

First-Order Logic = FOL = \mathcal{L}_1 , Part 2

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Intro to Logic-based AI
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Logic-&-AI In The News

Ambulance Chasing and AI

Wouldn't the wiser, more humane course be to regulate before a catastrophe?



The language program developed by OpenAI uses artificial intelligence to write a random binary code, Aug. 7. (PHOTO: FRANK RUMPENHORST/ZUMA PRESS)

Oct 02, 2024 10:40 a.m. ET



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Under Ketan Ramakrishnan's preferred means of regulating artificial intelligence ("[Tort Law Is the Best Way to Regulate AI](#)," op-ed, Sept. 25), "bioterrorist attacks or other grievous harm" are prerequisites to action. As he concedes, tort law purports to compensate the damaged after the damage has already occurred.

Sadly, the only ones truly compensated are the tort lawyers. Wouldn't the wiser, more humane course be to regulate before a catastrophe? If he

knows, as he claims, that a company has already "released a powerful new artificial-intelligence model this month that modestly but meaningfully increases the risk of catastrophic bioterrorism," why wait for catastrophe? That's rather coldblooded, as if one is after the contingency fee.

Christopher C. Spencer

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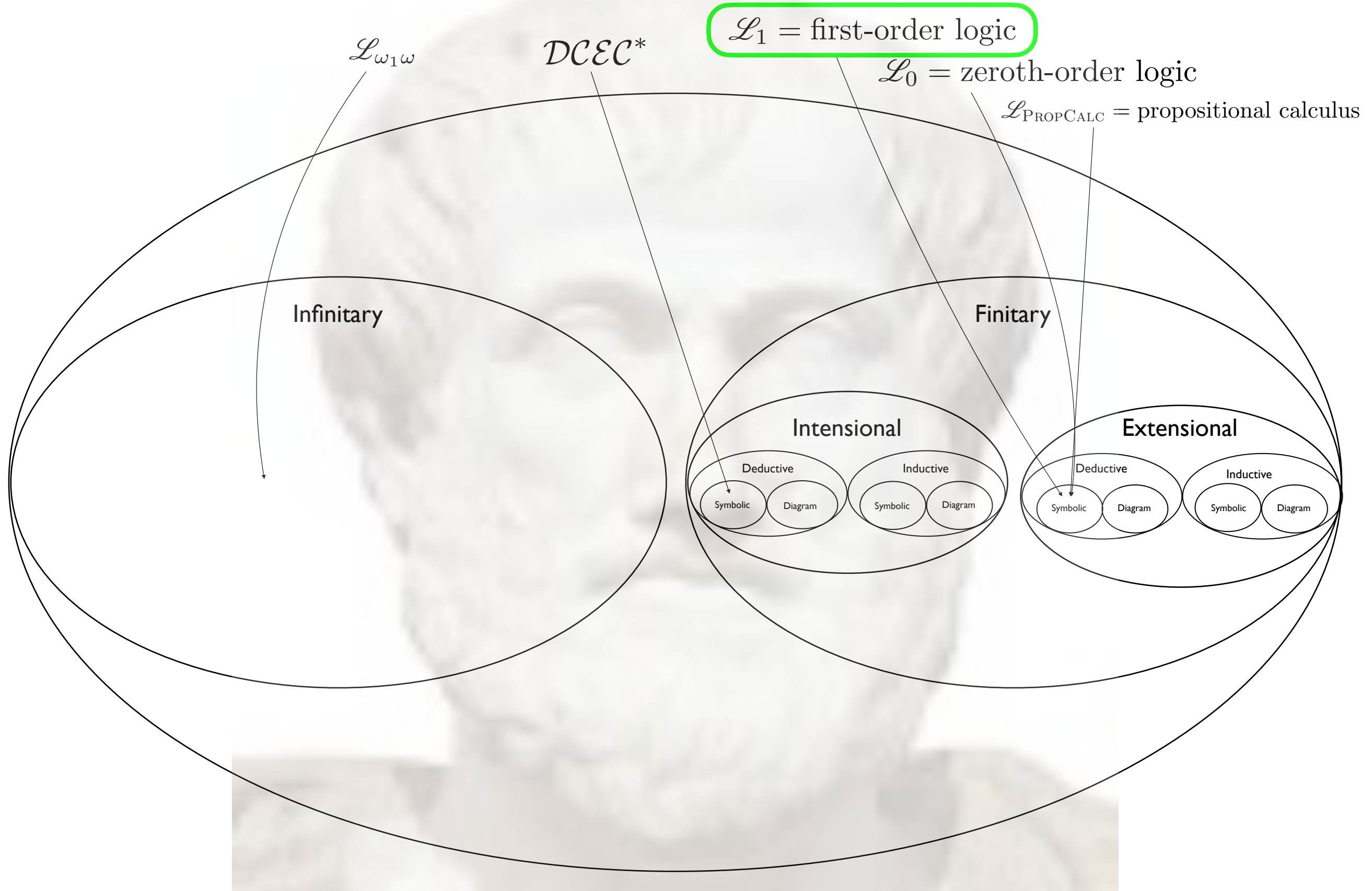
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You're right! We'll get to the engineering into AI's ethical/legal control later in the course.

The Universe of Logics



Let's dive in, discuss,
win some trophies, and
learn ...

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learn ...

(First, two Required
prop-calc problems;
then DFT fun ...)

Next New (*Not-So-Easy!*) Inference Rule in FOL

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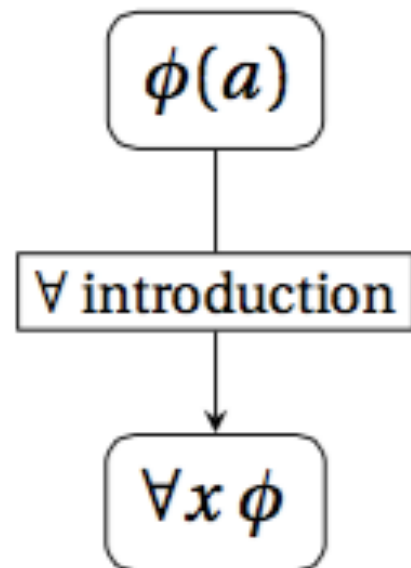
- universal introduction

Next New (*Not-So-Easy!*) Inference Rule in FOL

- universal introduction
 - If something a is an R , and the constant/name a is *genuinely arbitrary*, then we can deduce that everything is an R .

The Inference Schema

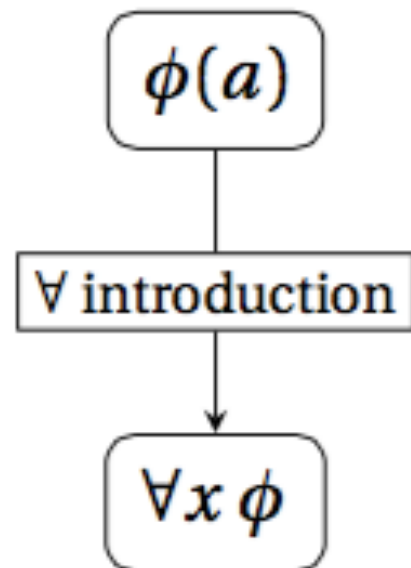
The Inference Schema



provided that a does not appear free in any in-scope assumption of ϕ , and that no occurrence of a appear in the inferred $\forall x \phi$

(3.16)

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(Why the provisos?)

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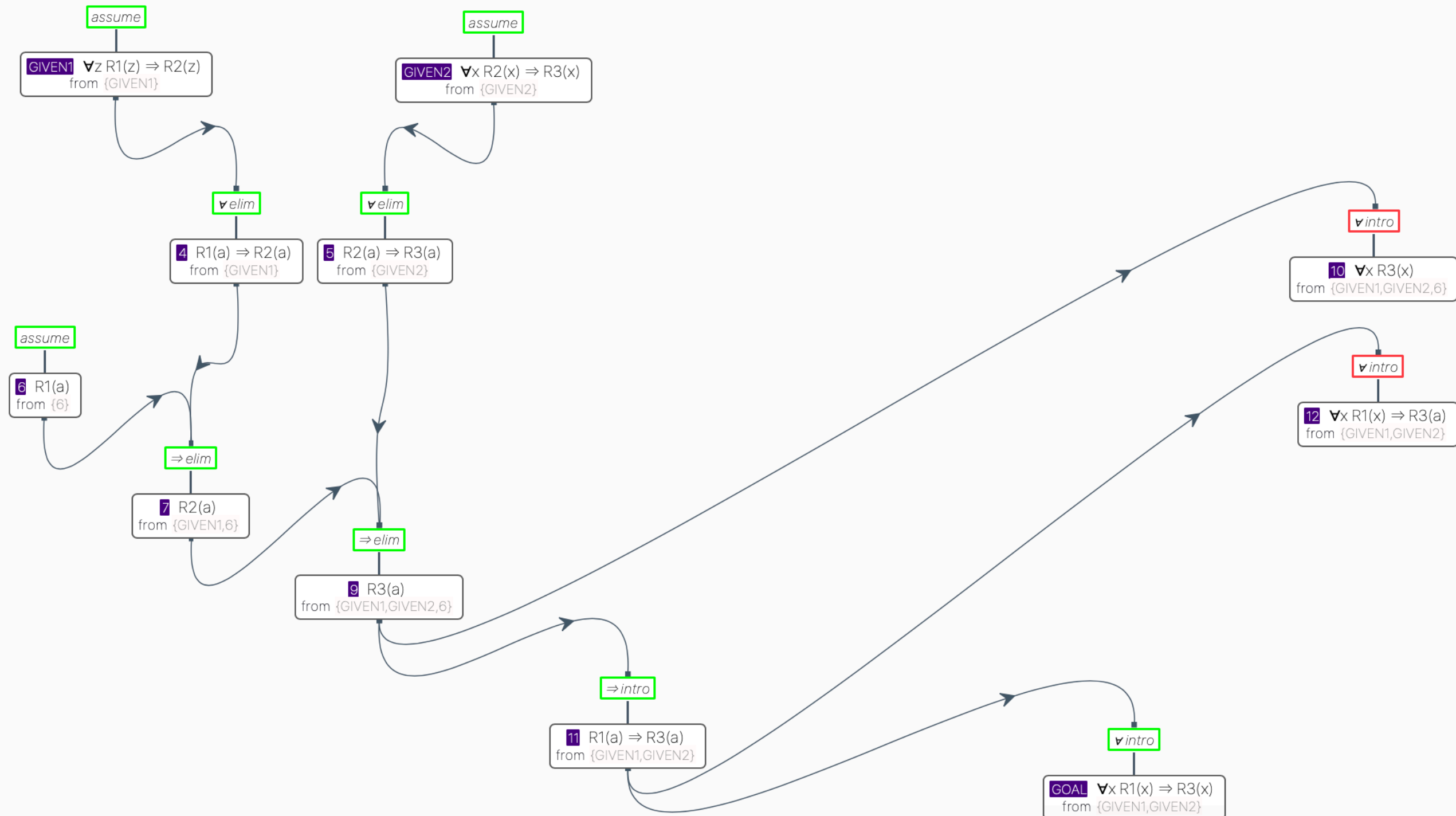
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UniversalIntroPractice [FIRST-ORDER-LOGIC]: Saved with 53 symbols.



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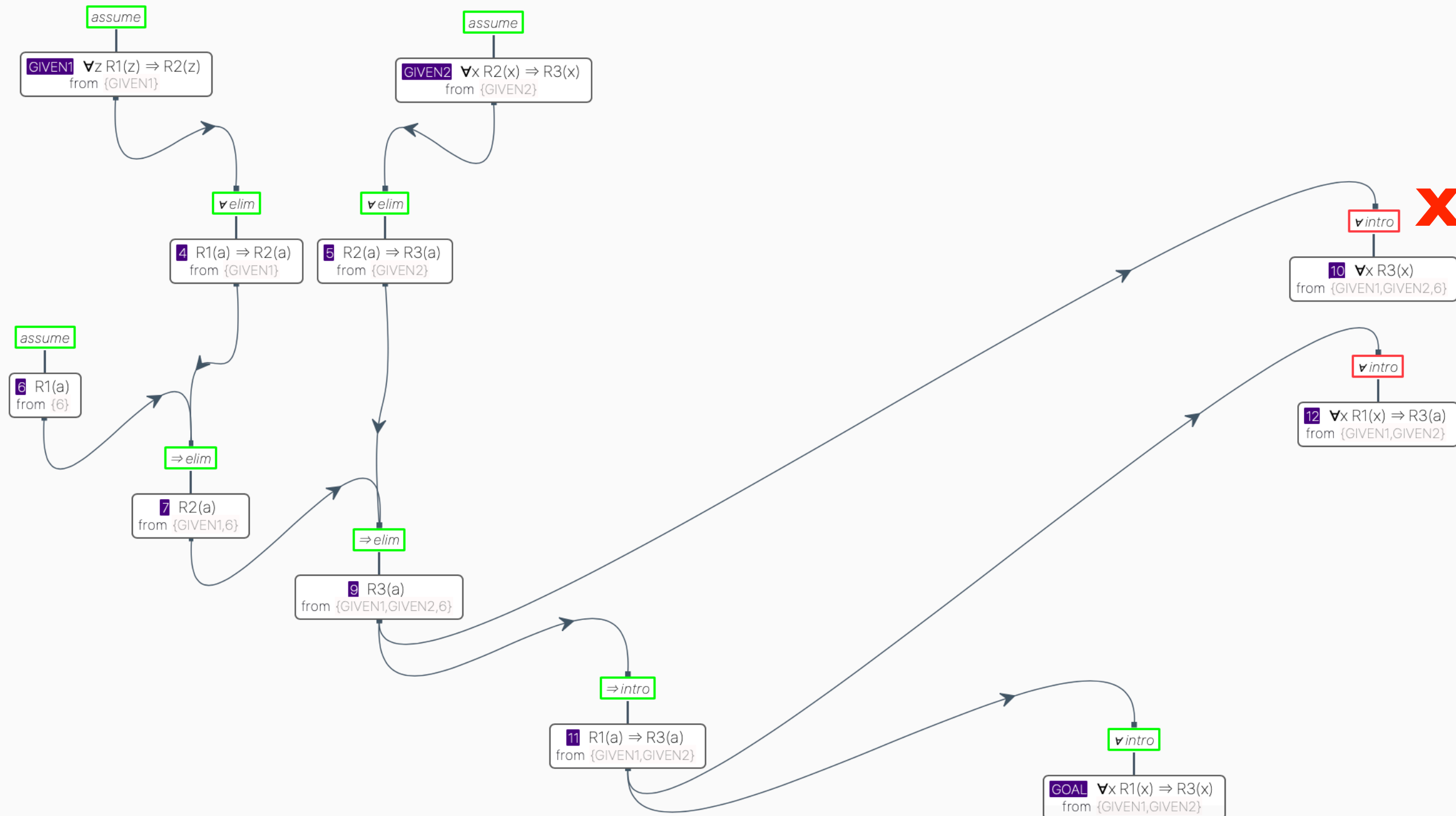
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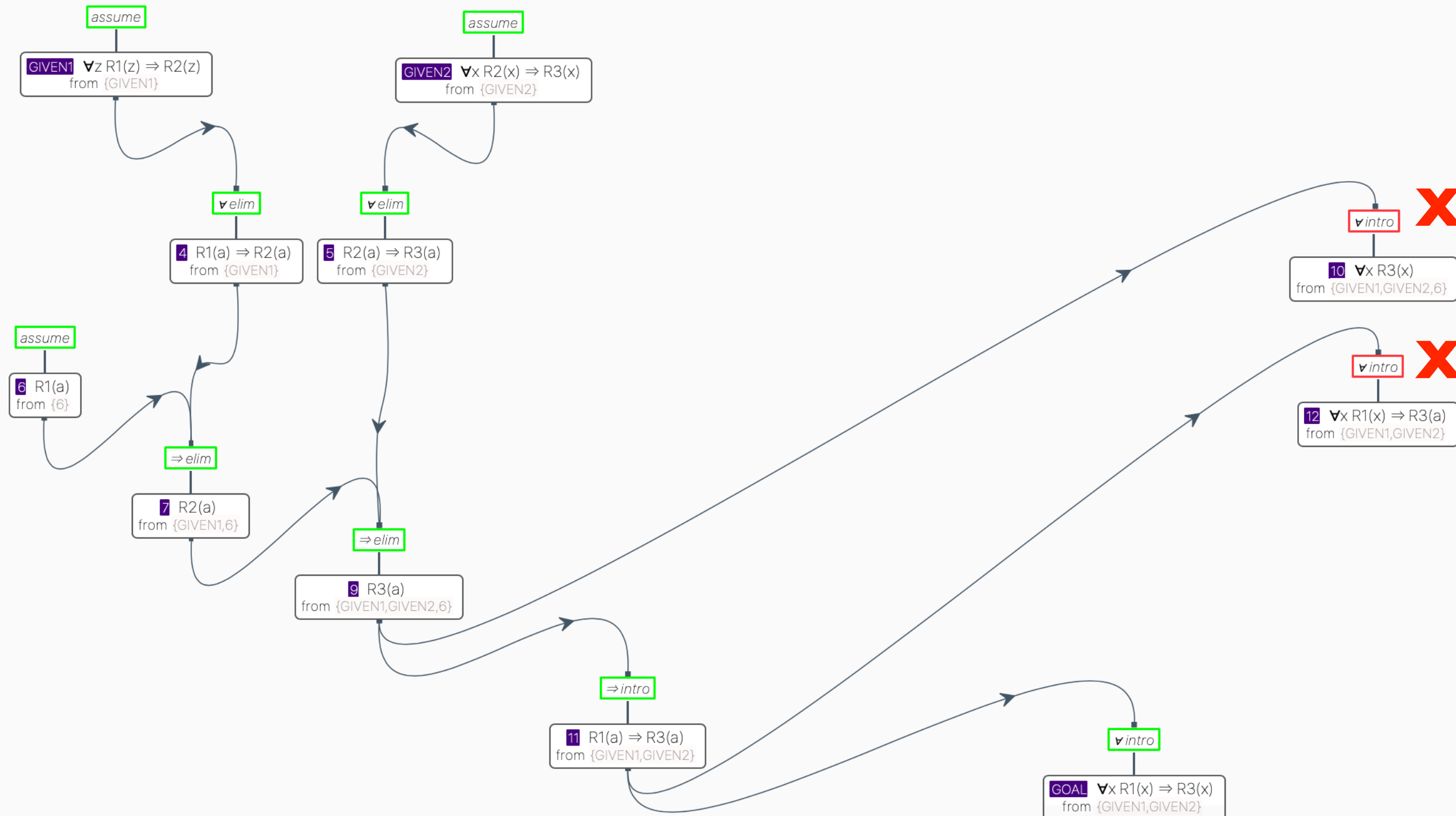
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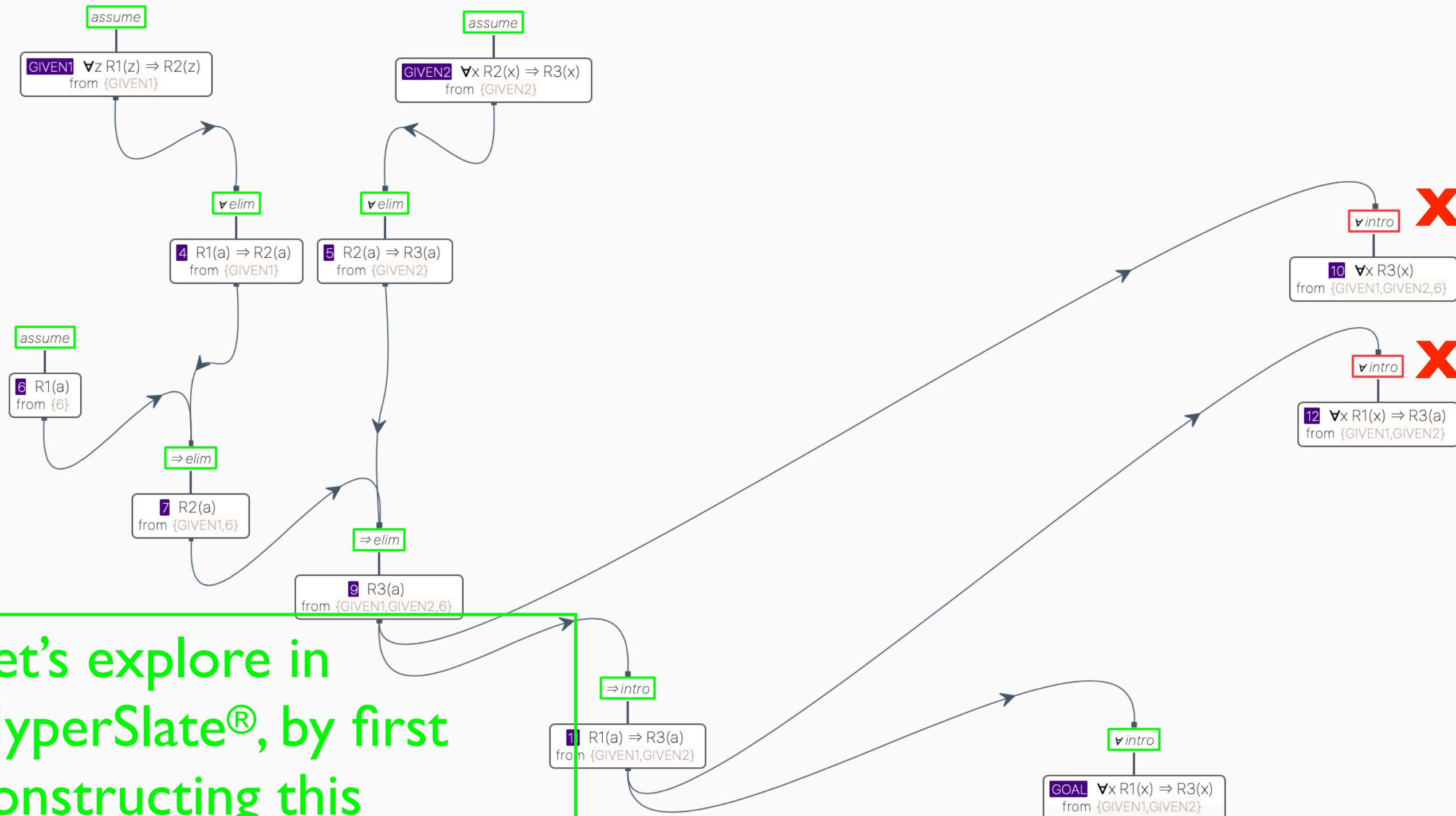
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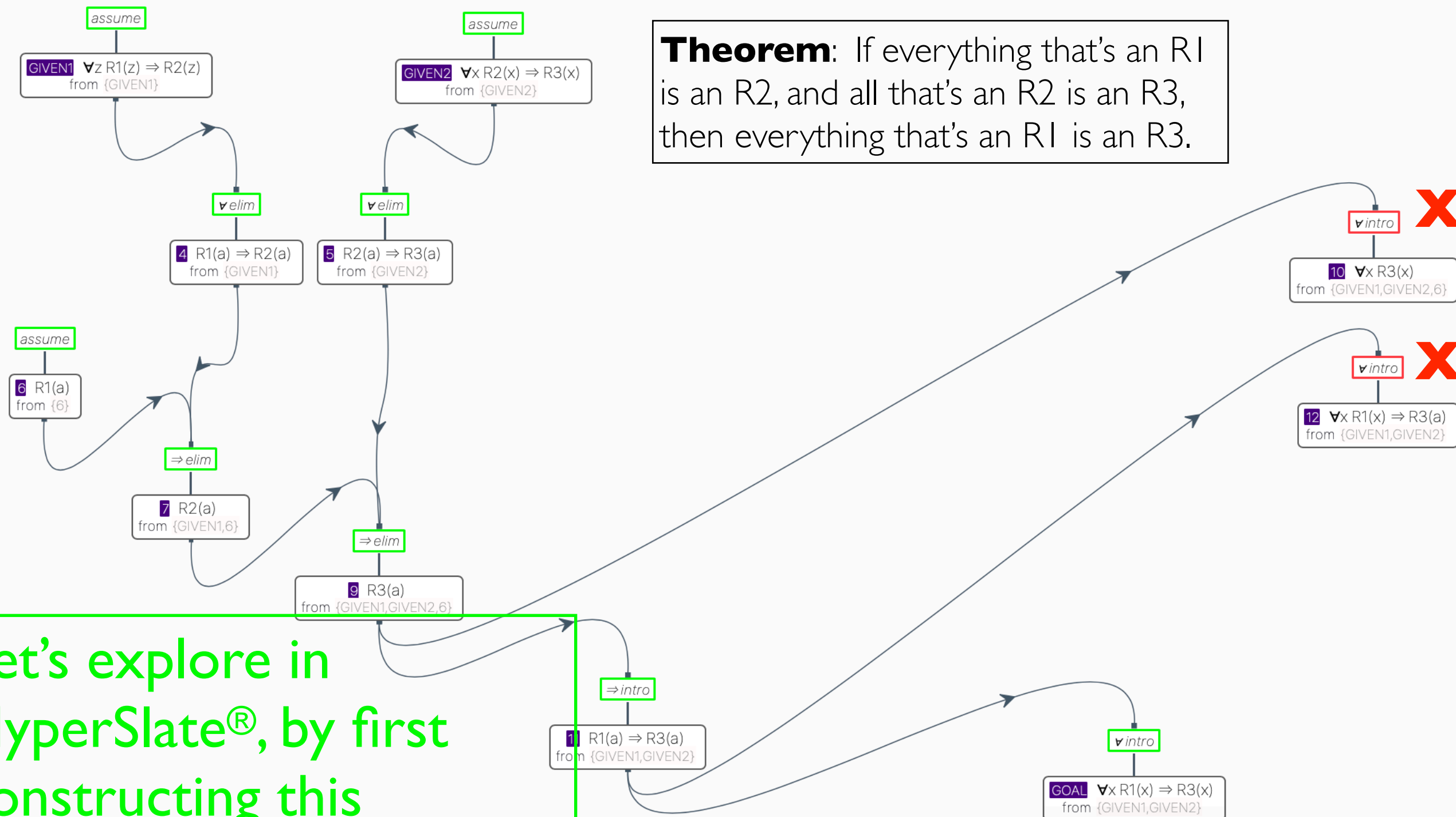
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UniversalIntroPractice [FIRST-ORDER-LOGIC]:

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Theorem: If everything that's an R1 is an R2, and all that's an R2 is an R3, then everything that's an R1 is an R3.



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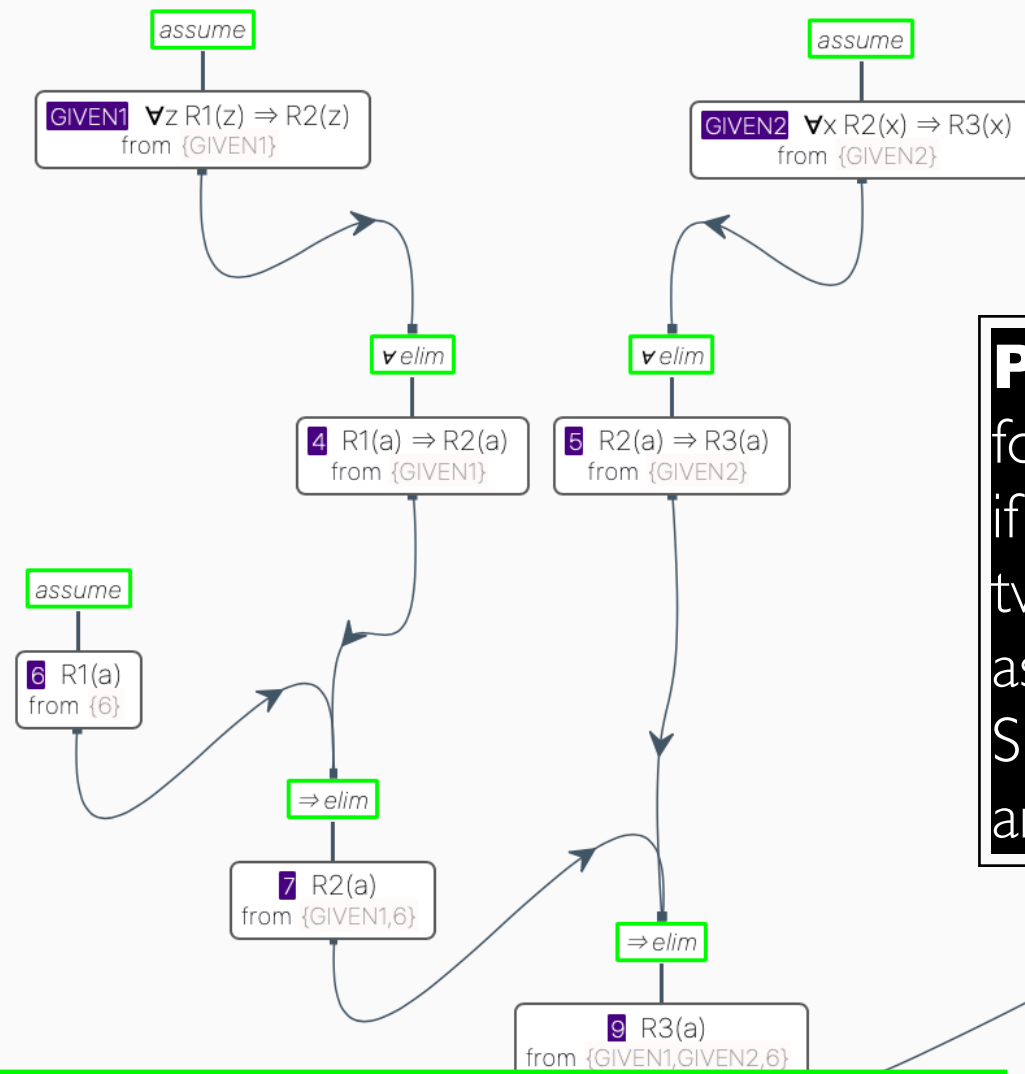


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UniversalIntroPractice [FIRST-ORDER-LOGIC]:

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Theorem: If everything that's an R1 is an R2, and all that's an R2 is an R3, then everything that's an R1 is an R3.

Proof: It follows from the hypothesis that for arbitrary a , both if $R1(a)$ then $R2(a)$, and if $R2(a)$ then $R3(a)$. But we can chain these two conditionals (by hypothetical syllogism, as it's known) to deduce if $R1(a)$ then $R3(a)$. Since a here is arbitrary, we know that, for anything at all, if it's an R1 it's also an R3. \blacksquare



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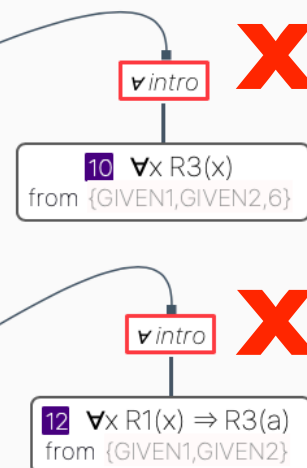
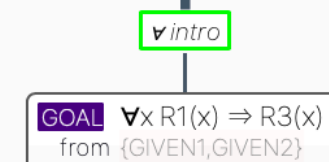
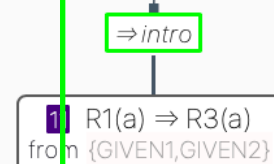
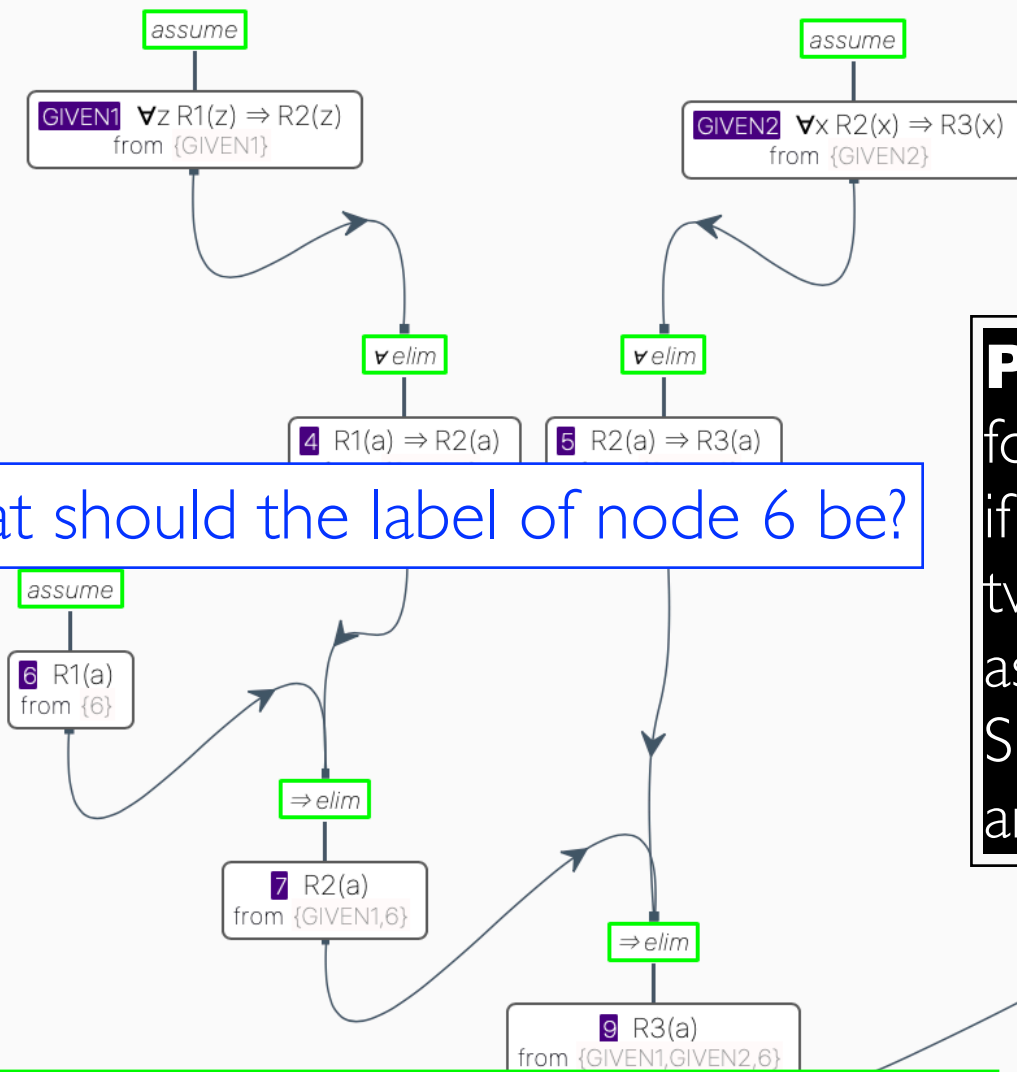
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What should the label of node 6 be?

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*Hvis du forstår det, kan
du bevise det.*