

First-Order Logic = FOL = $\mathcal{L}_1$, Part 2

Selmer Bringsjord

Rensselaer AI & Reasoning (RAIR) Lab
Department of Cognitive Science
Department of Computer Science
Lally School of Management & Technology
Rensselaer Polytechnic Institute (RPI)
Troy, New York 12180 USA

Intro to Logic-based AI
10/6/2025



Logic-&-AI In The News (2024)

Ambulance Chasing and AI

Wouldn't the wiser, more humane course be to regulate before a catastrophe?



The language program developed by OpenAI uses artificial intelligence to write a random binary code, Aug. 7. (PHOTO: FRANK RUMPENHORST/ZUMA PRESS)

Oct 02, 2024 10:40 a.m. ET



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Under Ketan Ramakrishnan's preferred means of regulating artificial intelligence ("[Tort Law Is the Best Way to Regulate AI](#)," op-ed, Sept. 25), "bioterrorist attacks or other grievous harm" are prerequisites to action. As he concedes, tort law purports to compensate the damaged after the damage has already occurred.

Sadly, the only ones truly compensated are the tort lawyers. Wouldn't the wiser, more humane course be to regulate before a catastrophe? If he

knows, as he claims, that a company has already "released a powerful new artificial-intelligence model this month that modestly but meaningfully increases the risk of catastrophic bioterrorism," why wait for catastrophe? That's rather coldblooded, as if one is after the contingency fee.

Christopher C. Spencer

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You're right! We'll get to the engineering into AI's ethical/legal control later in the course.

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The five-year agreement will challenge Nvidia's market dominance, as OpenAI plans to deploy AMD's new MI450 chips.

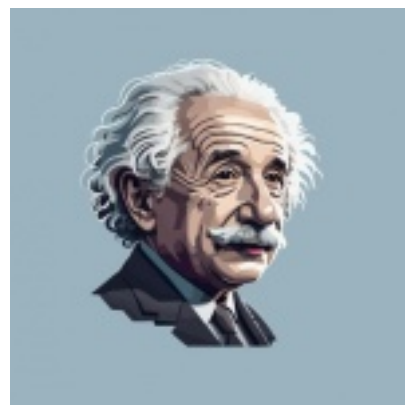
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xAI is aiming to win the tech arms race with its "Colossus" data centers, but Memphis is divided over its massive demand for power and water.

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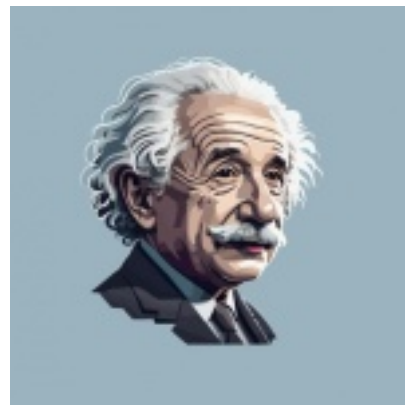
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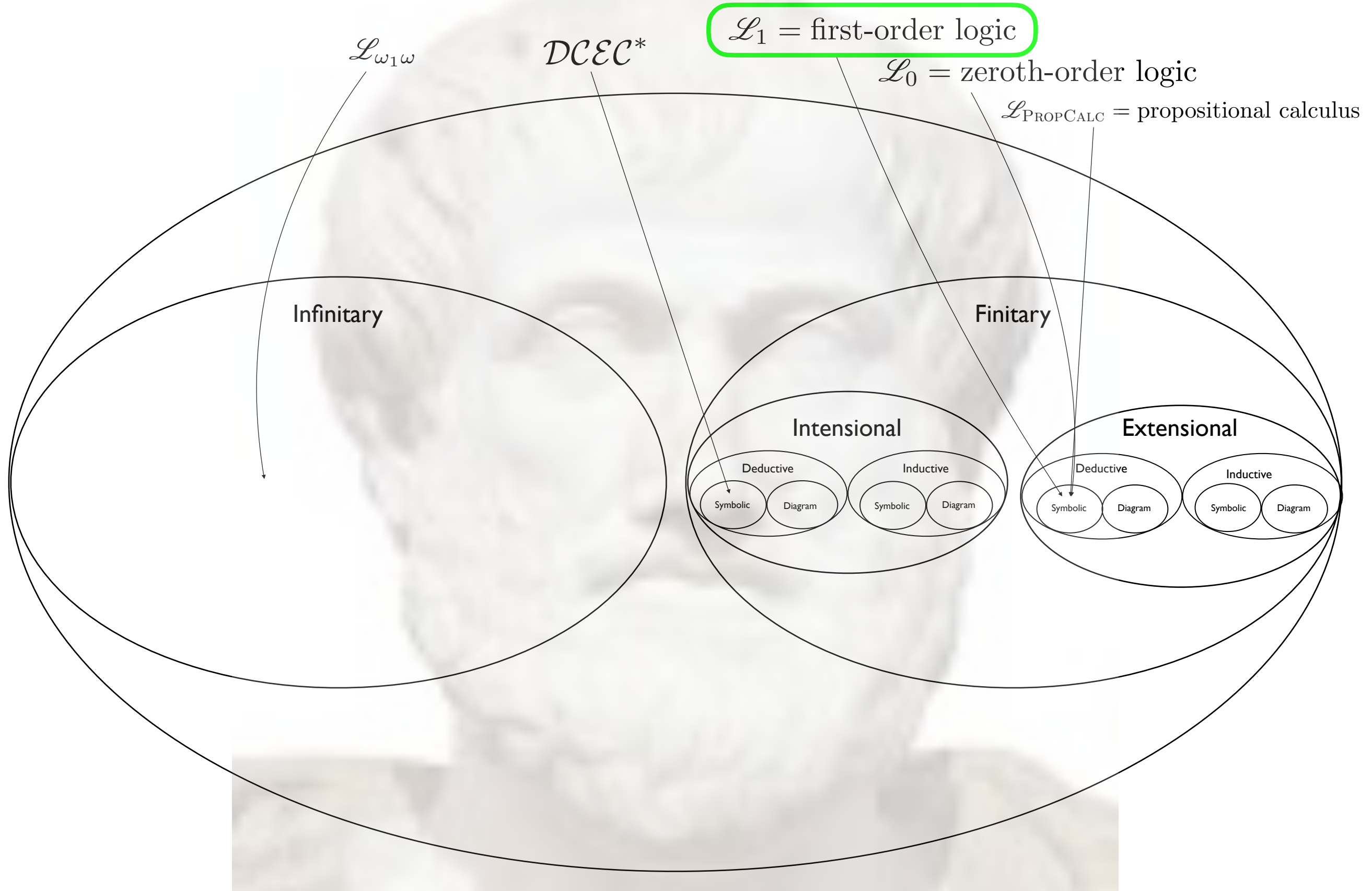
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The Universe of Logics



The AI-&-Aristotle Adventure Continues ...

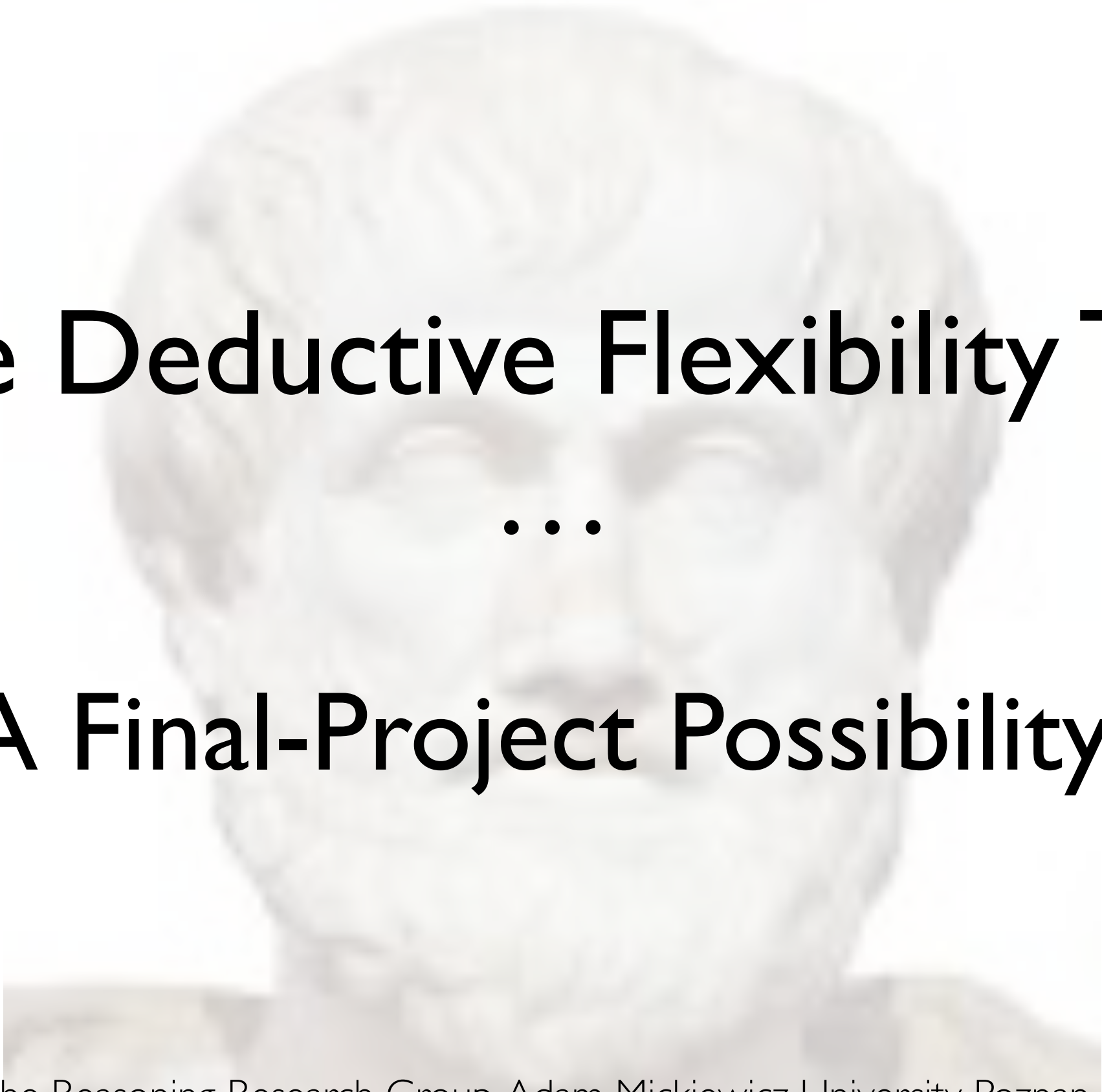
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Festino

The Deductive Flexibility Test

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From the Reasoning Research Group, Adam Mickiewicz University, Poznan, Poland
<http://murbansk-rrg.home.amu.edu.pl/research-projects/deductive-flexibility-test>



The Deductive Flexibility Test

...

(A Final-Project Possibility!)

From the Reasoning Research Group, Adam Mickiewicz University, Poznan, Poland
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Example with correct answer:

- (1) Some nedges are dwens.
- (2) Some strimes are dwens.
- (3) Every nedge is a strime.
- (4) Every nedge is a dwen.
- (5) This is not the case, that no dwen is a strime.
Some dwens are strimes.

Answer: (2); (5); (3 and 4); (1 and 4)

Correct? To HyperSlate® ...

- I (1) Every faub is a non-veece.
 (2) No phodd is a veece.
 (3) No veece is a phodd.
 (4) Every veece is a non-faub.
 (5) Every faub is a phodd.
 No faub is a veece.

Answer:_____

The *Not-So-Easy* Inference Rule in FOL

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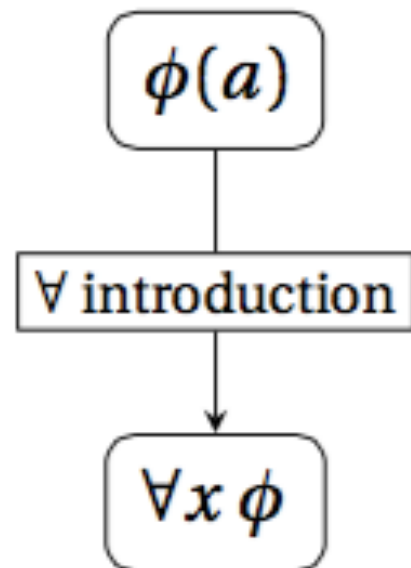
- universal introduction

The *Not-So-Easy* Inference Rule in FOL

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 - If something a is an R , and the constant/name a is *genuinely arbitrary*, then we can deduce that everything is an R .

The Inference Schema

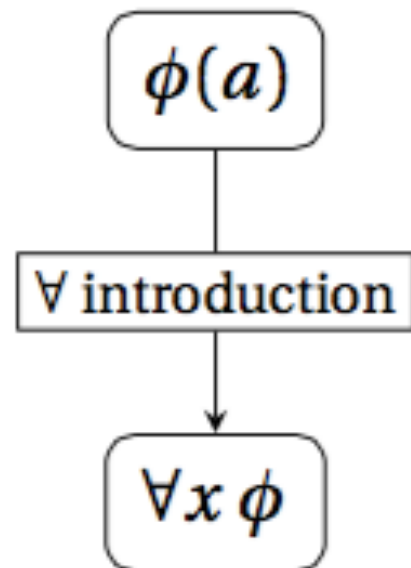
The Inference Schema



provided that a does not appear free in any in-scope assumption of ϕ , and that no occurrence of a appear in the inferred $\forall x \phi$

(3.16)

The Inference Schema



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(3.16)

(Why the provisos?)

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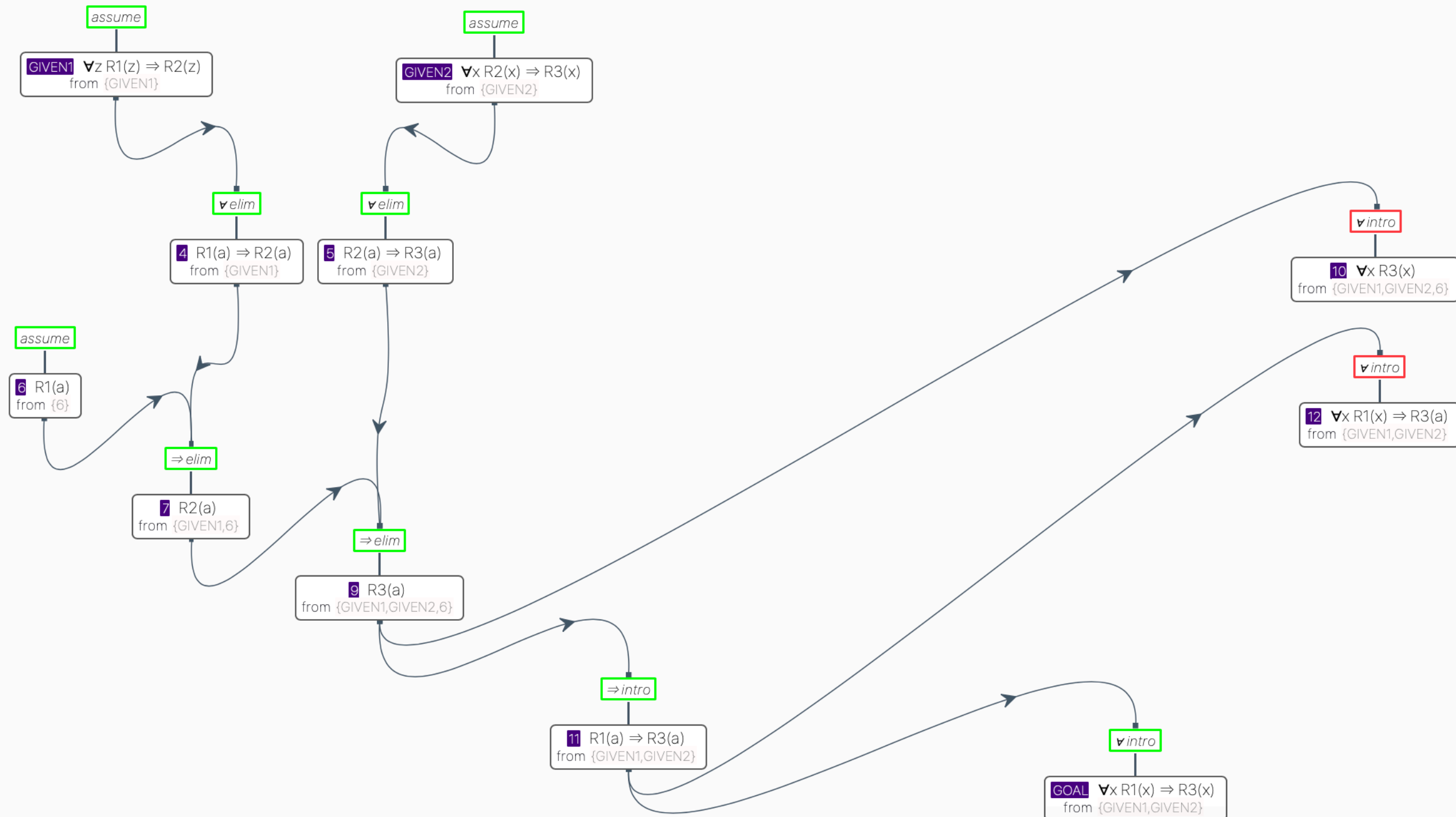
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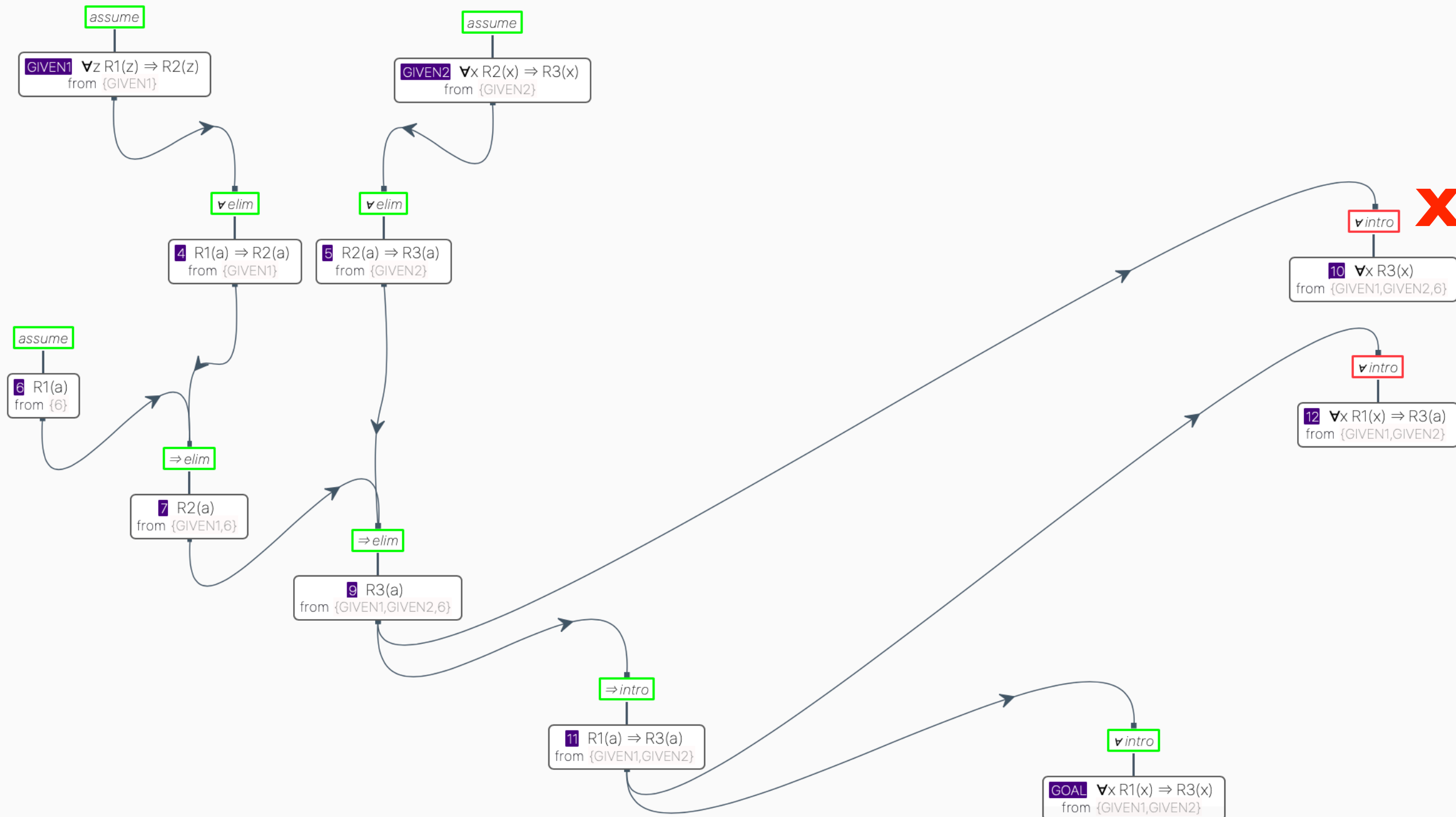
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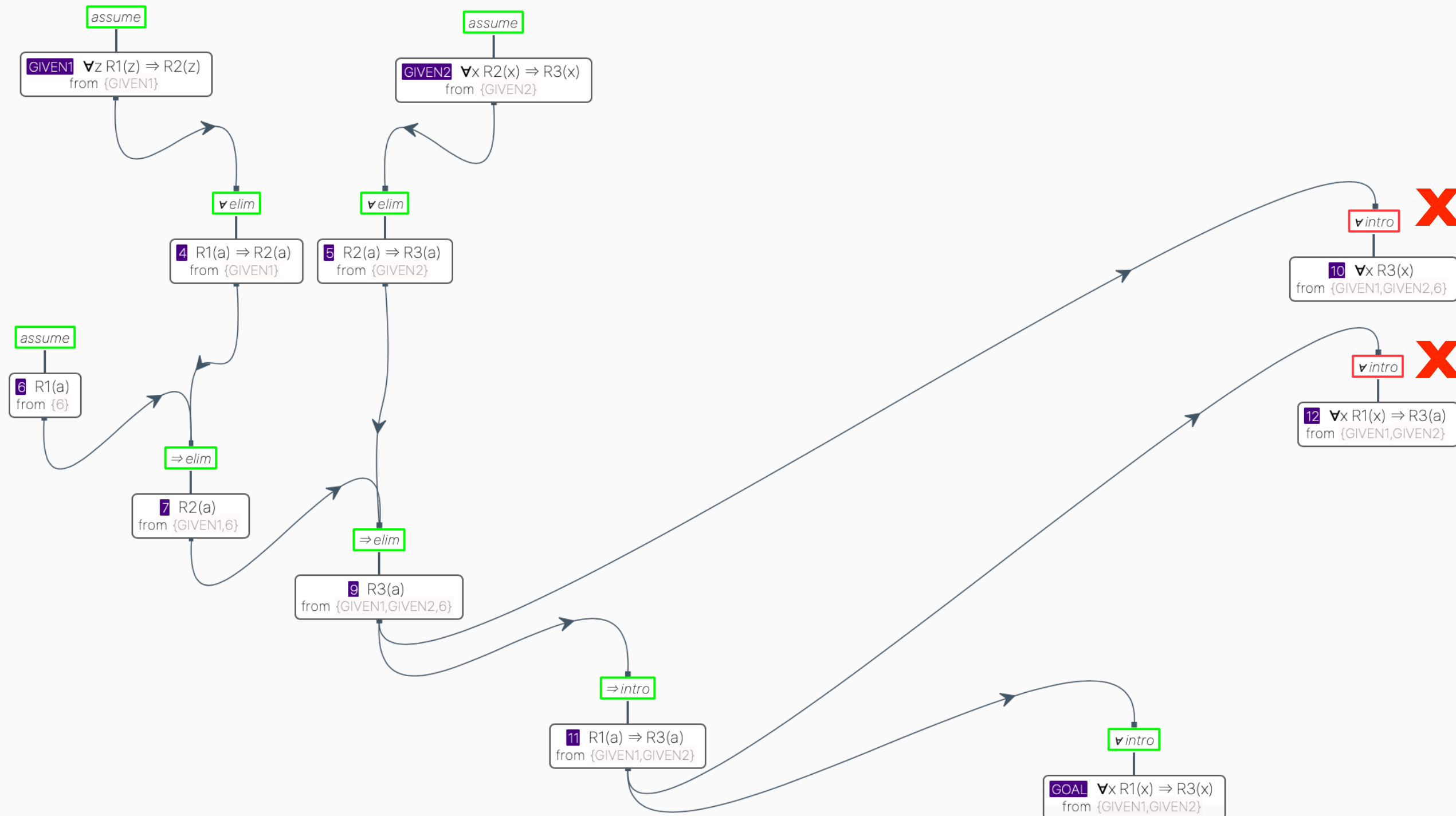
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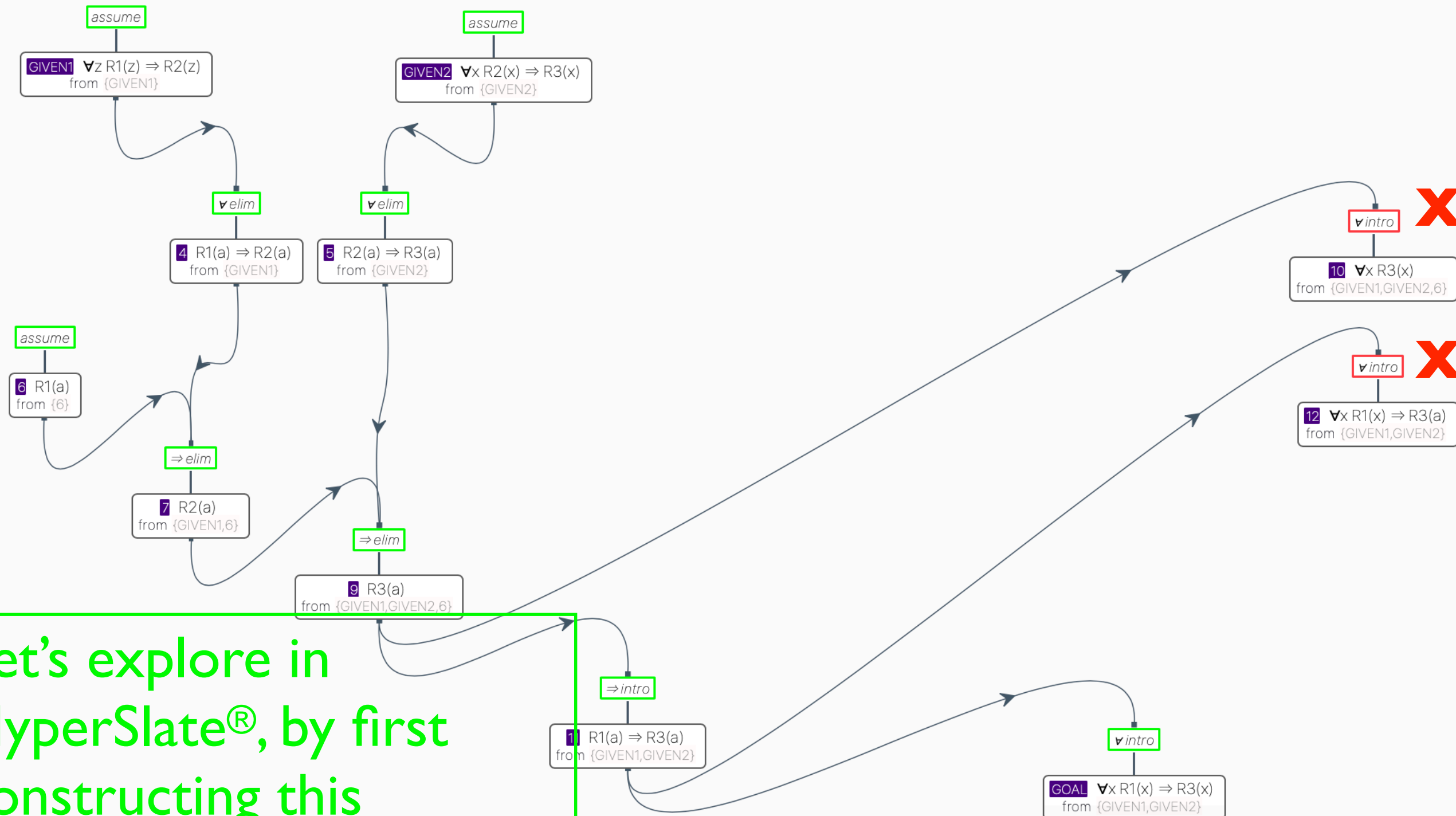
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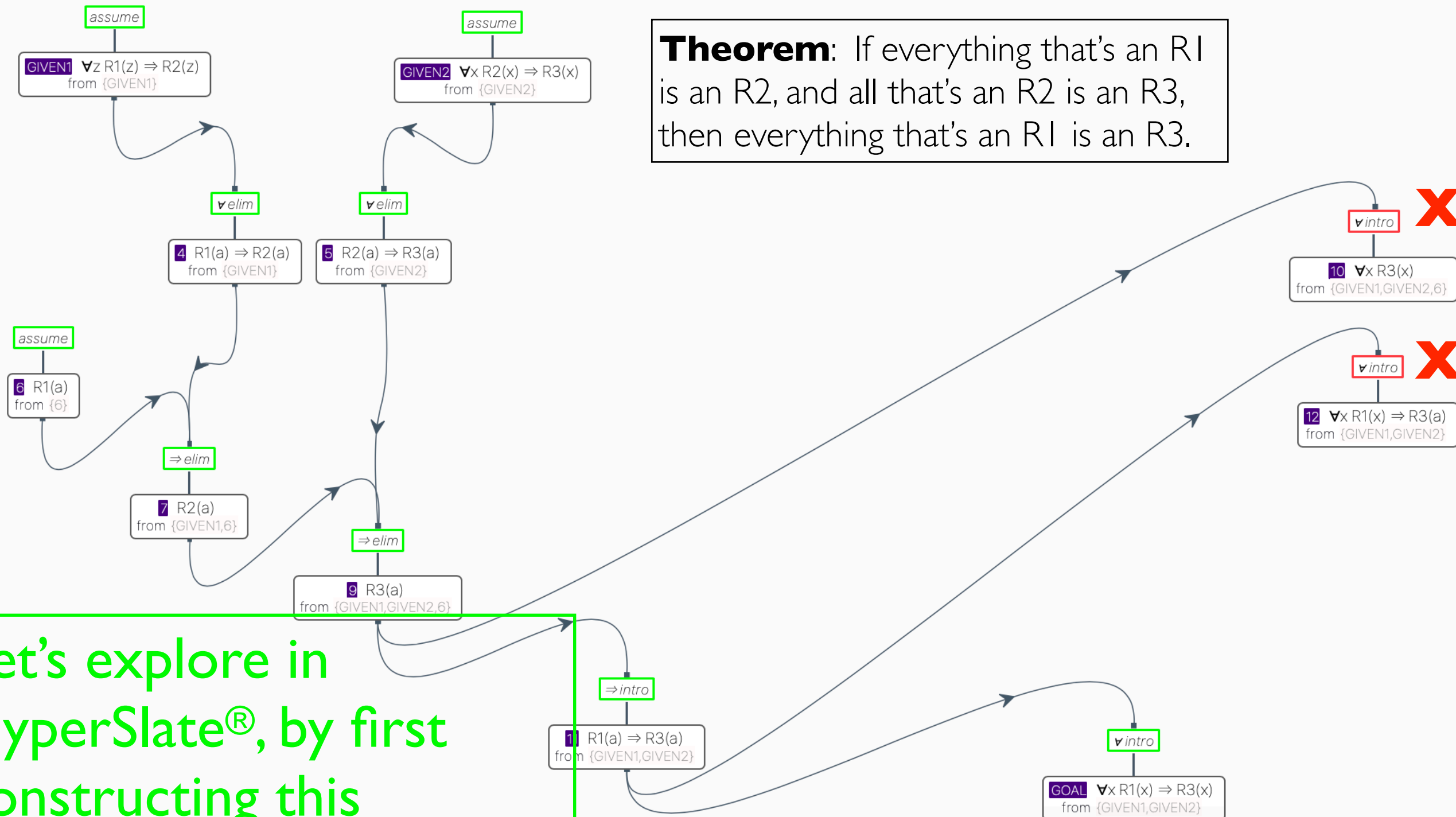


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Theorem: If everything that's an R1 is an R2, and all that's an R2 is an R3, then everything that's an R1 is an R3.



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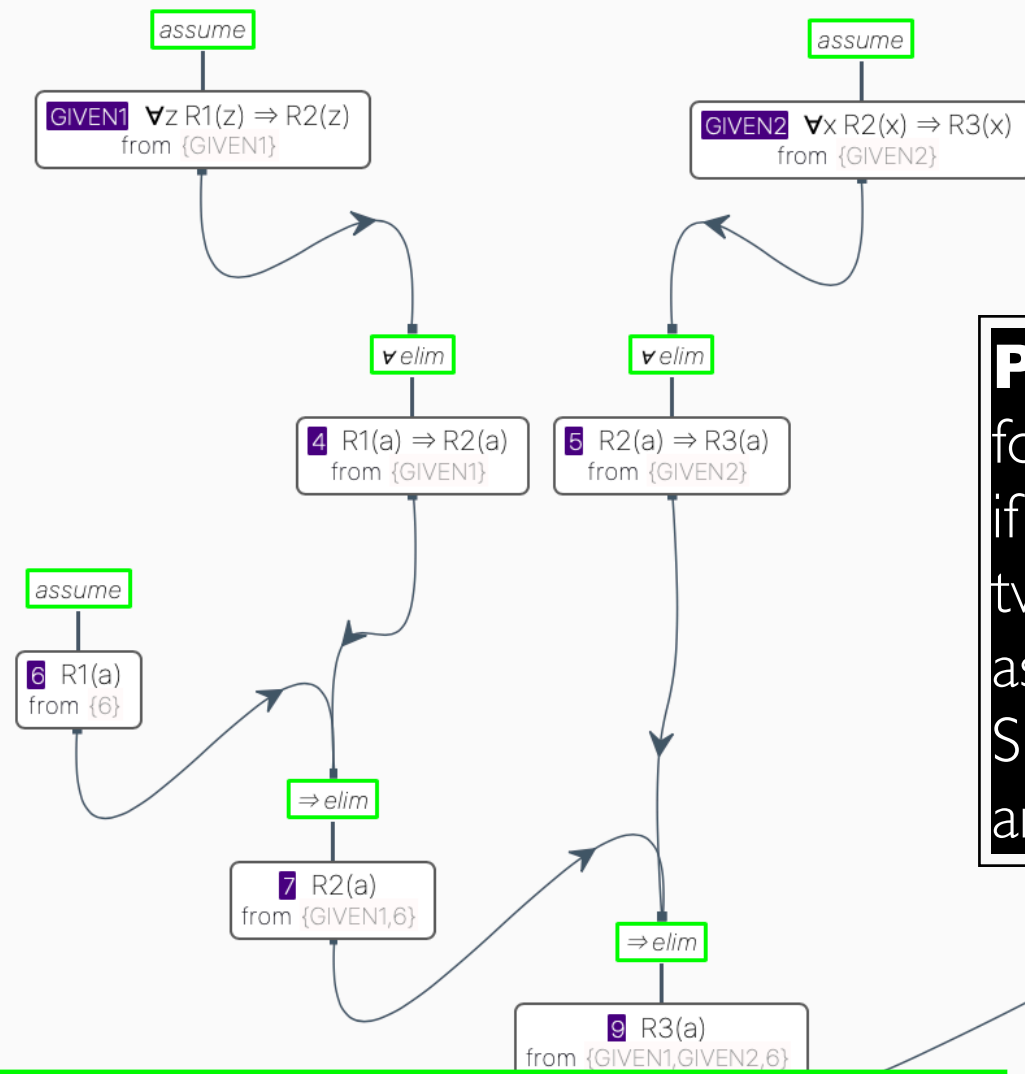


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Theorem: If everything that's an R1 is an R2, and all that's an R2 is an R3, then everything that's an R1 is an R3.

Proof: It follows from the hypothesis that for arbitrary a , both if $R1(a)$ then $R2(a)$, and if $R2(a)$ then $R3(a)$. But we can chain these two conditionals (by hypothetical syllogism, as it's known) to deduce if $R1(a)$ then $R3(a)$. Since a here is arbitrary, we know that, for anything at all, if it's an R1 it's also an R3. $\blacksquare$



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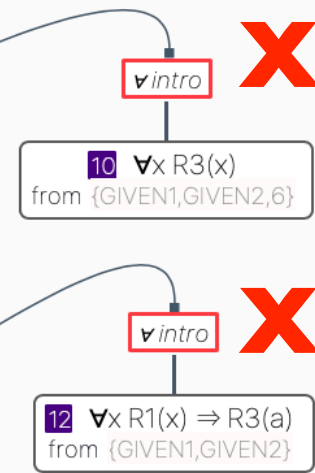
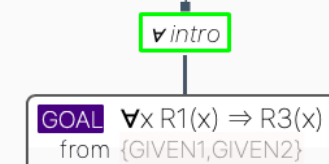
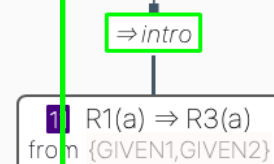
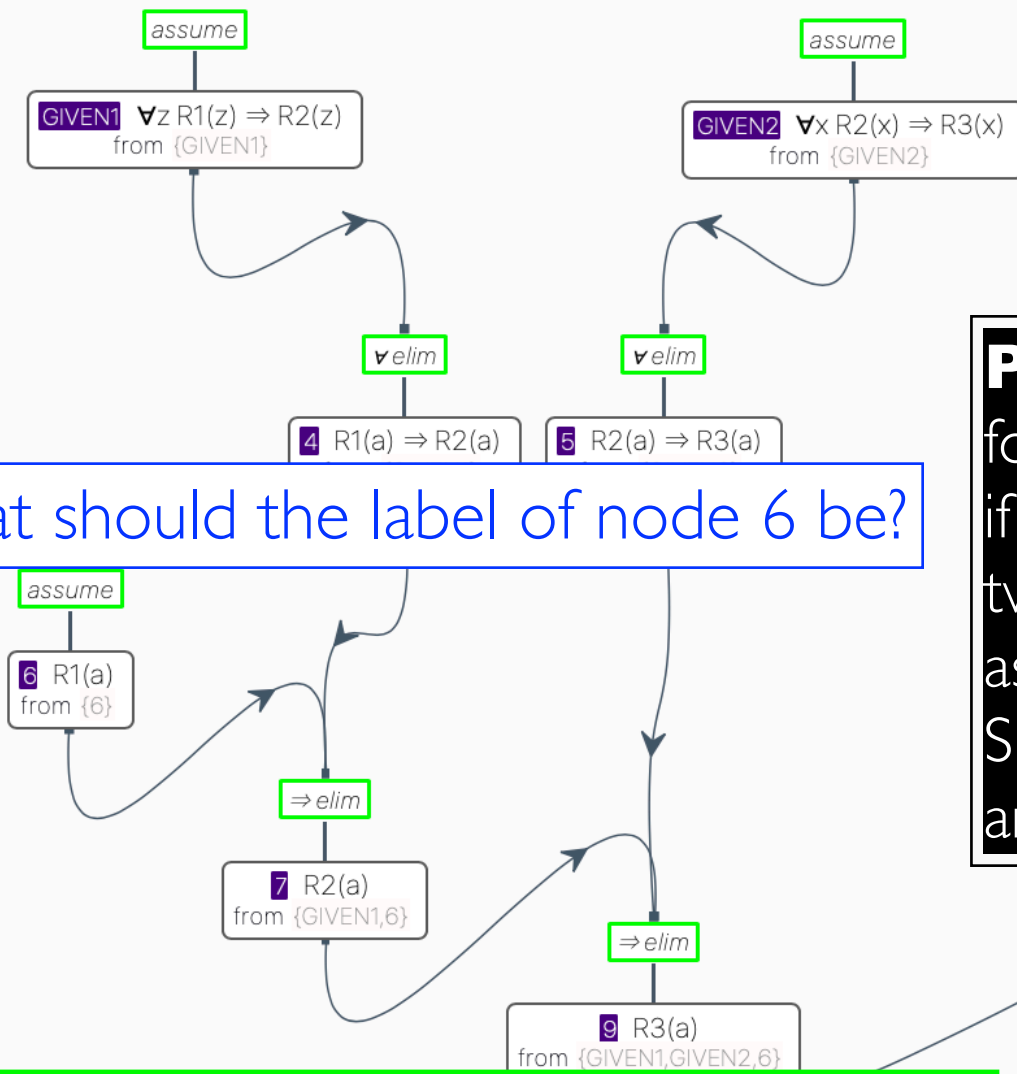
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What should the label of node 6 be?

Let's explore in HyperSlate®, by first constructing this example from scratch ...



*Hvis du forstår det, kan
du bevise det.*