

version 102422NY

The Argument for God's Existence

Selmer Bringsjord

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Troy, New York 12180 USA

IFLAI2
10/24/2022



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The Argument for God's Existence from AI

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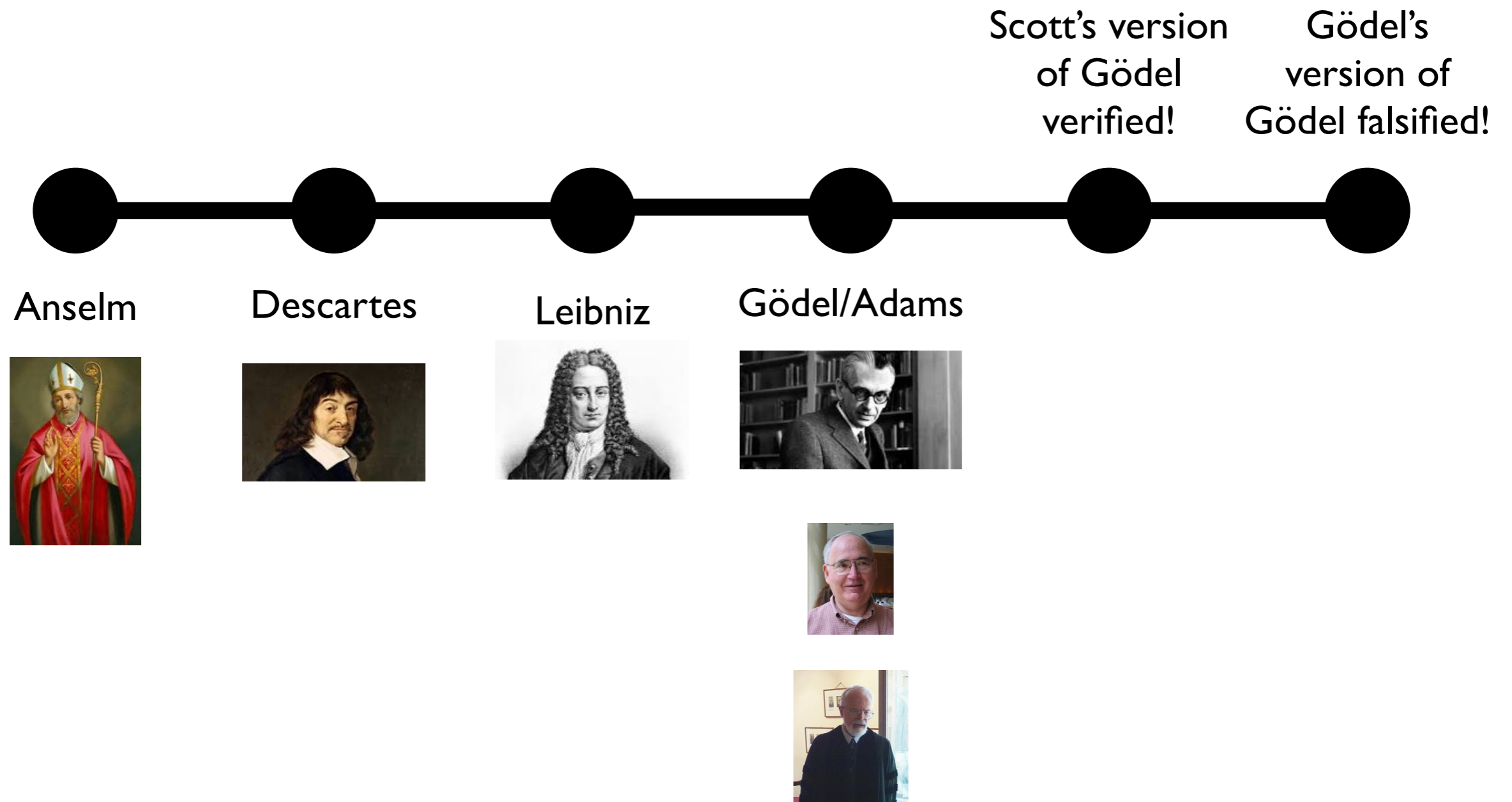
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The Ontological/Modal Argument Meets AI

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Automating Gödel's Ontological Proof of God's Existence with Higher-order Automated Theorem Provers

Christoph Benz Müller¹ and Bruno Woltzenlogel Paleo²

Abstract. Kurt Gödel's ontological argument for God's existence has been formalized and automated on a computer with higher-order automated theorem provers. From Gödel's premises, the computer proved: necessarily, there exists God. On the other hand, the theorem provers have also confirmed prominent criticism on Gödel's ontological argument, and they found some new results about it.

The background theory of the work presented here offers a novel perspective towards a *computational theoretical philosophy*.

1 INTRODUCTION

Kurt Gödel proposed an argumentation formalism to prove the existence of God [23, 30]. Attempts to prove the existence (or non-existence) of God by means of abstract, ontological arguments are an old tradition in western philosophy. Before Gödel, several prominent philosophers, including St. Anselm of Canterbury, Descartes and Leibniz, have presented similar arguments. Moreover, there is an impressive body of recent and ongoing work (cf. [31, 19, 18] and the references therein). Ontological arguments, for or against the existence of God, illustrate well an essential aspect of metaphysics: some (necessary) facts for our existing world are deduced by purely a priori, analytical means from some abstract definitions and axioms.

What motivated Gödel as a logician was the question, whether it

- | | | |
|----|--|--|
| A1 | Either a property or its negation is positive, but not both: | $\forall\phi[P(\neg\phi) \equiv \neg P(\phi)]$ |
| A2 | A property necessarily implied by a positive property is positive: | $\forall\phi\forall\psi[(P(\phi) \wedge \Box\forall x[\phi(x) \supset \psi(x)]) \supset P(\psi)]$ |
| T1 | Positive properties are possibly exemplified: | $\forall\phi[P(\phi) \supset \Diamond\exists x\phi(x)]$ |
| D1 | A <i>God-like</i> being possesses all positive properties: | $G(x) \equiv \forall\phi[P(\phi) \supset \phi(x)]$ |
| A3 | The property of being God-like is positive: | $P(G)$ |
| C | Possibly, God exists: | $\Diamond\exists xG(x)$ |
| A4 | Positive properties are necessarily positive: | $\forall\phi[P(\phi) \supset \Box P(\phi)]$ |
| D2 | An <i>essence</i> of an individual is a property possessed by it and necessarily implying any of its properties: | $\phi \text{ ess. } x \equiv \phi(x) \wedge \forall\psi(\psi(x) \supset \Box\forall y(\phi(y) \supset \psi(y)))$ |
| T2 | Being God-like is an essence of any God-like being: | $\forall x[G(x) \supset G \text{ ess. } x]$ |
| D3 | <i>Necessary existence</i> of an individ. is the necessary exemplification of all its essences: | $NE(x) \equiv \forall\phi[\phi \text{ ess. } x \supset \Box\exists y\phi(y)]$ |
| A5 | Necessary existence is a positive property: | $P(NE)$ |
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Figure 1. Scott's version of Gödel's ontological argument [30].

Proceedings of the Twenty-Fifth International Joint Conference on Artificial Intelligence (IJCAI-16)

The Inconsistency in Gödel's Ontological Argument: A Success Story for AI in Metaphysics

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Bruno Woltzenlogel Paleo

Australian National University
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Abstract

This paper discusses the discovery of the inconsistency in Gödel's ontological argument as a success story for artificial intelligence. Despite the popularity of the argument since the appearance of Gödel's manuscript in the early 1970's, the inconsistency of the axioms used in the argument remained unnoticed until 2013, when it was detected automatically by the higher-order theorem prover

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on the proof [Fuhrmann, 2016].

The in-depth analysis presented here substantially extends previous computer-assisted studies of Gödel's ontological argument. Similarly to the related work [Benz Müller and Woltzenlogel-Paleo, 2013a; 2014] the analysis has been conducted with automated theorem provers for classical higher-order logic (HOL; cf. [Andrews, 2014] and the references therein), even though Gödel's proof is actually formulated in higher-order *modal* logic (HOML; cf. [Muskens, 2006]

T3 Necessarily, God exists: $\Box \exists x G(x)$

Figure 1. Scott's version of Gödel's ontological argument [30].

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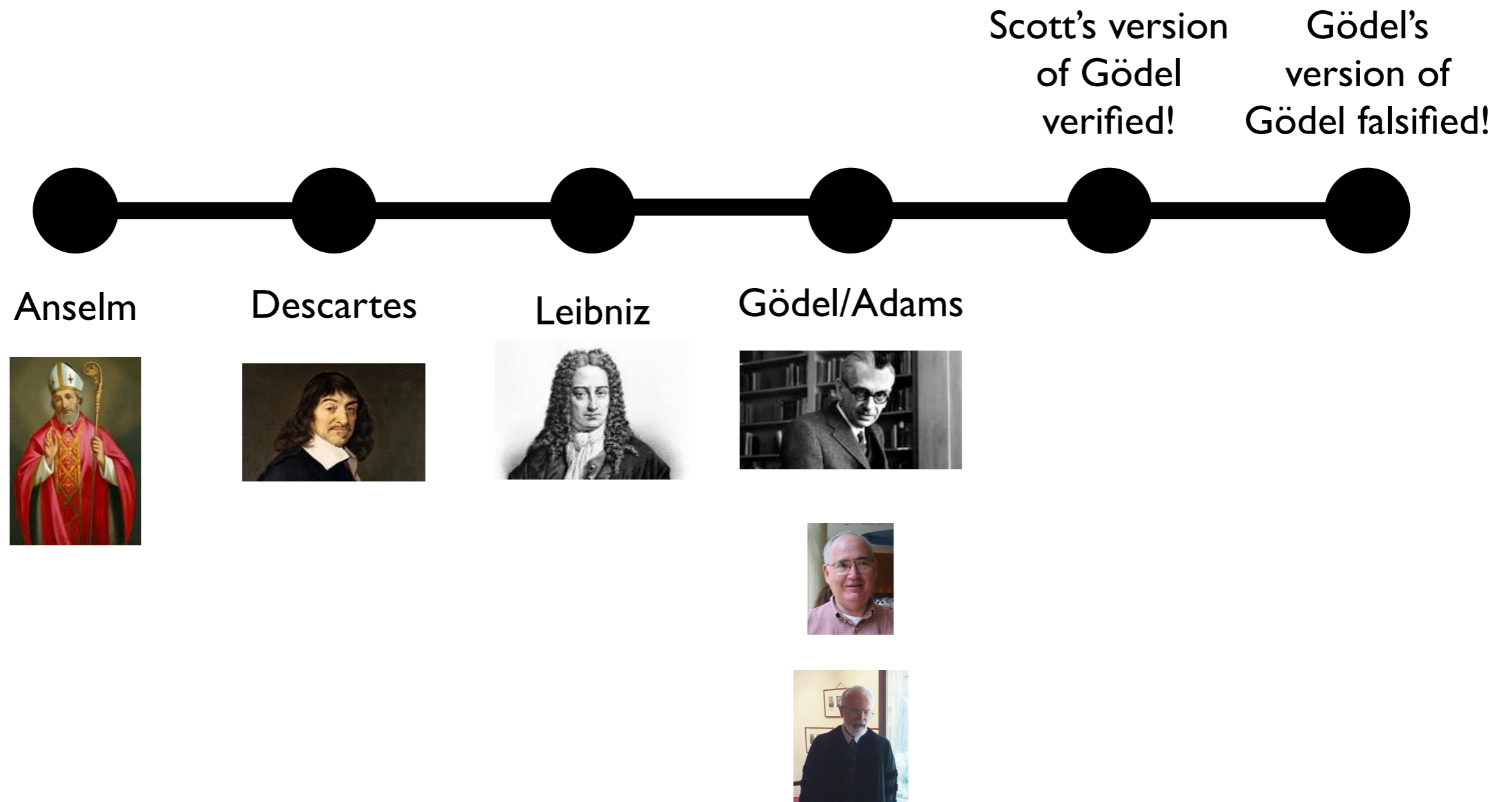
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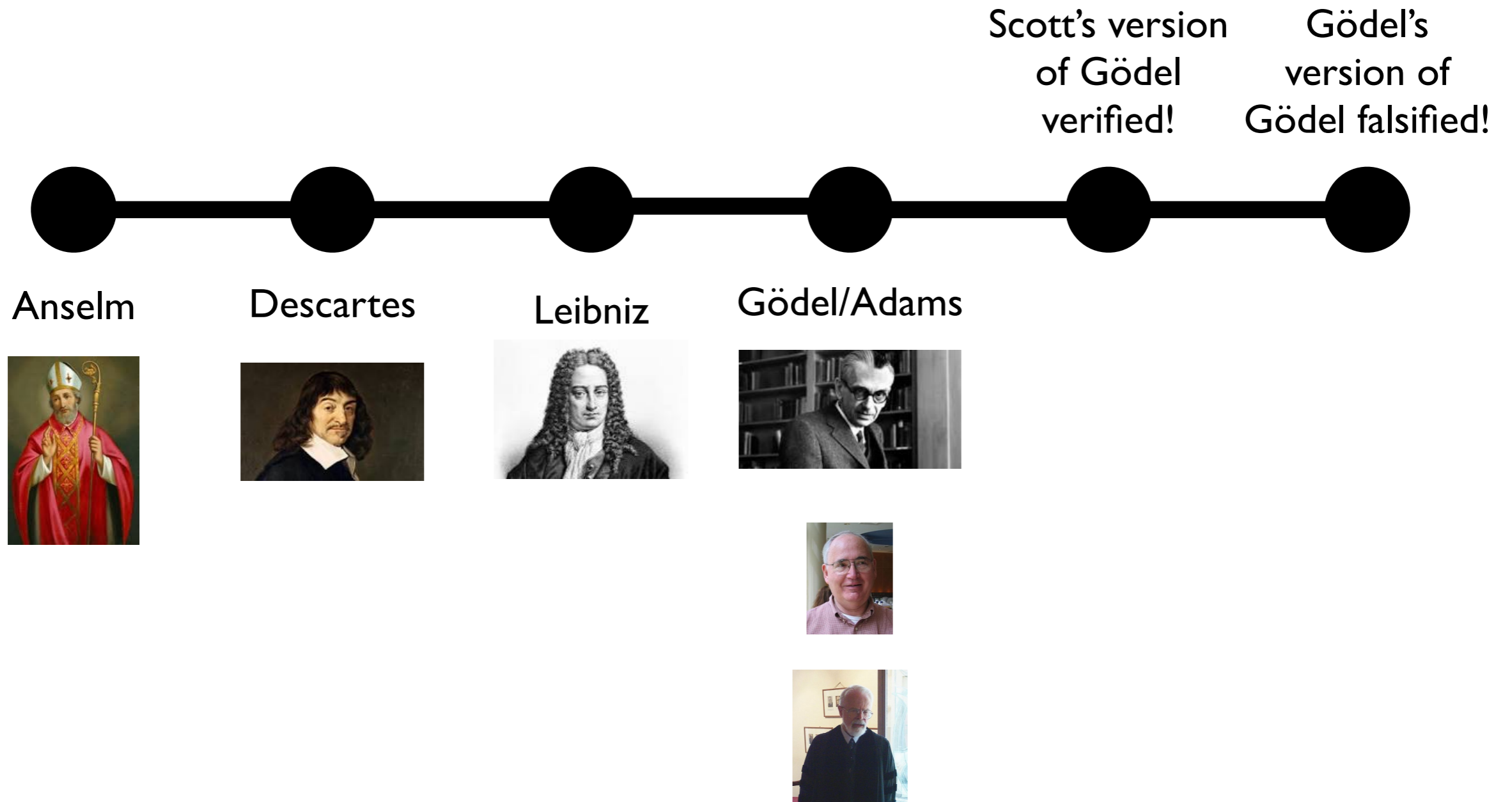
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The Ontological/Modal Argument Meets AI

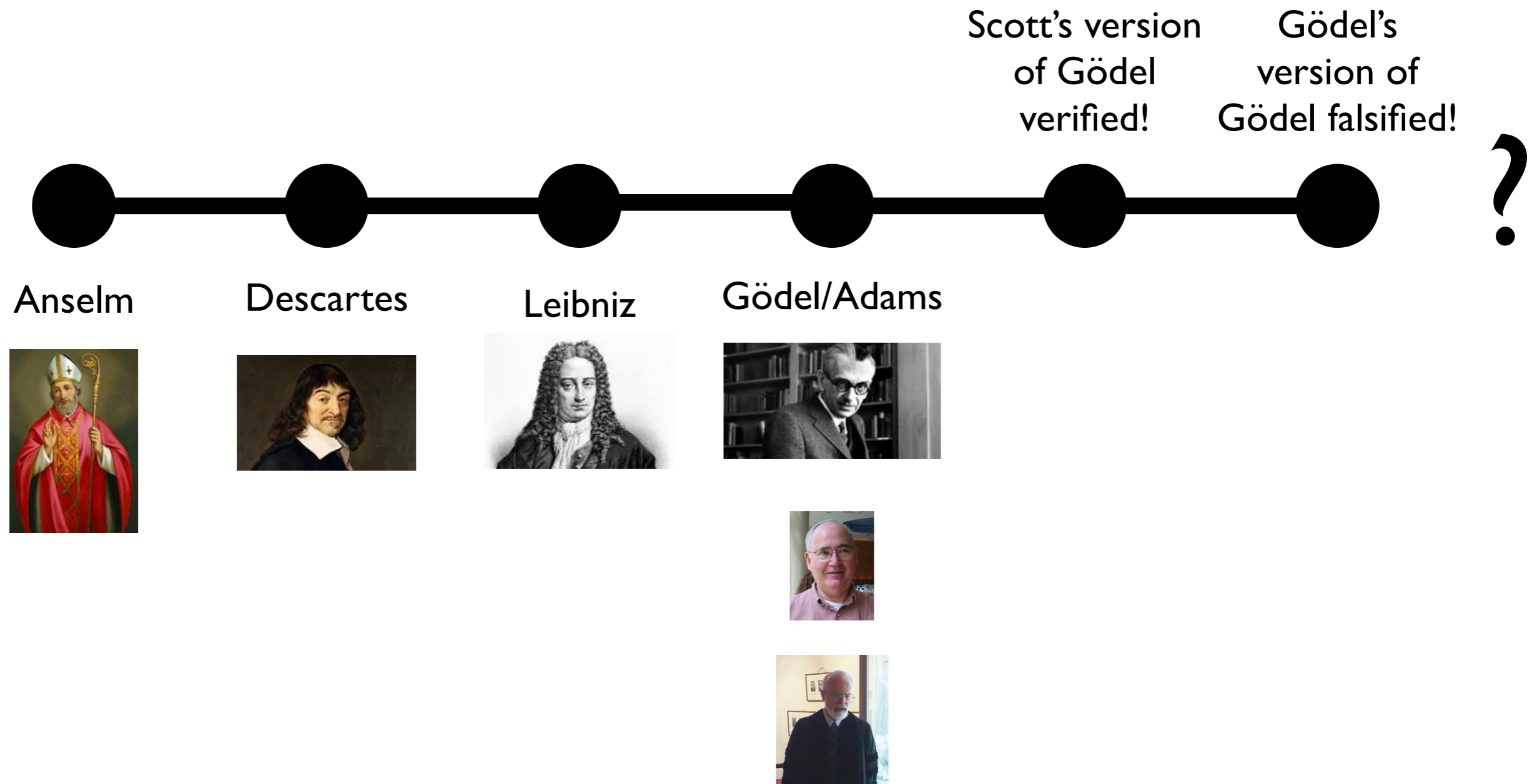


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The Ontological/Modal Argument Meets AI



The Ontological/Modal Argument Meets AI



This is argumentation for
God's existence that *uses*
AI; it's not *based* on AI.

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God's existence that *uses*
AI; it's not *based* on AI.

Today, The Argument for
God's Existence *from* AI ...

The Canyon of Discontinuity (or Darwin's Dread)



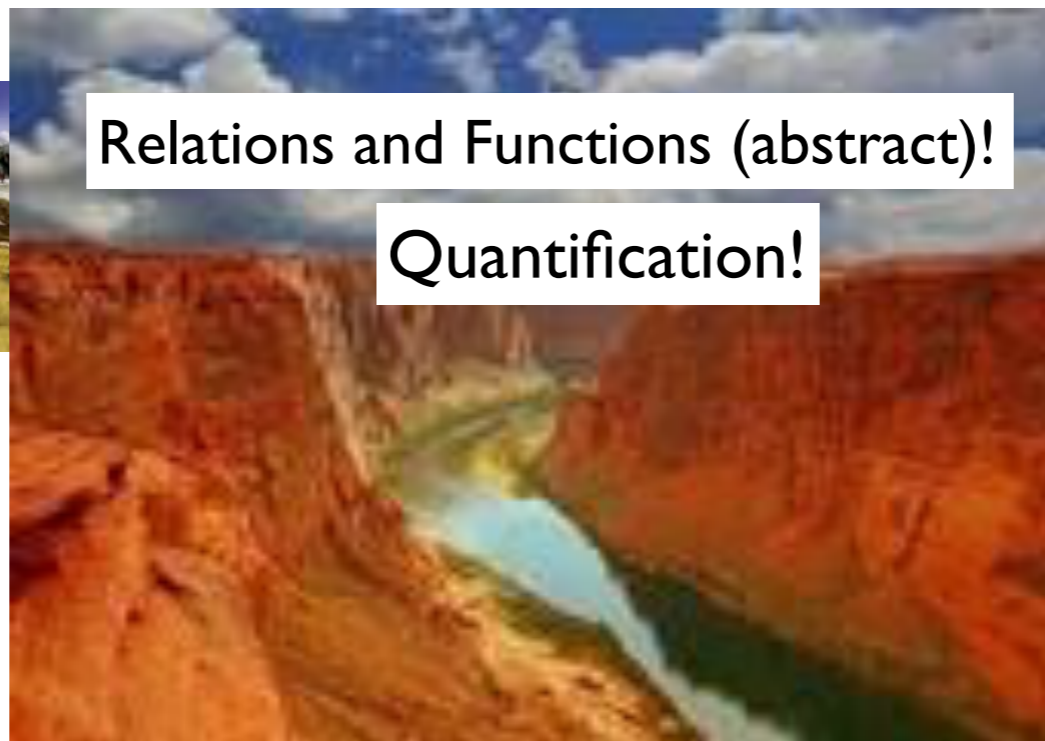
gradual increase in
cognitive powers

The Canyon of Discontinuity (or Darwin's Dread)



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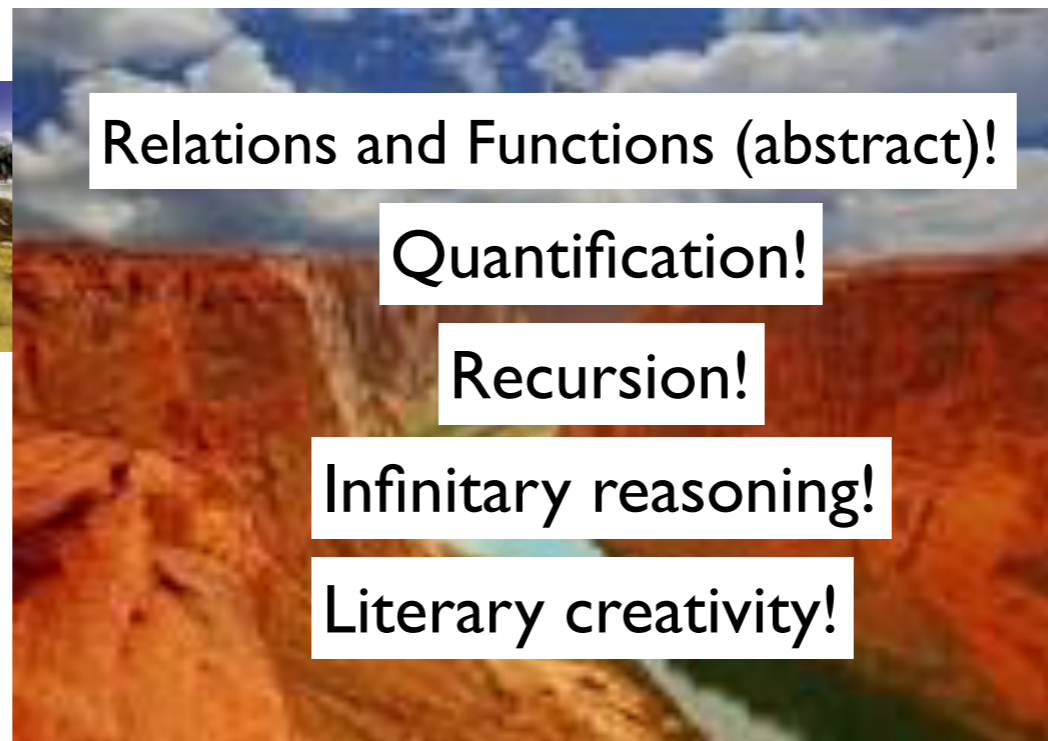
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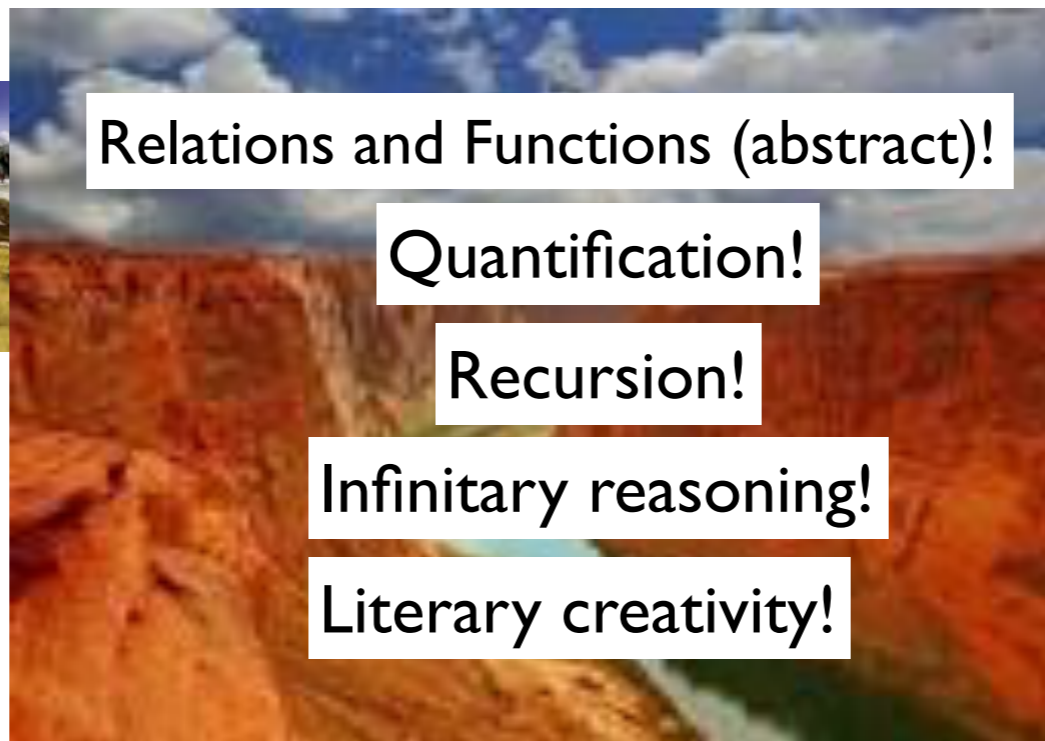
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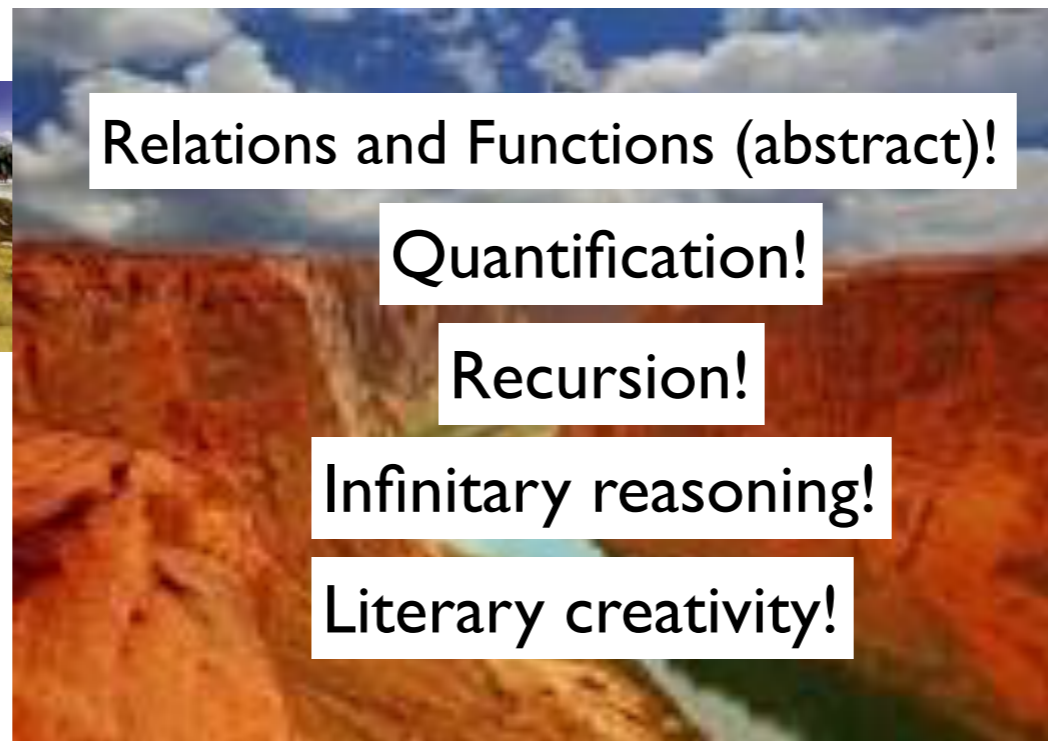
P^∞

The Canyon of Discontinuity (or Darwin's Dread)



P^{HG}

gradual increase in
cognitive powers



P^∞

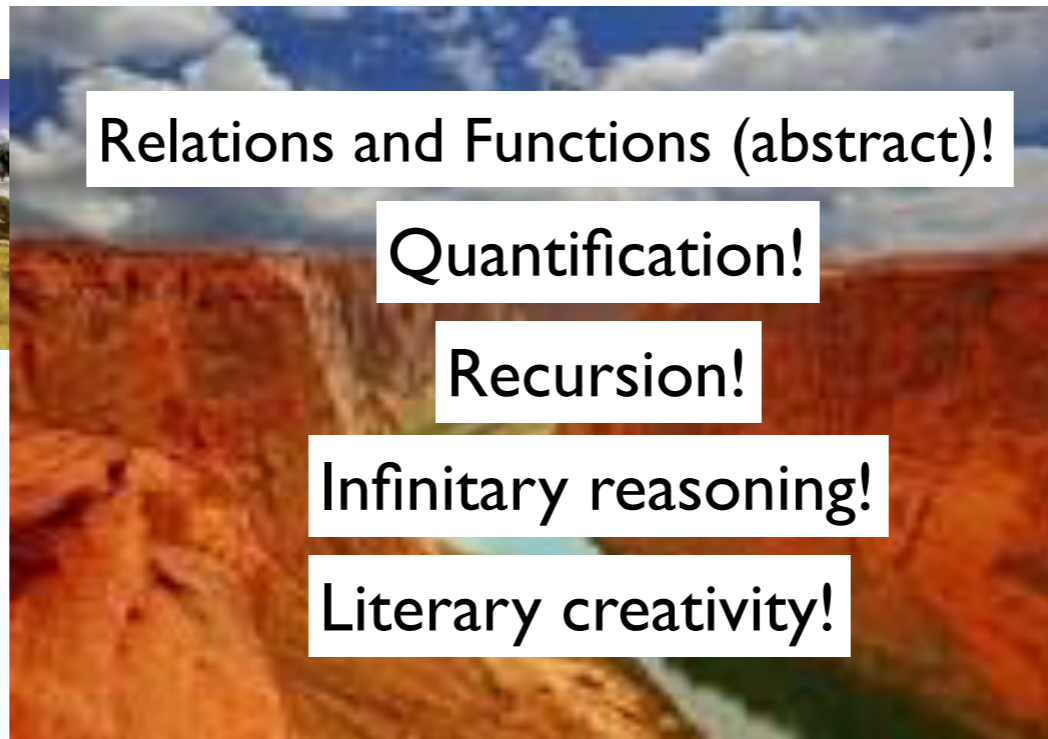
The Canyon of Discontinuity (or Darwin's Dread)



P^{HG}



gradual increase in
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P^∞

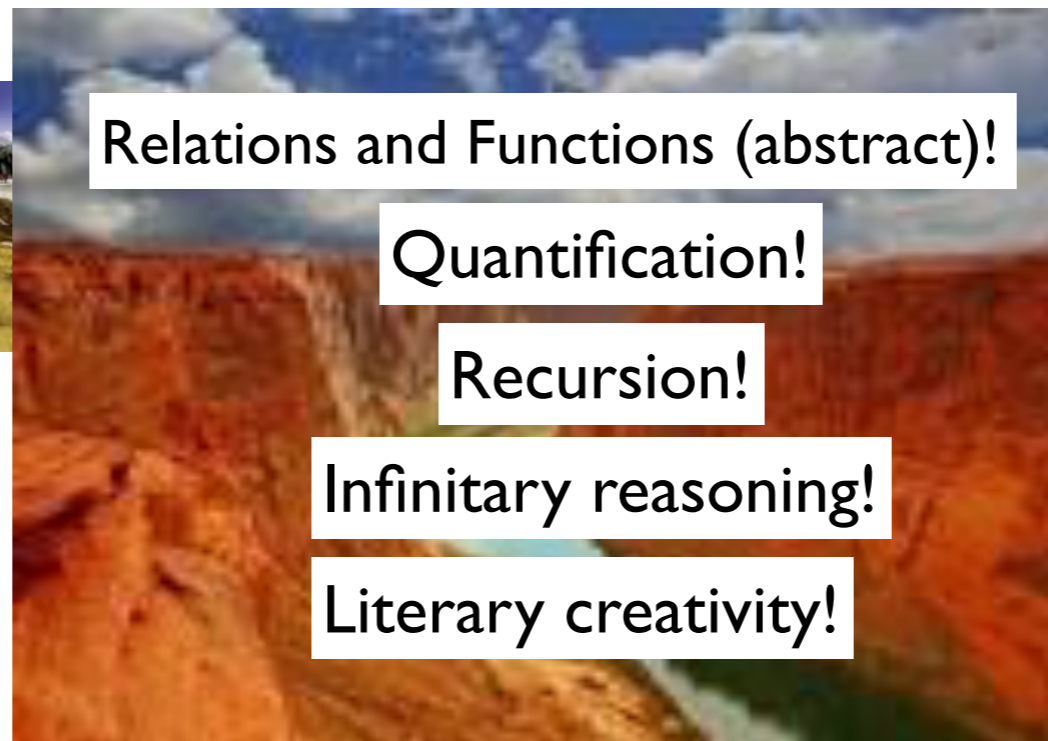
The Canyon of Discontinuity (or Darwin's Dread)



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P^{∞}

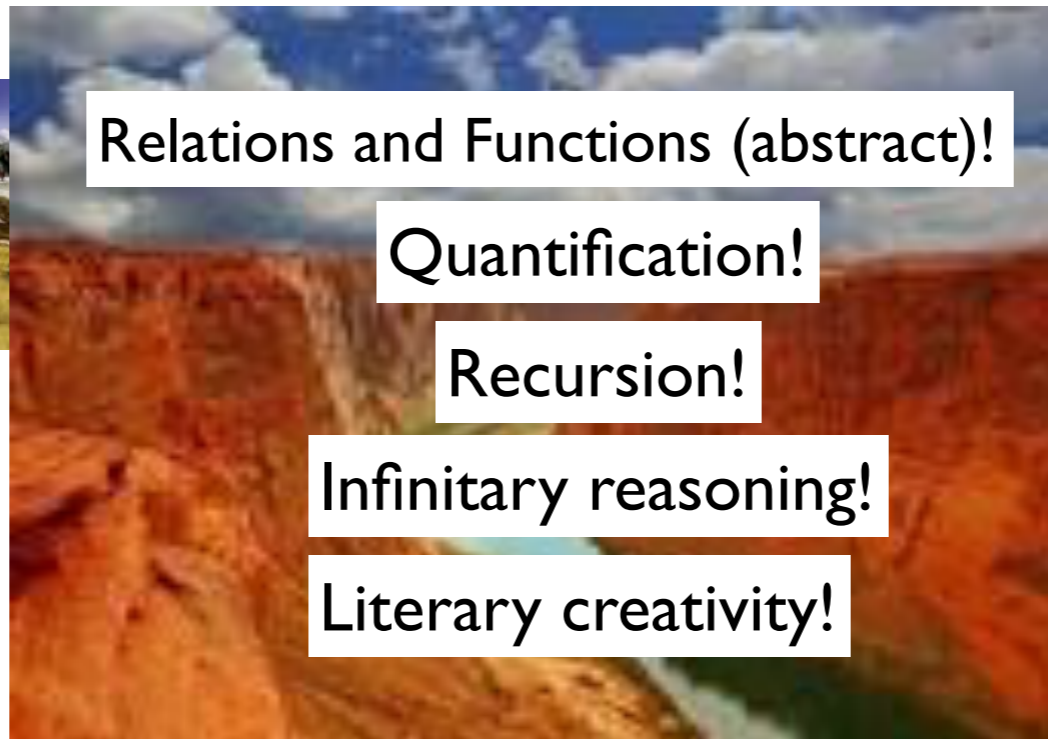
The Canyon of Discontinuity (or Darwin's Dread)



P^{HG}



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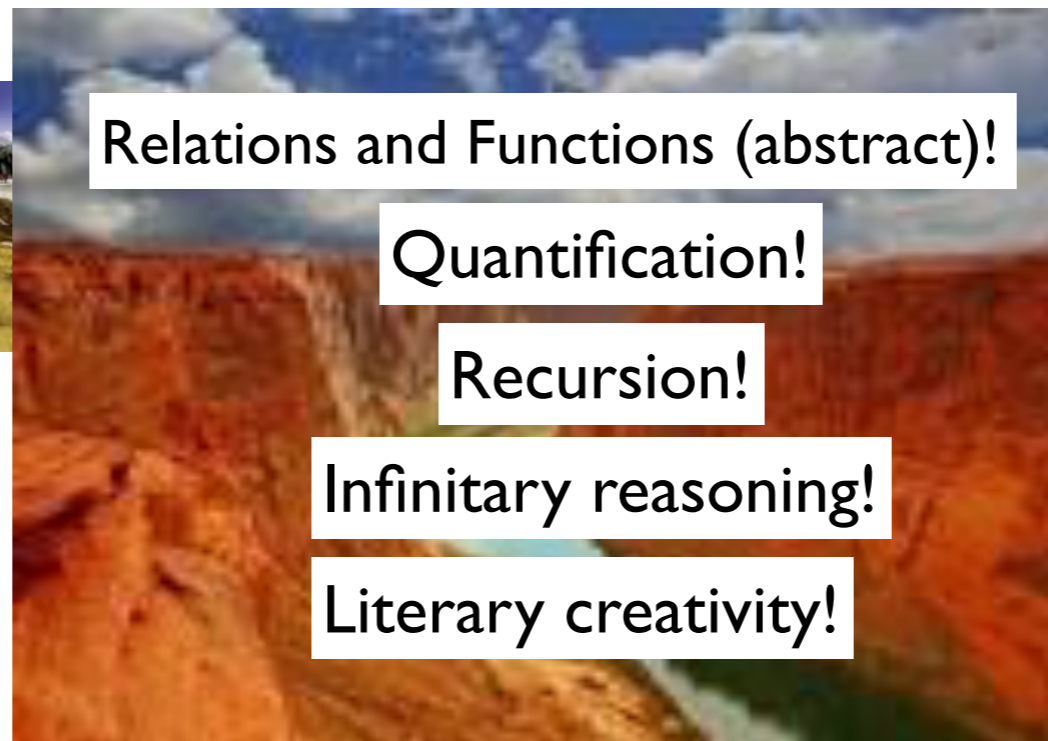
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P^{HG}



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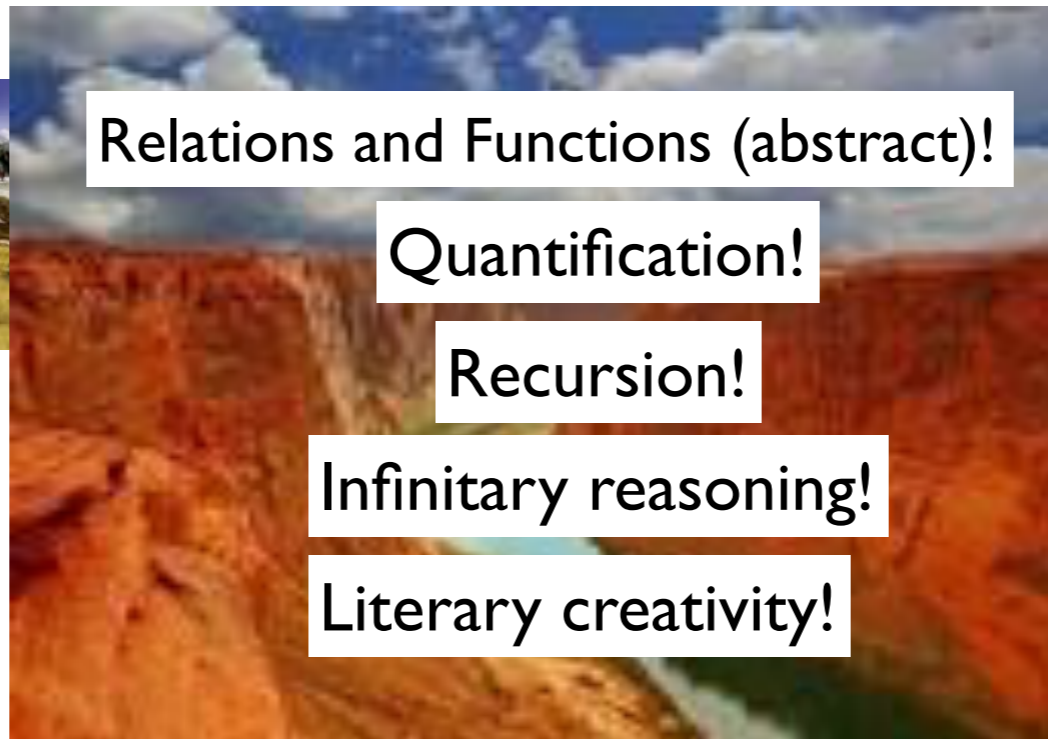
The Canyon of Discontinuity (or Darwin's Dread)



P^{HG}



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P^{∞}

What about neanderthals?

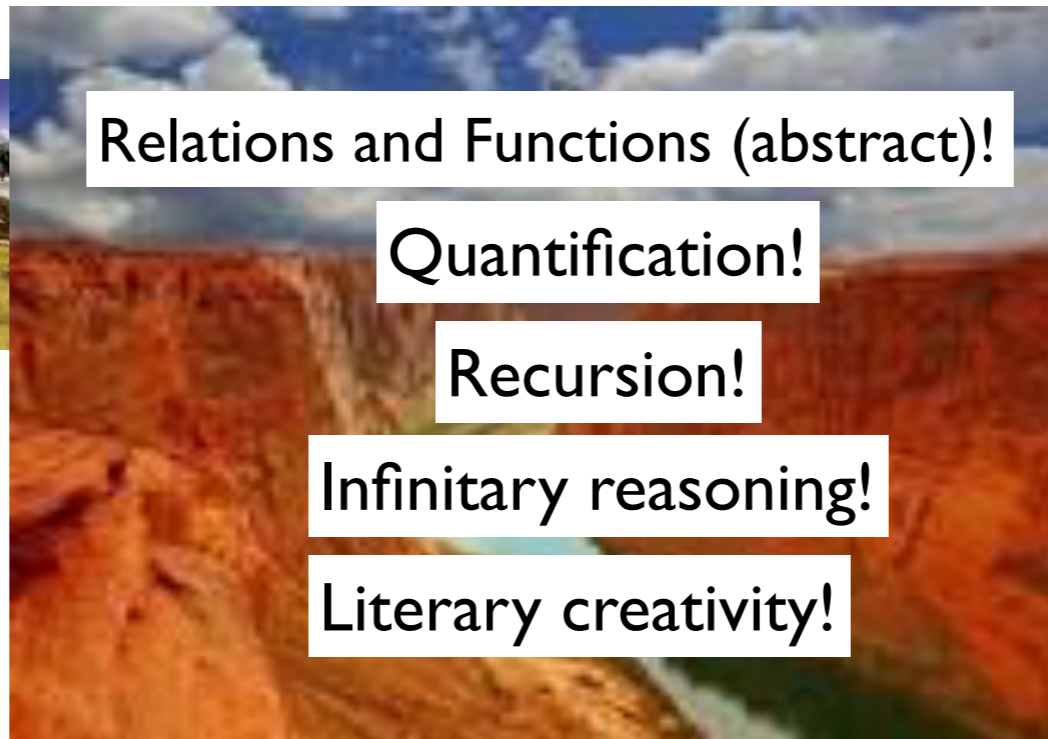
The Canyon of Discontinuity (or Darwin's Dread)



P^{HG}



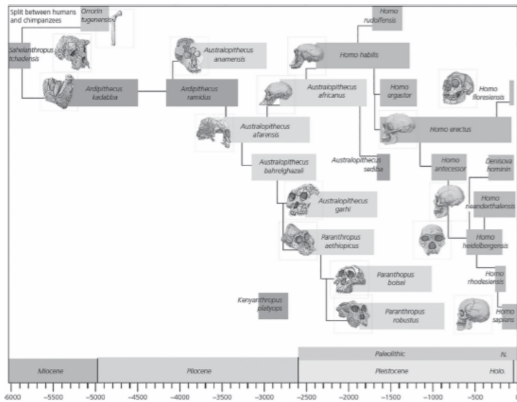
gradual increase in
cognitive powers



P^∞

What about neanderthals?

The Canyon of Discontinuity (or Darwin's Dread)



Relations and Functions (abstract)!

Quantification!

Recursion!

Infinitary reasoning!

Literary creativity!



P^∞



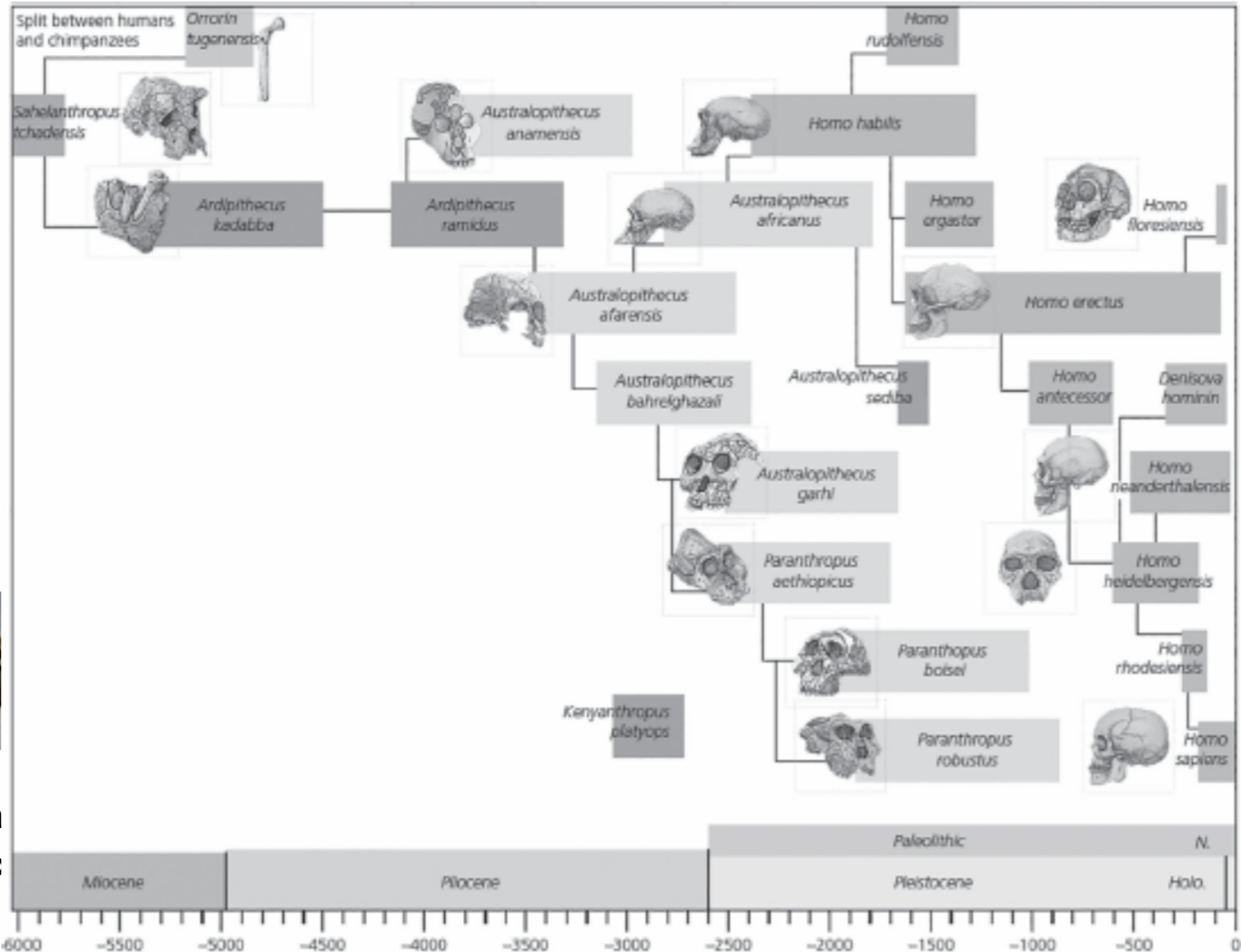
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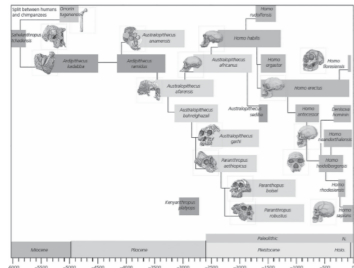
The Canyon of Discontinuity



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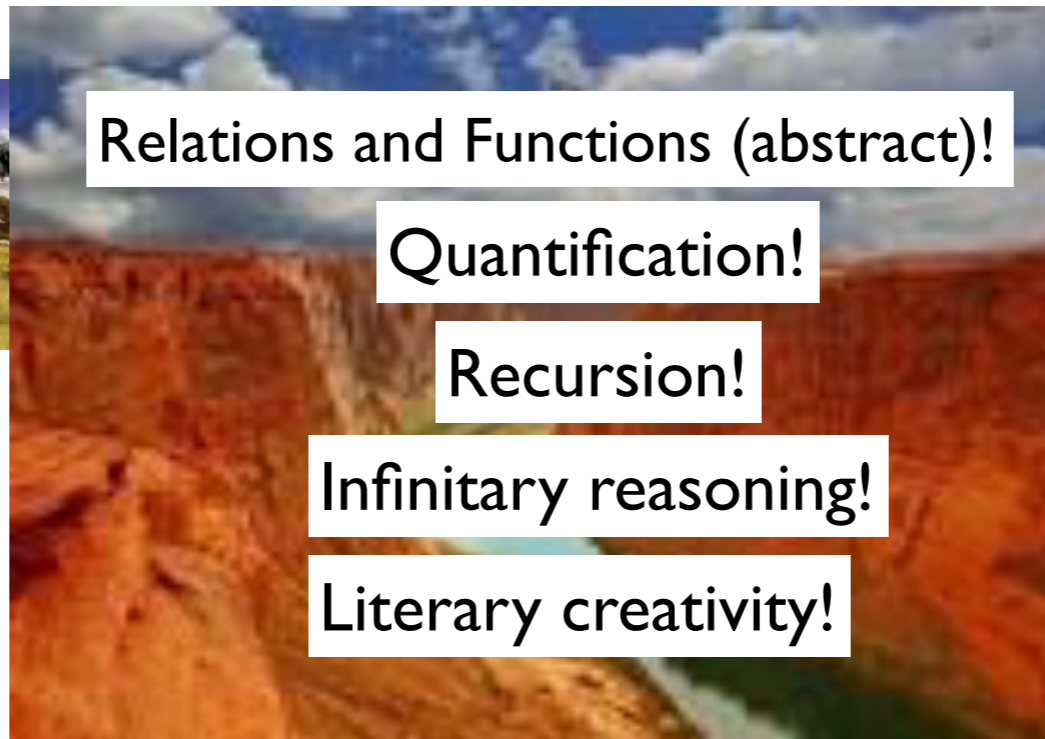
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P^{HG}



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P^{∞}

The Argument

	(1)	Hunter-gatherers possessed the cognitive power P^∞ to e.g. invent the calculus and create literary art of the caliber of Blecher/Proust/Ibsen/...	undisputed
	(2)	AI shows us that these early versions of us, to hunt and gather, needed only humble cognitive power P^{HG} , where $P^{\text{HG}} < P^\infty$, because $P^{\text{AI}} \approx P^{\text{HG}}$ (where P^{AI} is a limit on the cognitive power of AI), and AIs can hunt and gather.	see AI today
\therefore	(3)	We have $(P^\infty - P^{\text{HG}})$.	abstraction (1), (2)
	(4)	Our having $(P^\infty - P^{\text{HG}})$, <i>contra</i> Darwin, is inexplicable by gradual mutation and natural selection (i.e. P^∞ is discontinuous from P^{HG}).	see critique of <i>DoM</i> see theorem/proof
	(5)	If our having $(P^\infty - P^{\text{HG}})$ is explicable, then $E_1 \vee E_2 \vee \text{God exists}$.	sub-arg
	(6)	Our having $(P^\infty - P^{\text{HG}})$ is explicable.	undeniable
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Set “subtraction”: The extreme cognitive powers, but none of the routine ones. So, that which we share with hunter-gatherer activity & the lower animals is irrelevant.

Gentner, T., Fenn, K., Margoliash, D. & Nusbaum, H. (2006) "Recursive Syntactic Pattern Learning by Songbirds" *Nature* **440**: 1204–1207.



Humans



Songbirds

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Humans



Songbirds

the birds sing differentially based on what song they hear

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$$P^\infty - P^{\text{HG}} / P^\infty - P^{\text{AI}}$$

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See ...

See . . .

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Library Penn, Holyoak, Povinelli.2008

doi: 10.1017/S0140525X08003543

Darwin's mistake: Explaining the discontinuity between human and nonhuman minds

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Abstract: Over the last quarter century, the dominant tendency in comparative cognitive psychology has been to emphasize the similarities between human and nonhuman minds and to downplay the differences as “one of degree and not of kind” (Darwin 1871). In the present target article, we argue that Darwin was mistaken: the profound biological continuity between human and nonhuman animals masks an equally profound discontinuity between human and nonhuman minds. To wit, there is a significant discontinuity in the degree to which human and nonhuman animals are able to approximate the higher-order, systematic, relational capabilities of a physical symbol system (PSS) (Newell 1980). We show that this symbolic-relational discontinuity pervades nearly every domain of cognition and runs much deeper than even the spectacular scaffolding provided by language or culture alone can explain. We propose a representational-level specification as to where human and nonhuman animals’ abilities to approximate a PSS are similar and where they differ. We conclude by suggesting that recent symbolic-connectionist models of cognition shed new light on the mechanisms that underlie the gap between human and nonhuman minds.

Keywords: analogy; animal cognition; causal learning; connectionism; Darwin; discontinuity; evolution; human mind; language; language of thought; physical symbol system; reasoning; same-different; theory of mind

1. Introduction

Human animals – and no other – build fires and wheels, diagnose each other’s illnesses, communicate using symbols, navigate with maps, risk their lives for ideals, collaborate with each other, explain the world in terms of hypothetical causes, punish strangers for breaking rules, imagine impossible scenarios, and teach each other how to do all of the above. At first blush, it might appear obvious that human minds are qualitatively different from those of every other animal on the planet. Ever since Darwin, however, the dominant tendency in comparative cognitive psychology has been to emphasize the continuity between human and nonhuman minds and to downplay the differences as “one of degree and not of kind” (Darwin 1871). Particularly in the last quarter century,

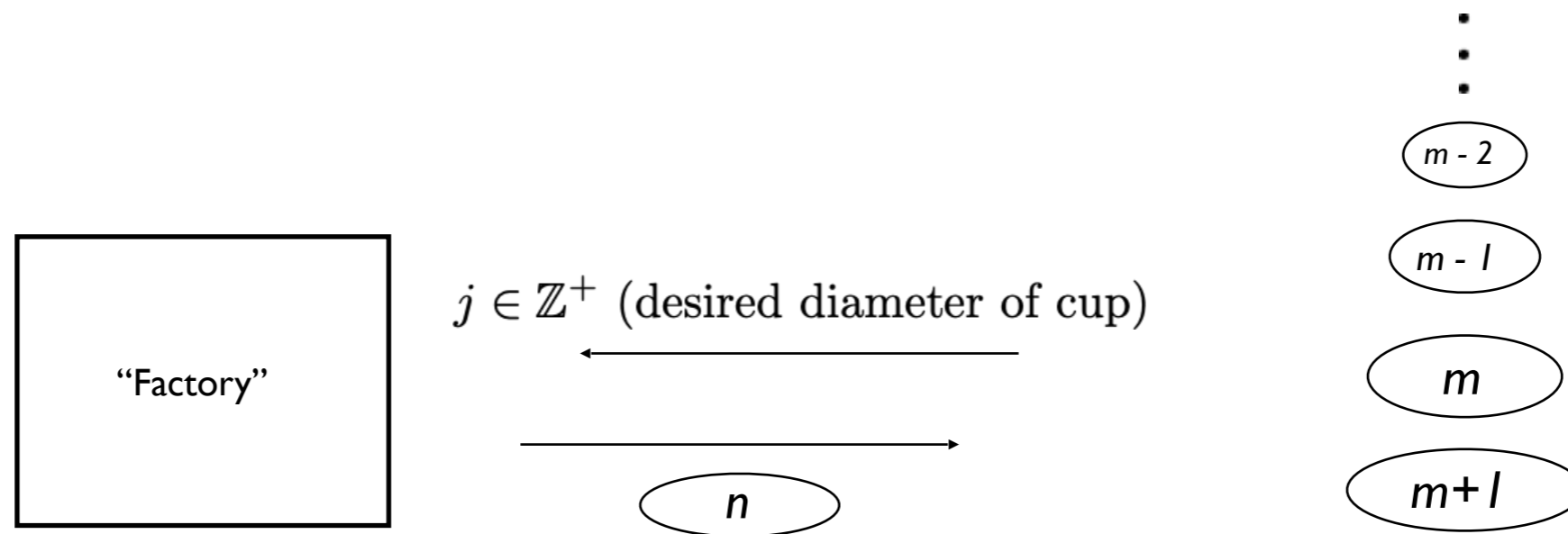
many prominent comparative researchers have claimed that the traditional hallmarks of human cognition – for example, complex tool use, grammatically structured language, causal-logical reasoning, mental state attribution, metacognition, analogical inferences, mental time travel, culture, and so on – are not nearly as unique as we once thought (see, e.g., Bekoff et al. 2002; Call 2006; Clayton et al. 2003; de Waal & Tyack 2003; Matsuzawa 2001; Pepperberg 2002; Rendell & Whitehead 2001; Savage-Rumbaugh et al. 1998; Smith et al. 2003; Tomasello et al. 2003a). Pepperberg (2005, p. 469) aptly sums up the comparative consensus as follows: “for over 35 years, researchers have been demonstrating through tests both in the field and in the laboratory that the capacities of nonhuman animals to solve complex problems form a continuum with those of

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Selmer's Seriated Cup Challenge #1

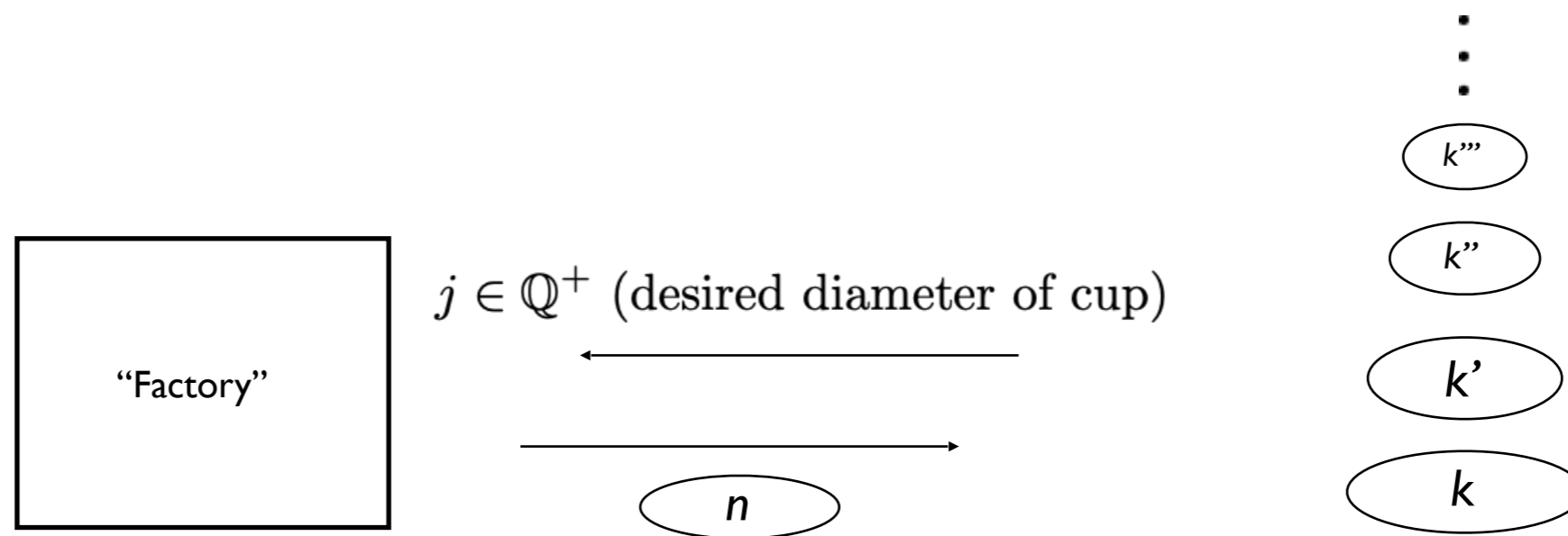
Suppose you have at your disposal a “factory” that, upon hearing you announce a number j , can quickly output a cup having a diameter of precisely j units. Can you insert a new cup between two of the seriated, stacked cups in the tower shown here? — where the j you send in *must* be a positive integer, m is likewise a positive integer, and every cup in every tower must be more in diameter than the one immediately above it, and less in diameter than the one immediately below it? ** Prove that your answer is correct.



**E.g., if $m = 3$, the tower in that case will have a base cup 4 units in diameter, immediately above that a cup 3 units in diameter, then a cup 2 units in diameter, and then finally a top cup of 1 unit in diameter.

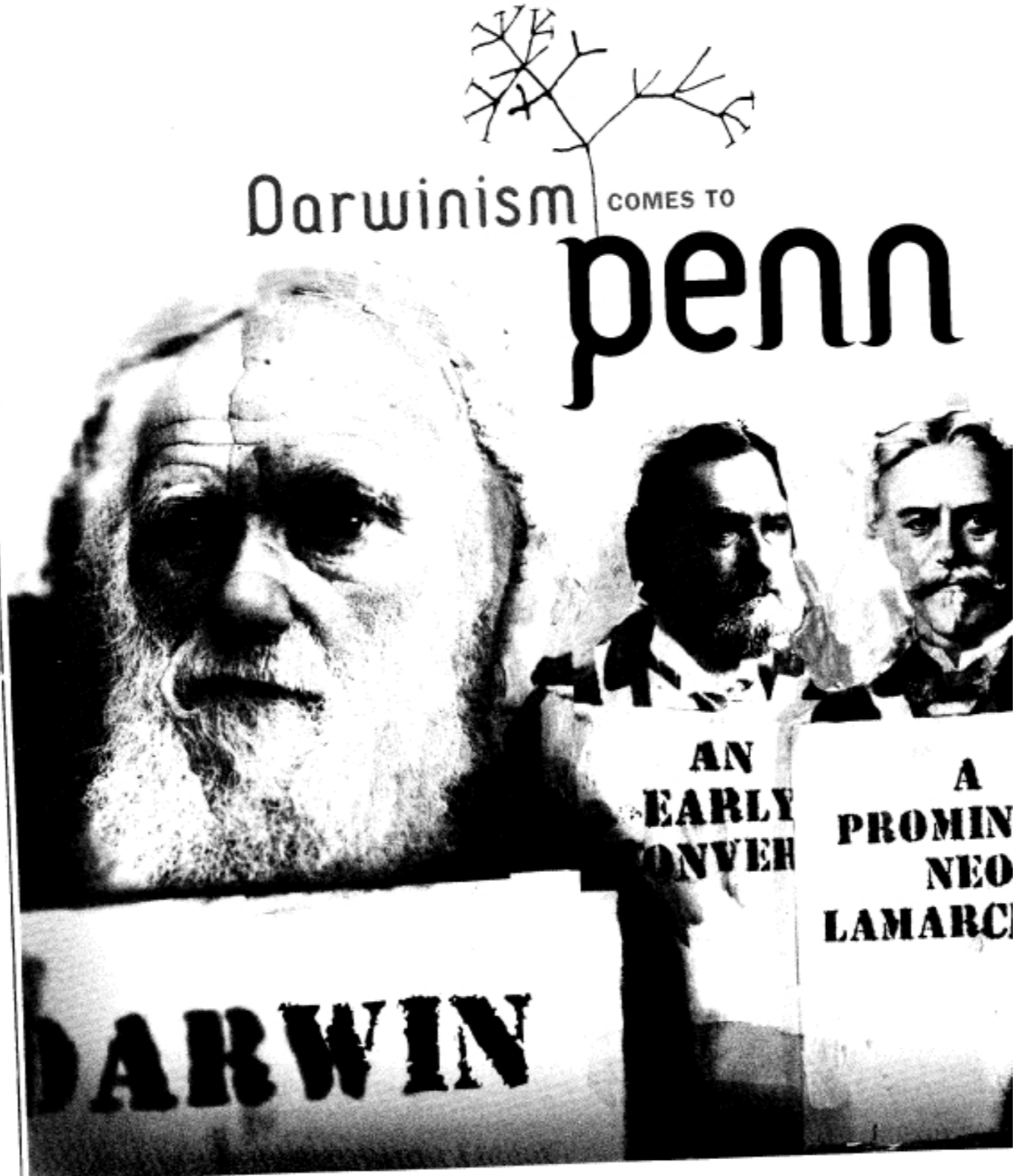
Selmer's Seriated Cup Challenge #2

Suppose you have at your disposal a “factory” that, upon hearing you announce a number j , can quickly output a cup having a diameter of precisely j units. Can you insert a new cup between two of the seriated, stacked cups in the tower shown here? — where the j you send in *must* be a positive rational number; $k, k', k'', k''' \dots$ are likewise positive rational numbers, and every cup in every tower must be more in diameter than the one immediately above it, and less in diameter than the one immediately below it? ** Prove that your answer is correct.



**E.g., if $k = \frac{1}{2}$, the tower in that case will have a base cup $\frac{1}{2}$ units in diameter, immediately above that there could be a cup $\frac{1}{3}$ units in diameter, then perhaps a cup $\frac{1}{4}$ units in diameter, and then perhaps finally a top cup of $\frac{1}{32}$ units in diameter.

Check your history books ...



From my alma mater: *Pennsylvania Gazette* Nov/Dec 2009

A century-and-a-half after the November 1859 publication of *On the Origin of Species*, a Penn microbiologist looks back at how Darwin's ideas were received by some of the University's leading thinkers. **BY HOWARD GOLDFINE**

ON June 18, 1858, Charles Darwin received a manuscript from Alfred Russel Wallace, which outlined a theory of evolution based on natural selection. Wallace's letter came from an island in the Malay Archipelago, where he was collecting field specimens and studying the distribution of species. Wallace, like Darwin, invoked the Malthusian concept that a struggle for existence within rapidly expanding populations would be the driving force for selection of natural variants within a species. Darwin's immediate reaction was one of dismay. He had been working on his "big book on species" since his five-year voyage on the *Beagle* (1831-36) and a relatively unknown naturalist had forestalled

him. Darwin wrote to Charles Lyell, "If Wallace had my [manuscript] sketch written out in 1842, he could not have written out a better short abstract!"

Fortunately, Darwin had previously outlined his theory to his friends, the distinguished geologist Lyell and the botanist Joseph D. Hooker, and in a brief, unpublished draft to Asa Gray, a botanist at Harvard. Lyell and Hooker immediately arranged for Wallace's paper and a brief summary of Darwin's theory to be read simultaneously at the Linnaean Society in London on July 1, 1858. These were received with little comment. The president of the society later noted that nothing of great interest had happened that year.

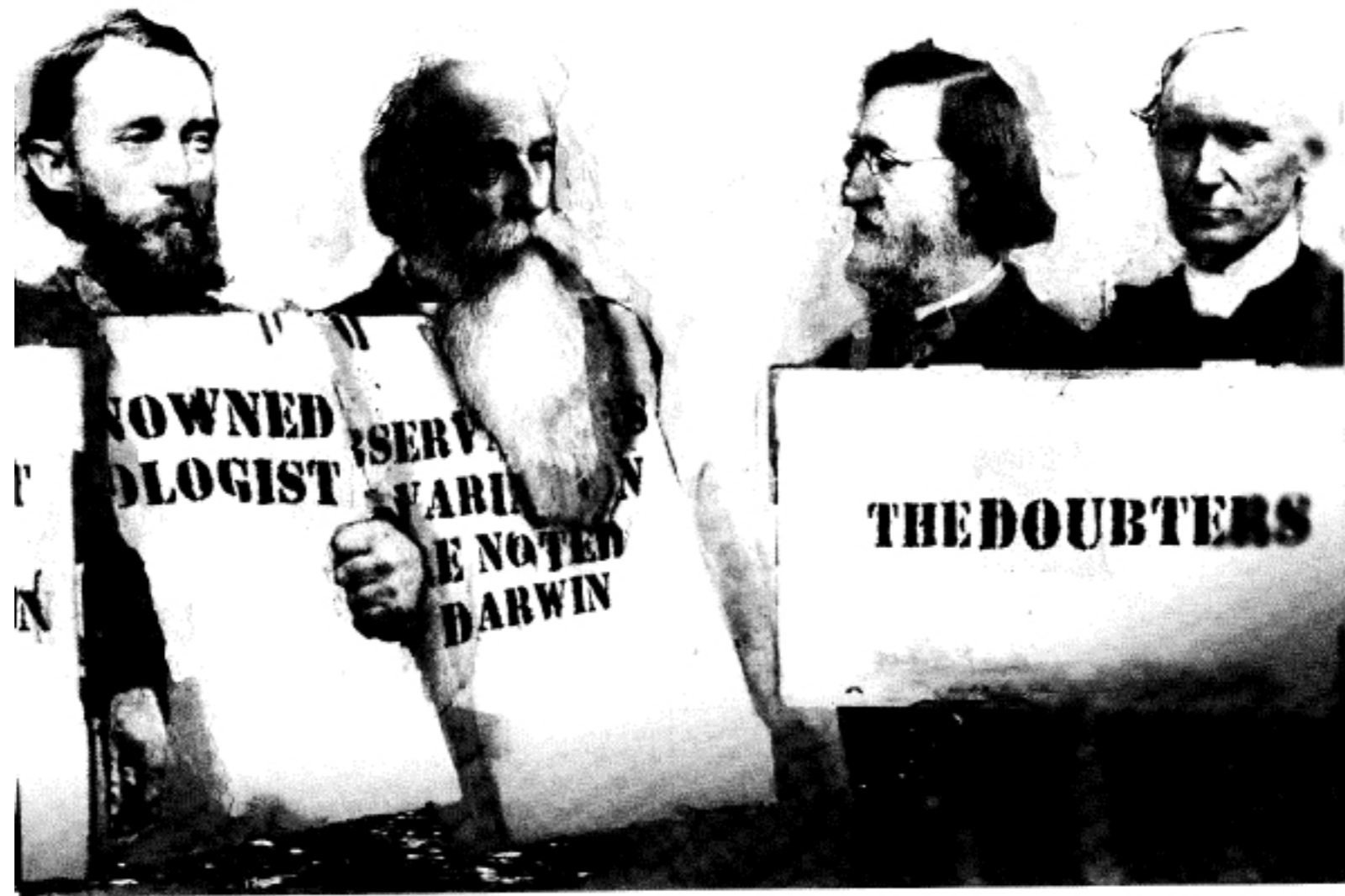


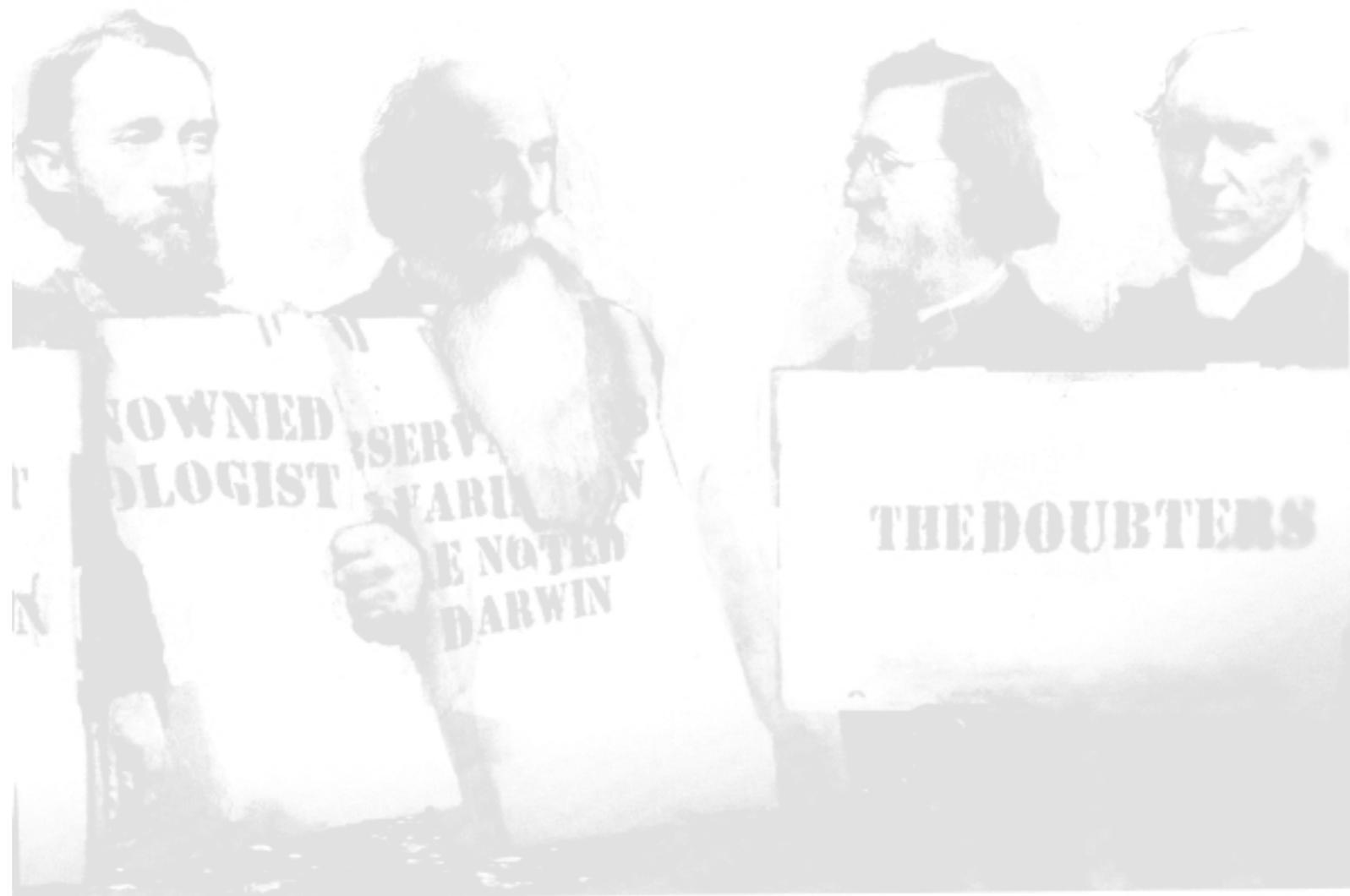
ILLUSTRATION BY DAVID HOLLENBACH THE PENNSYLVANIA GAZETTE NOV | DEC 2009 39

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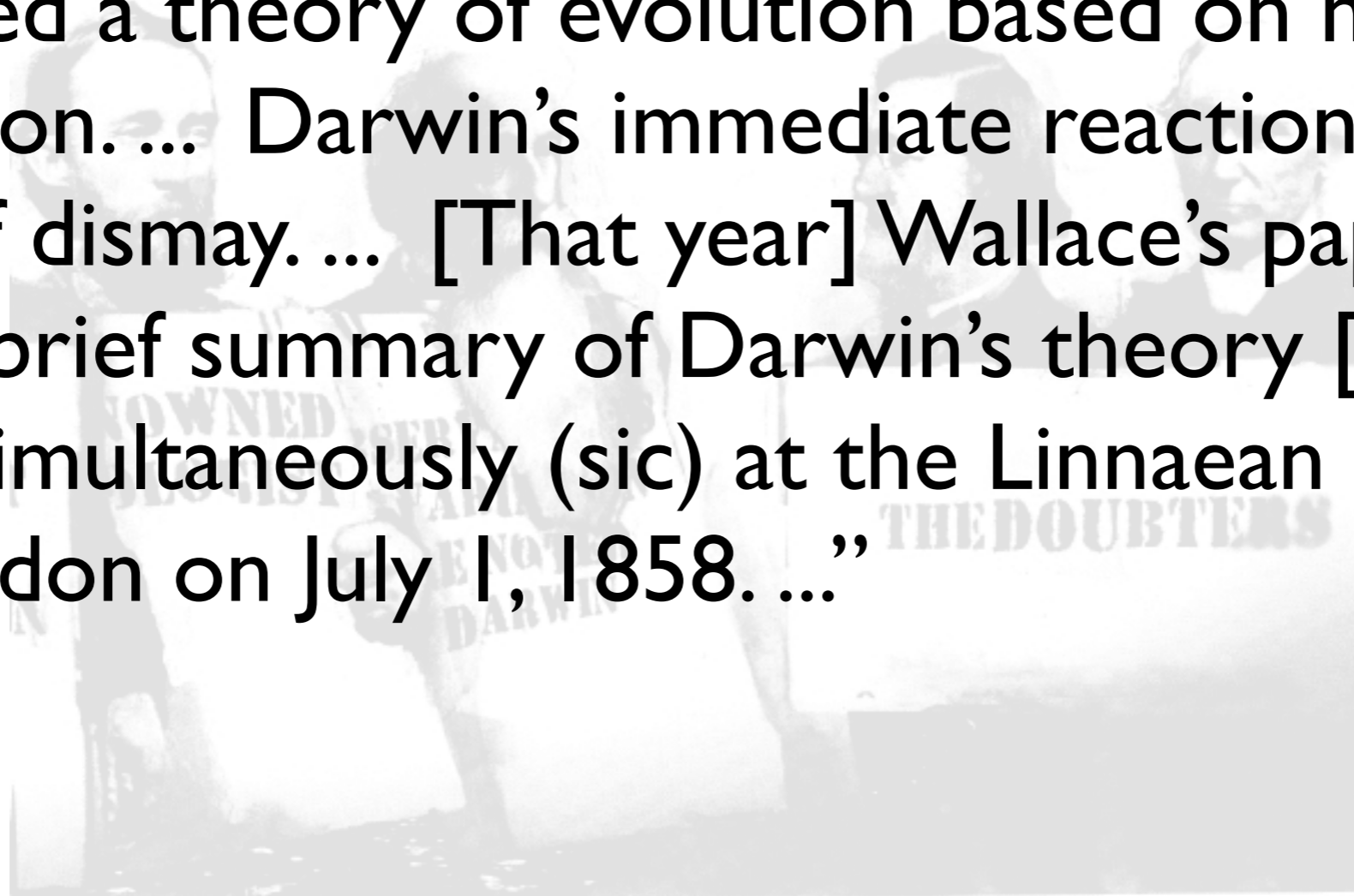
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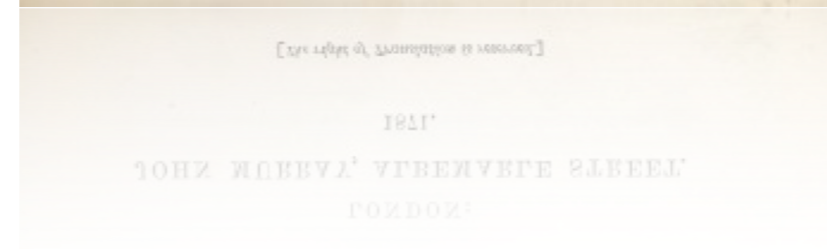
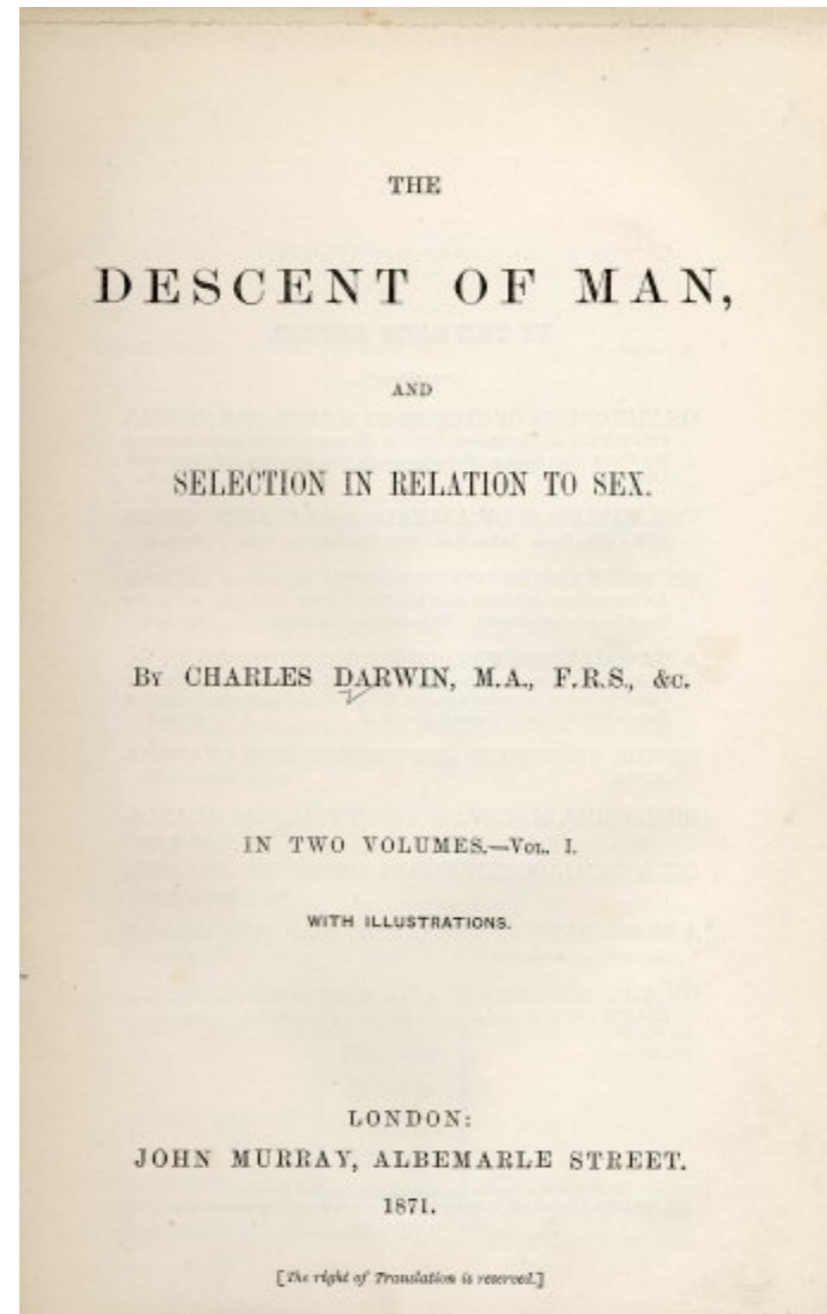
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Wallace seems to me to be right; Darwin to be wrong...

The book that shook the world, and supposedly obliterated the stupid notion that human persons are made in (in Milton's unpacked version of the phrase) God's image.



Praise for Darwin & *DoM*

Back cover of my Amazon.com version of *DoM*:
“Darwin’s engaging literary style, charming modesty, brilliant argument, and discursive method of proof makes the book an exhilarating romp through Earth’s natural history and Man’s history ...”

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Really?

I found no brilliant arguments, and not a single proof.

A Key Proposition

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\bar{A}

There is at least one mental power possessed by human persons, but not by any mere animal; and the mental powers of human persons are of a wholly different nature than those of mere animals.

Efficient Refutation of Darwin's *DoM*

∴	(1) If human persons are the product of evolution, then it's not the case that \bar{A} holds.	
	(2) \bar{A} does hold.	
	(3) Human persons are not the product of evolution.	from (1), (2) by <i>modus tollens</i>

QED

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\therefore	(1) If human persons are the product of evolution, then it's not the case that \bar{A} holds.	
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Note: (3) doesn't deductively entail that *no* parts of human personhood are the product of evolution. In other words, (3) can be rephrased as: "Human persons are not solely and completely the product of evolution." As seen shortly, the power of human persons to carry out abstract, infinitary reasoning (as in the case of developing the tensor calculus) would be — according to Wallace & Bringsjord — something that evolution didn't produce.

Whence comes the first premise in this argument?

From Darwin Himself

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“If no organic being excepting man had possessed any mental power, or if his powers had been of a wholly different nature from those of the lower animals, then we should never have been able to convince ourselves that our high faculties had been gradually developed.”

(Descent of Man, Part One, Chapter Two)

The Argument

	(1)	Hunter-gatherers possessed the cognitive power P^∞ to e.g. invent the calculus and create literary art of the caliber of Blecher/Proust/Ibsen/....	undisputed
	(2)	AI shows us that these early versions of us, to hunt and gather, needed only humble cognitive power P^{HG} , where $P^{\text{HG}} < P^\infty$, because $P^{\text{AI}} \approx P^{\text{HG}}$ and, where P^{AI} is a limit on the cognitive power of AI, AIs can hunt and gather.	see AI today
\therefore	(3)	We have $(P^\infty - P^{\text{HG}})$.	abstraction (1), (2)
	(4)	Our having $(P^\infty - P^{\text{HG}})$, <i>contra</i> Darwin, is inexplicable by gradual mutation and natural selection (i.e. P^∞ is discontinuous from P^{HG}).	see critique of <i>DoM</i> see theorem/proof
	(5)	If our having $(P^\infty - P^{\text{HG}})$ is explicable, then $E_1 \vee E_2 \vee \text{God exists}$.	sub-arg
	(6)	Our having $(P^\infty - P)$ is explicable.	undeniable
	(7)	$\neg E_1 \wedge \neg E_2$	sub-argument
\therefore	(8)	God exists.	<i>modus ponens</i> (5), (6), (7)

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