$ Things x and y , along with the father of x , share a certain property; and, x R^2 s y , where R^2 is a positive property.

SOL $\exists x \exists y \exists R [R(x) \wedge R(y) \wedge \textit{Likes}(x, y) \wedge R(\textit{fatherOf}(x))]$

$\mathcal{L}_2$ Things x and y , along with the father of x , share a certain property (and x likes y).

FOL $\exists x [Llama(x) \wedge Llama(b) \wedge \textit{Likes}(x, b) \wedge Llama(\textit{fatherOf}(x))]$

$\mathcal{L}_1$ There's some thing which is a llama and likes b (which is also a llama), and whose father is a llama too.

ZOL $Llama(a) \wedge Llama(b) \wedge \textit{Likes}(a, b) \wedge Llama(\textit{fatherOf}(a))$

$\mathcal{L}_0$ a is a llama, as is b , a likes b , and the father of a is a llama as well.

Climbing the k -order Ladder

⋮

TOL $\exists x, y \exists R, R^2 [R(x) \wedge R(y) \wedge R^2(x, y) \wedge \textit{Positive}(R^2) \wedge R(\textit{fatherOf}(x))]$

$\mathcal{L}_3$ Things x and y , along with the father of x , share a certain property; and, x R^2 s y , where R^2 is a positive property.

SOL $\exists x \exists y \exists R [R(x) \wedge R(y) \wedge \textit{Likes}(x, y) \wedge R(\textit{fatherOf}(x))]$

$\mathcal{L}_2$ Things x and y , along with the father of x , share a certain property (and x likes y).

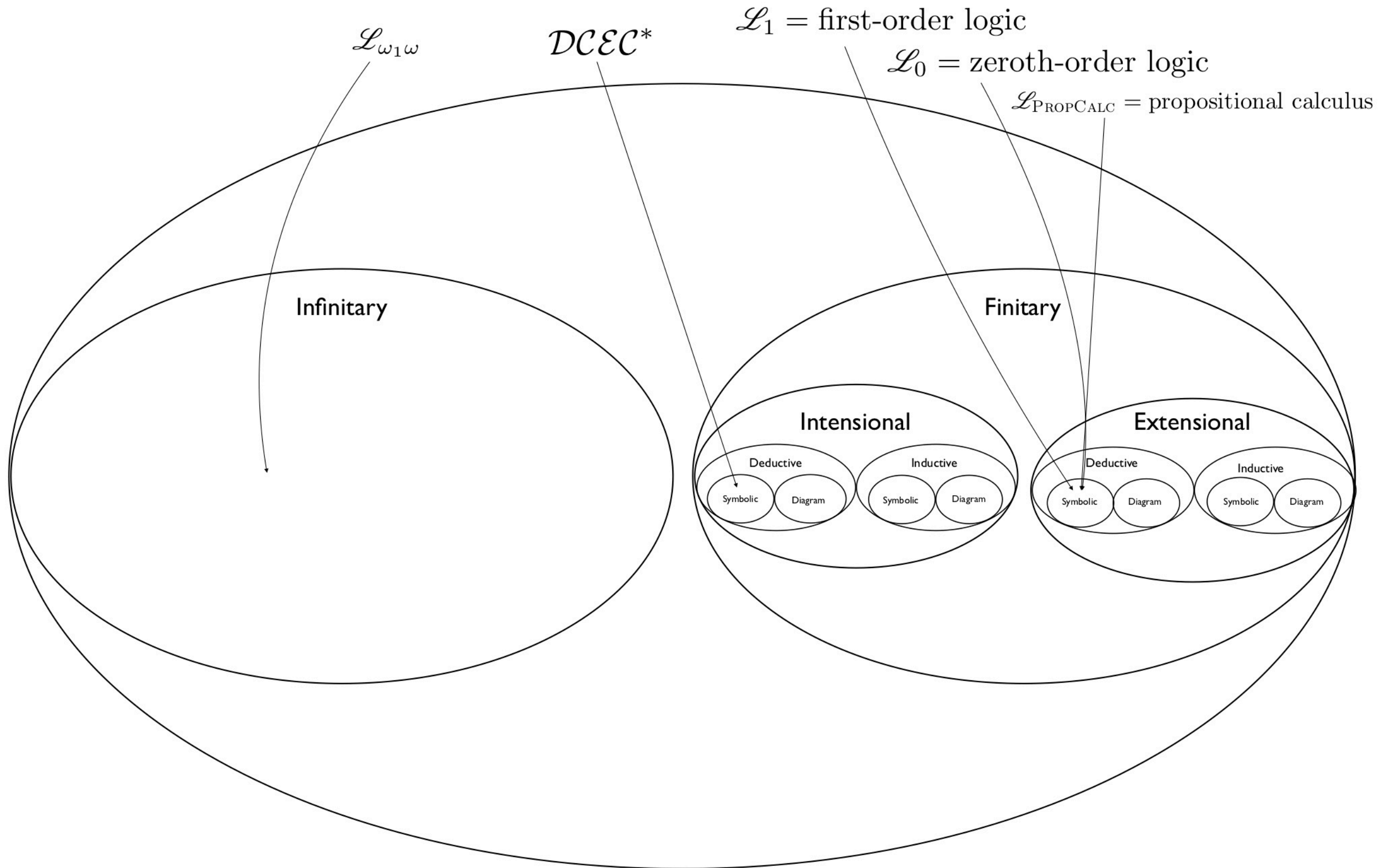
FOL $\exists x [Llama(x) \wedge Llama(b) \wedge \textit{Likes}(x, b) \wedge Llama(\textit{fatherOf}(x))]$

$\mathcal{L}_1$ There's some thing which is a llama and likes b (which is also a llama), and whose father is a llama too.

ZOL $Llama(a) \wedge Llama(b) \wedge \textit{Likes}(a, b) \wedge Llama(\textit{fatherOf}(a))$

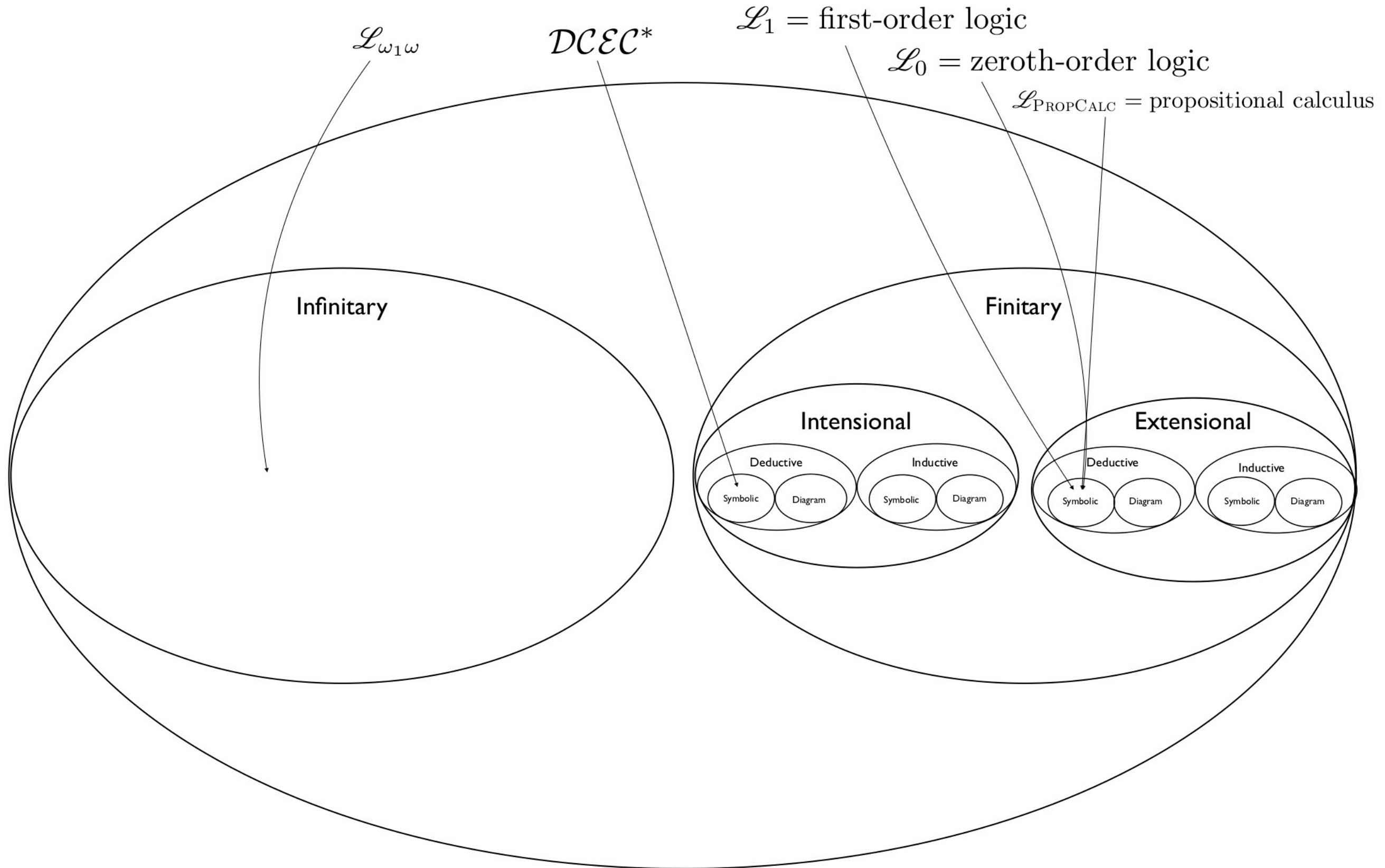
$\mathcal{L}_0$ a is a llama, as is b , a likes b , and the father of a is a llama as well.

The Universe of Logics

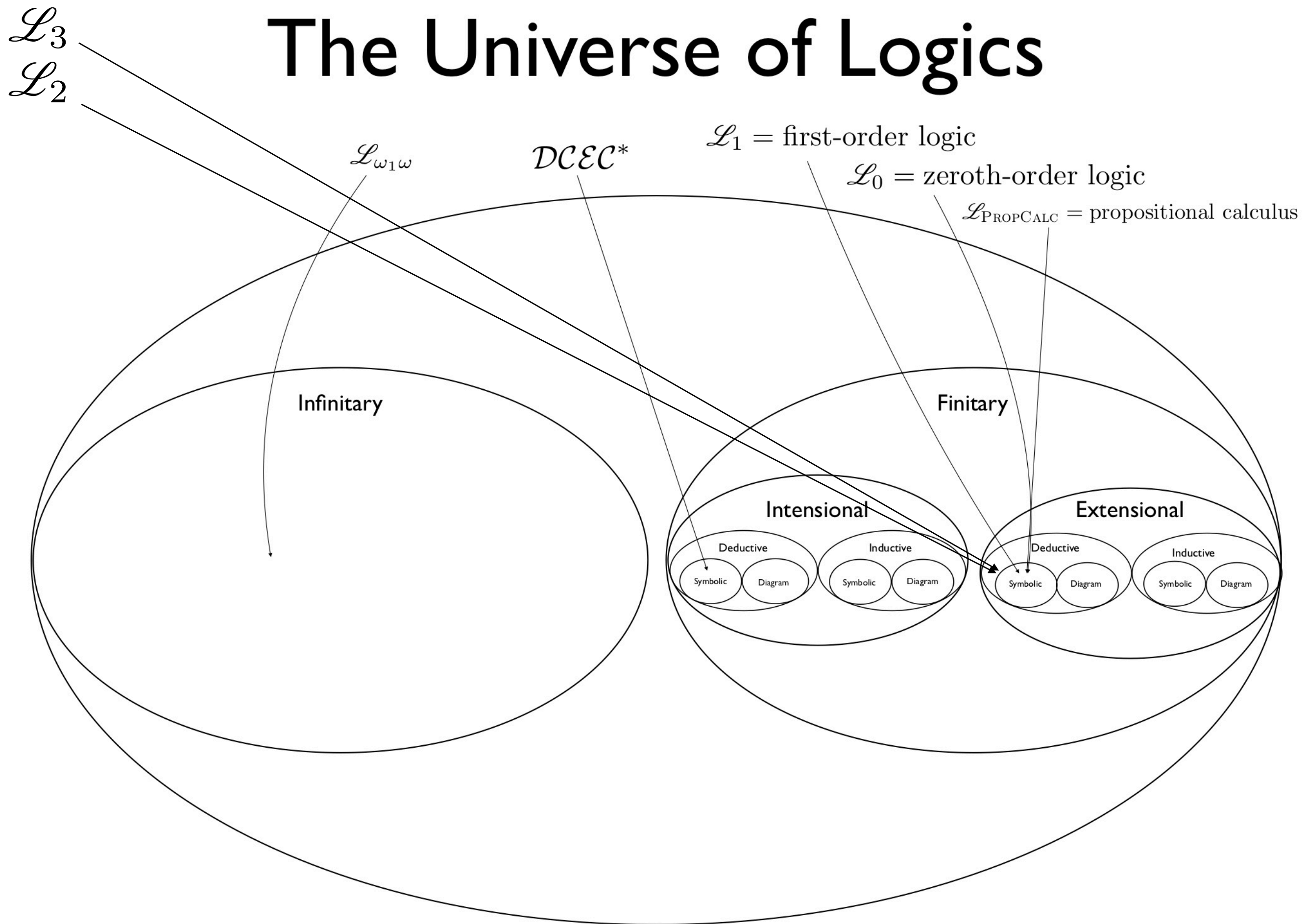


$\mathcal{L}_3$
 $\mathcal{L}_2$

The Universe of Logics



The Universe of Logics



Climbing the k -order Ladder

⋮

TOL $\exists x, y \exists R, R^2 [R(x) \wedge R(y) \wedge R^2(x, y) \wedge \textit{Positive}(R^2) \wedge R(\textit{fatherOf}(x))]$

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SOL $\exists x \exists y \exists R [R(x) \wedge R(y) \wedge \textit{Likes}(x, y) \wedge R(\textit{fatherOf}(x))]$

$\mathcal{L}_2$ Things x and y , along with the father of x , share a certain property (and x likes y).

FOL $\exists x [Llama(x) \wedge Llama(b) \wedge \textit{Likes}(x, b) \wedge Llama(\textit{fatherOf}(x))]$

$\mathcal{L}_1$ There's some thing which is a llama and likes b (which is also a llama), and whose father is a llama too.

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Climbing the k -order Ladder

⋮

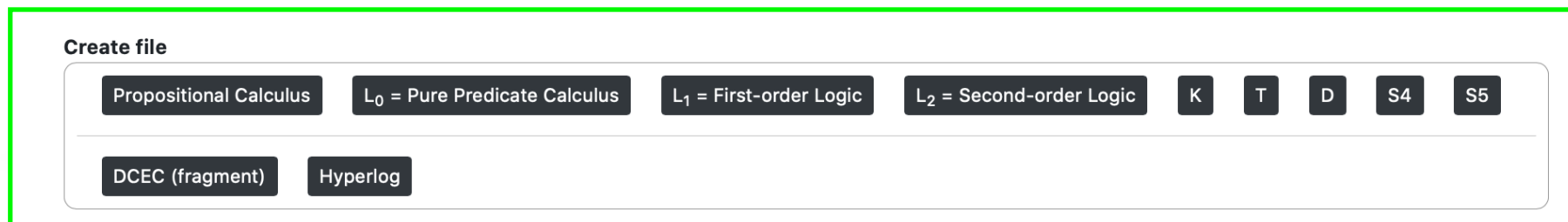
TOL

$$\exists x, y \exists R, R^2 [R(x) \wedge R(y) \wedge R^2(x, y) \wedge \text{Positive}(R^2) \wedge R(\text{fatherOf}(x))]$$

$\mathcal{L}_3$

Things x and y , along with the father of x , share a certain property; and, x R^2 s y , where R^2 is a positive property.

SOL



$\mathcal{L}_2$

Things x and y , along with the father of x , share a certain property (and x likes y).

FOL

$$\exists x [Llama(x) \wedge Llama(b) \wedge Likes(x, b) \wedge Llama(\text{fatherOf}(x))]$$

$\mathcal{L}_1$

There's some thing which is a llama and likes b (which is also a llama), and whose father is a llama too.

ZOL

$$Llama(a) \wedge Llama(b) \wedge Likes(a, b) \wedge Llama(\text{fatherOf}(a))$$

$\mathcal{L}_0$

a is a llama, as is b , a likes b , and the father of a is a llama as well.

Climbing the k -order Ladder

⋮

TOL

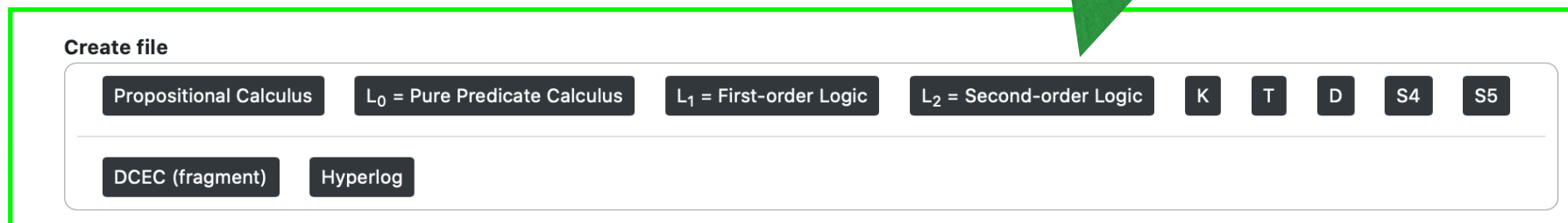
$\mathcal{L}_3$

$\exists x, y \exists R, R^2 [R(x) \wedge R(y) \wedge R^2(x, y) \wedge \text{Positive}(R^2) \wedge R(\text{fatherOf}(x))]$

Things x and y , along with the father of x , share a certain property; and, x R^2 s y , where R^2 is a positive property.

SOL

$\mathcal{L}_2$



Things x and y , along with the father of x , share a certain property (and x likes y).

FOL

$\mathcal{L}_1$

$\exists x [Llama(x) \wedge Llama(b) \wedge Likes(x, b) \wedge Llama(\text{fatherOf}(x))]$

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ZOL

$\mathcal{L}_0$

$Llama(a) \wedge Llama(b) \wedge Likes(a, b) \wedge Llama(\text{fatherOf}(a))$

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Og med det .. er vårt klasse møte ferdig!