

FOL III

Selmer Bringsjord

Rensselaer AI & Reasoning (RAIR) Lab

Department of Cognitive Science

Department of Computer Science

Lally School of Management & Technology

Rensselaer Polytechnic Institute (RPI)

Troy, New York 12180 USA

Intro to Logic

3/15/2021



\mathcal{L}_1 **FOL III**

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Live-action on
HyperGrader ...


ThxForThePCOracle

ThxForThePCOracle

Please attempt that now-ish; thx.

 Problem Bank Edit Problems

Exercises

 Metrics for Exercises

Download: LAMA-BDLAHSYG020421.pdf

Problems

☐ ThxForThePCOracle☒ RipsSaysNo1☐ BiconditionalIntroByChaini
... New☐  ThxForThePCOracle

This straightforward problem is quickly solved with a minimum of tedium, courtesy of the PC (entailment) provability oracle, use of which is allowed to remain in your finished proof (but no use of any other oracle can be in the finished proof). This oracle is for the logic \mathcal{L}_{PC} . Any learning of formal logic, at more than a trivial level, without the availability of the kind of AI embodied by this oracle (and more powerful ones farther up the ladder of extensional logic), is not only pedagogically unwise, but also, for the learner, downright painful.

Deadline March 18, 2021, 12:00 PM EDT Solve Submissions Metrics☒  RipsSaysNo1

This problem relates to the interesting book *The Psychology of Proof*, by psychologist L. Rips, a book that, shortly before he died, nobelist and computational-logic pioneer Herbert Simon praised as crucial to advancing automated reasoning/AI. Specifically, you are presented here with the challenge of crafting a proof that, as implied by what Rips presents in his volume, is supposed to be beyond the reach of (at least logically naïve) humans! This is quite peculiar, because as you will soon see, that which is to be proved, expressed in meta-logic, is simply this: $\{\neg(\phi \rightarrow \psi)\} \vdash \phi$.

Deadline March 18, 2021, 12:00 PM EDT

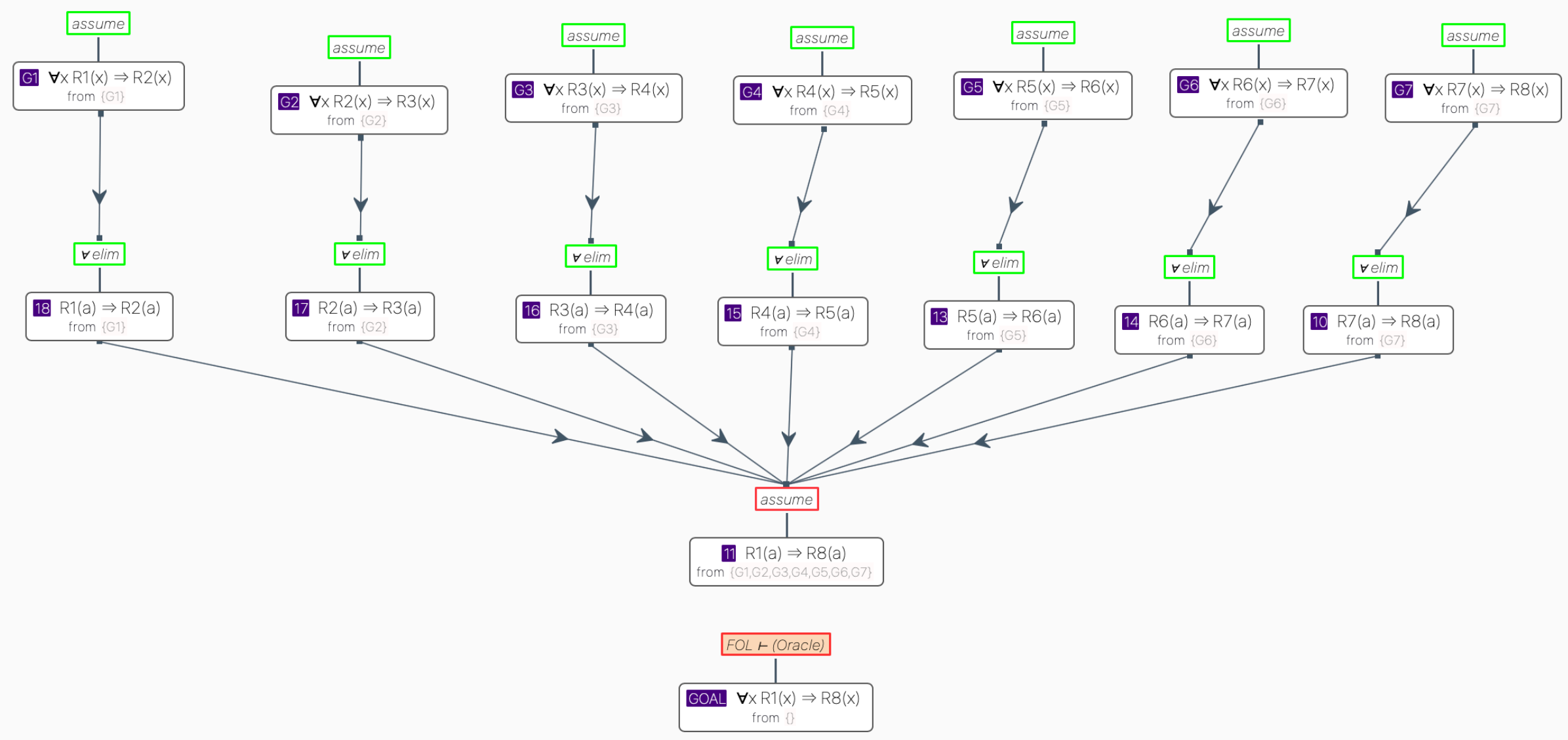
[Open in HyperSlate](#)☐ ThxForThePCOracle

This straightforward problem is quickly solved with a minimum of tedium, courtesy of the PC (entailment) provability oracle, use of which is allowed to remain in your finished proof (but no use of any other oracle can be in the finished proof). This oracle is for the logic \mathcal{L}_{PC} . Any learning of formal logic, at more than a trivial level, without the availability of the kind of AI embodied by this oracle (and more powerful ones farther up the ladder of extensional logic), is not only pedagogically unwise, but also, for the learner, downright painful.

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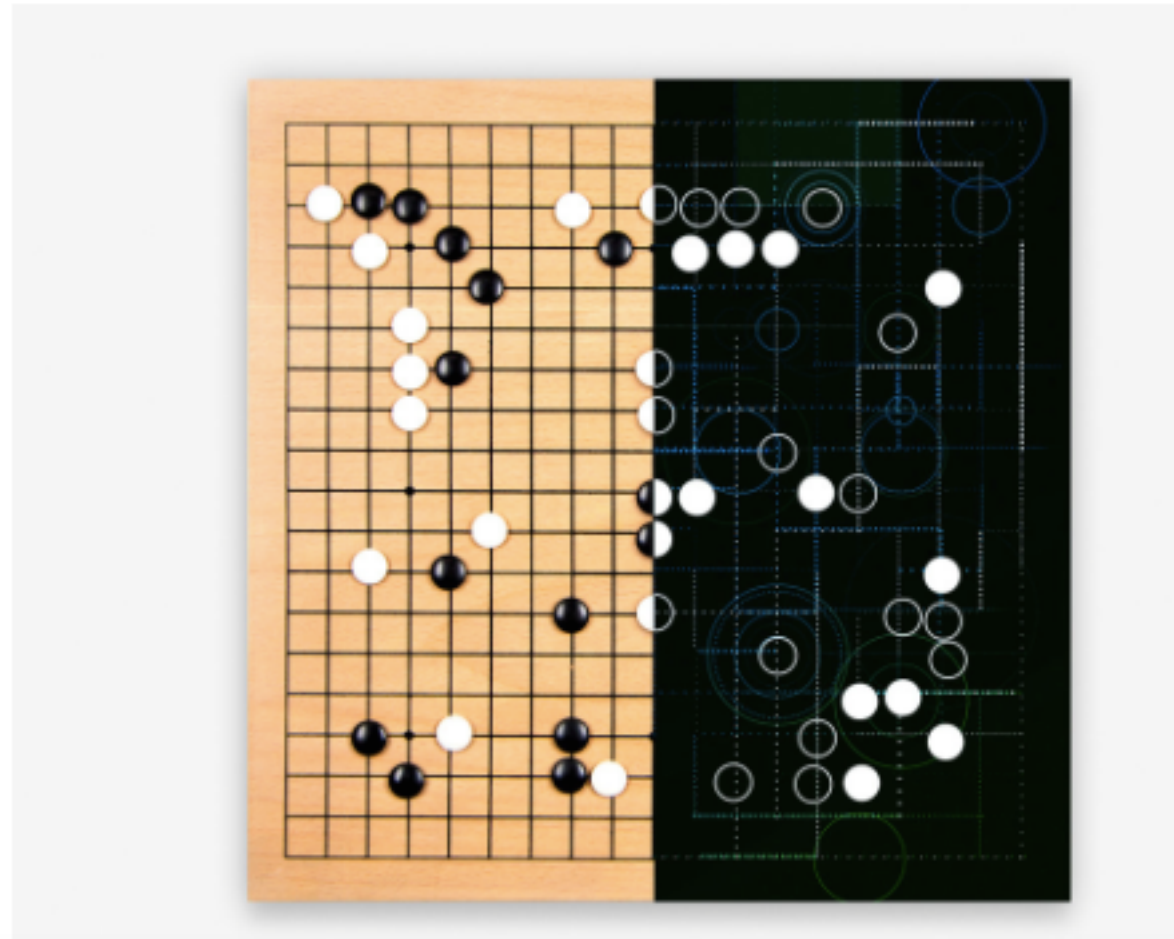
Days Hours Minutes Seconds

03:19:39:00**Problem Type:** SIMPLE**Difficulty:** 1**Points:** 10[Leaderboard](#)

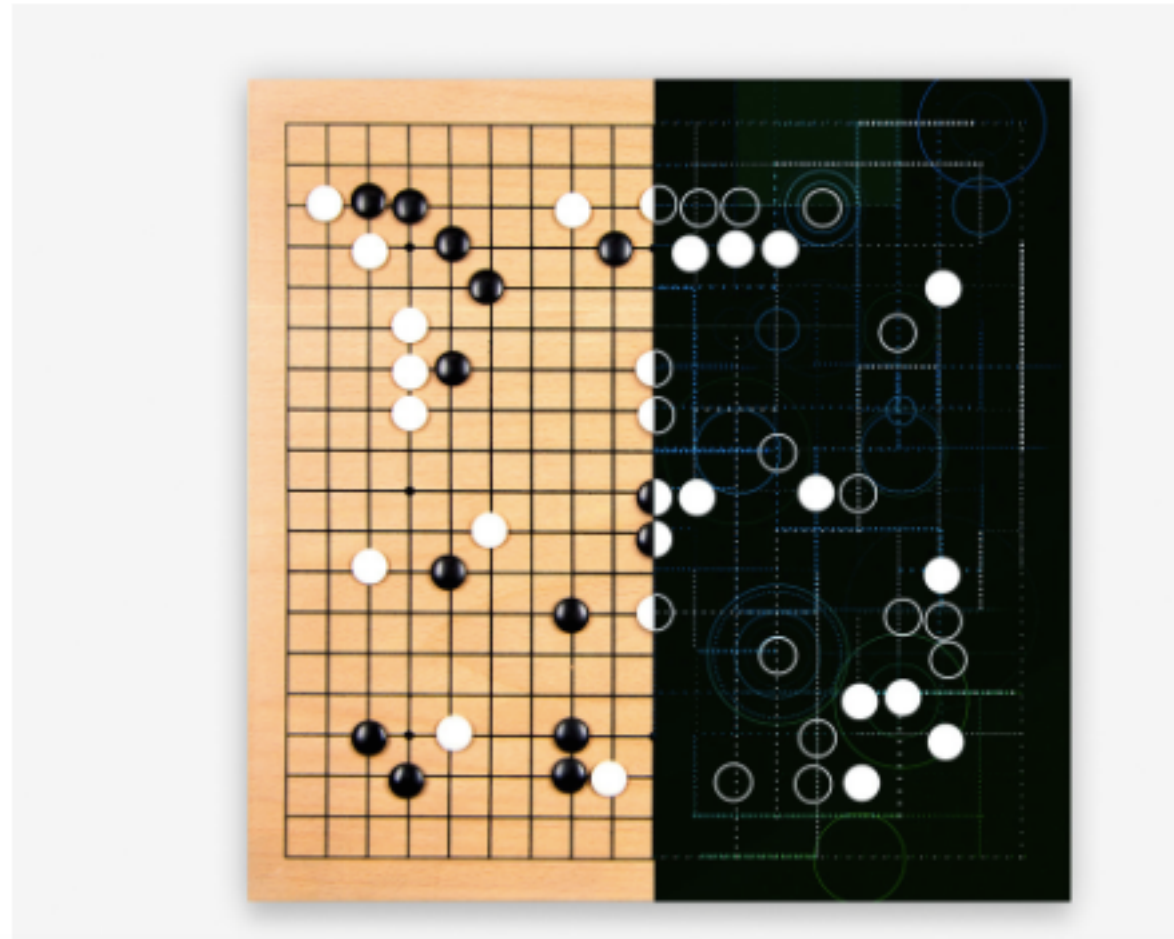


Interlude re Formal Logic & Games ...

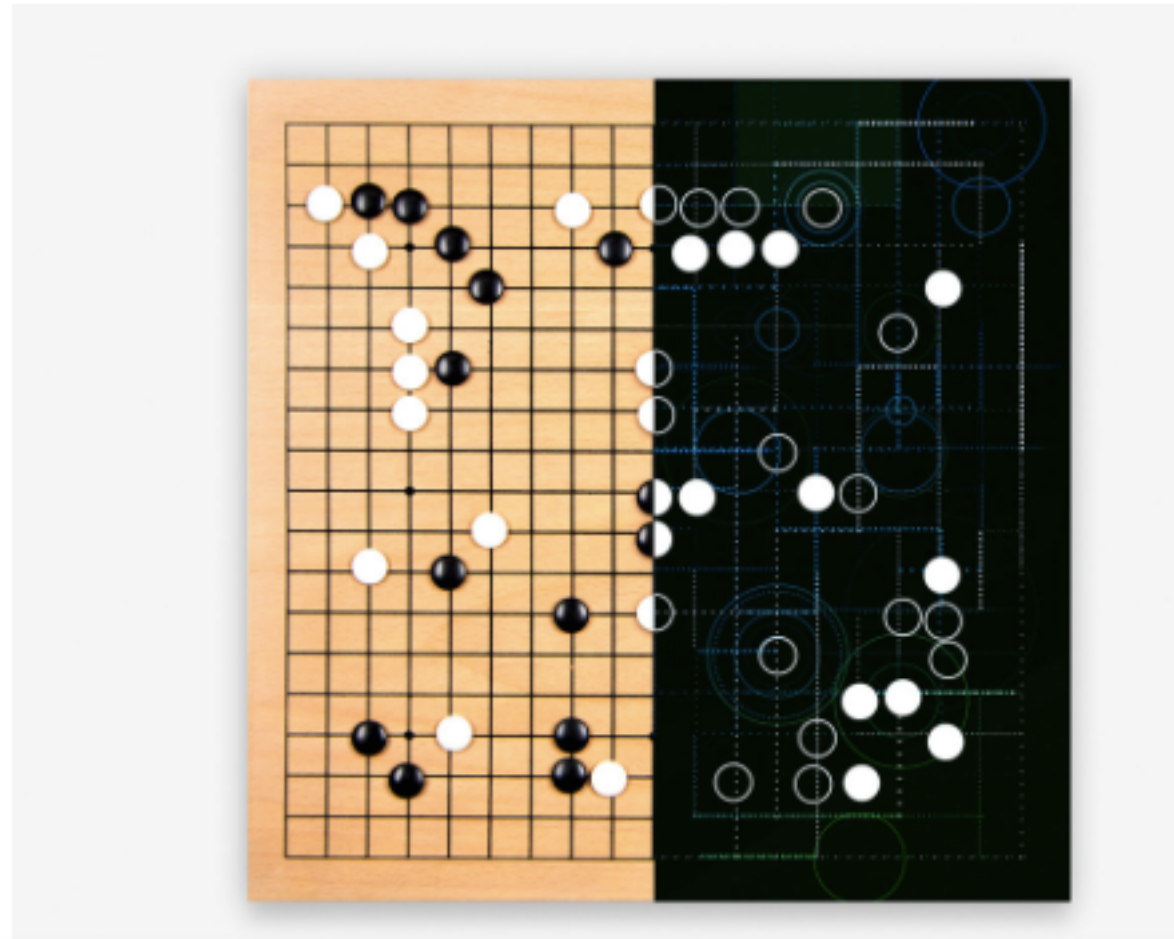
IN A HUGE BREAKTHROUGH, GOOGLE'S AI BEATS A TOP PLAYER AT THE GAME OF GO



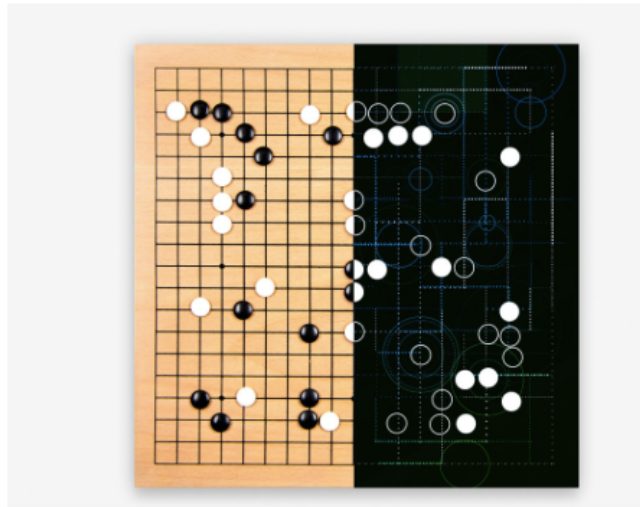
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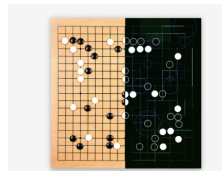
IN A HUGE BREAKTHROUGH, GOOGLE'S AI BEATS A TOP PLAYER AT THE GAME OF GO



**IN A HUGE BREAKTHROUGH,
GOOGLE'S AI BEATS A TOP
PLAYER AT THE GAME OF GO**

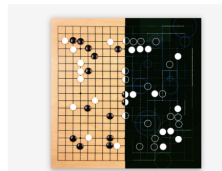


IN A HUGE BREAKTHROUGH,
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The *Entscheidungsproblem*

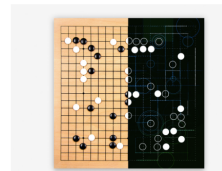
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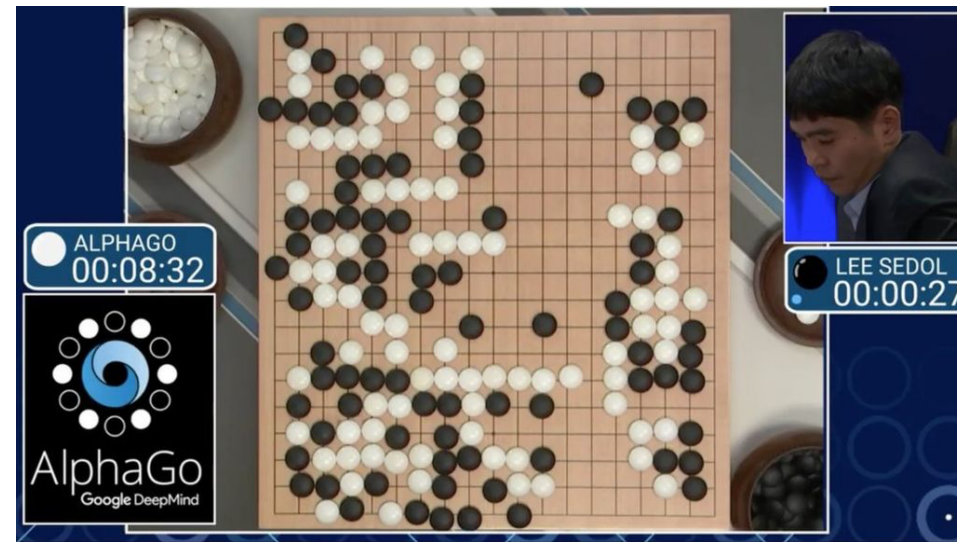


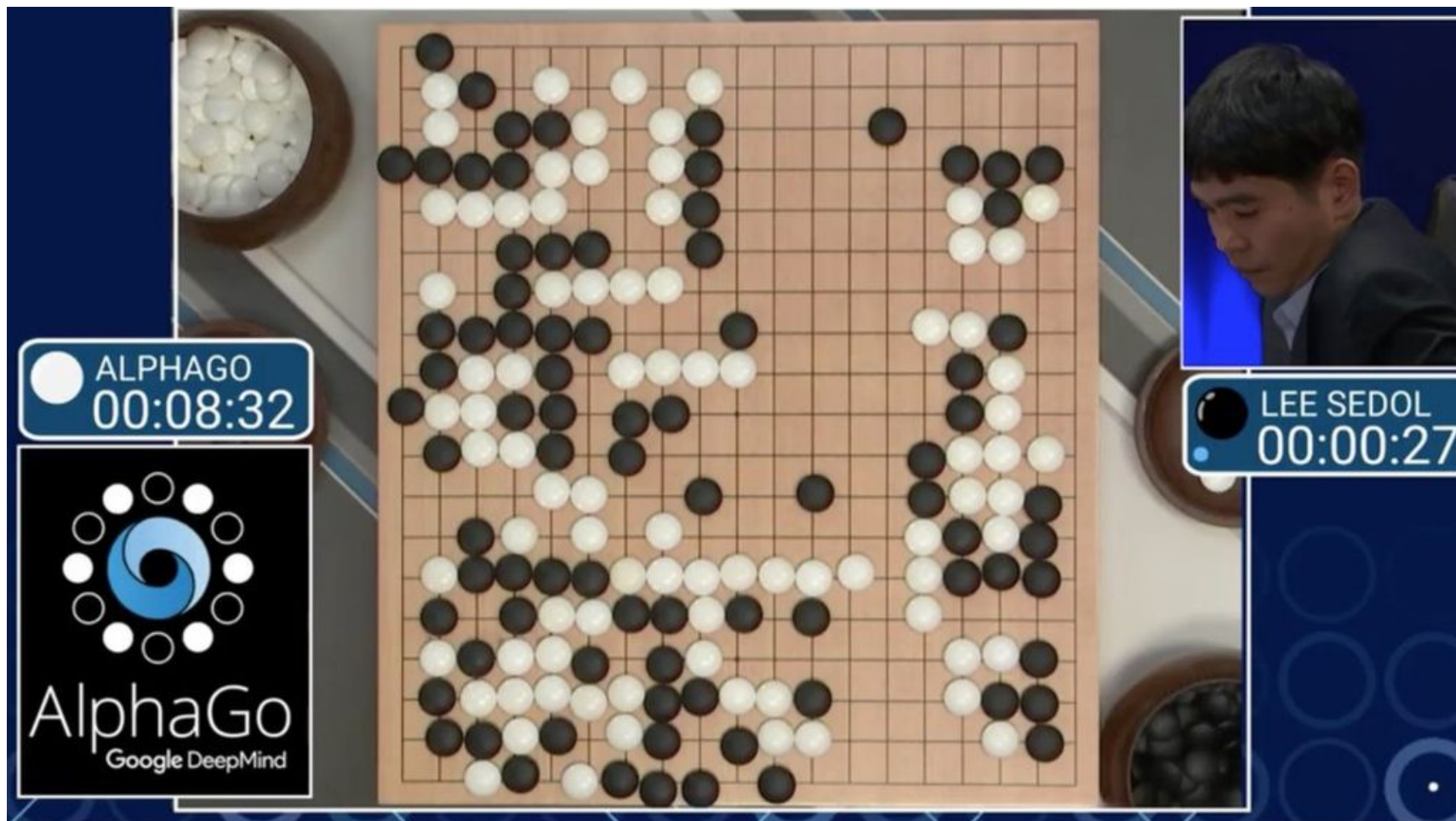
The *Entscheidungsproblem*

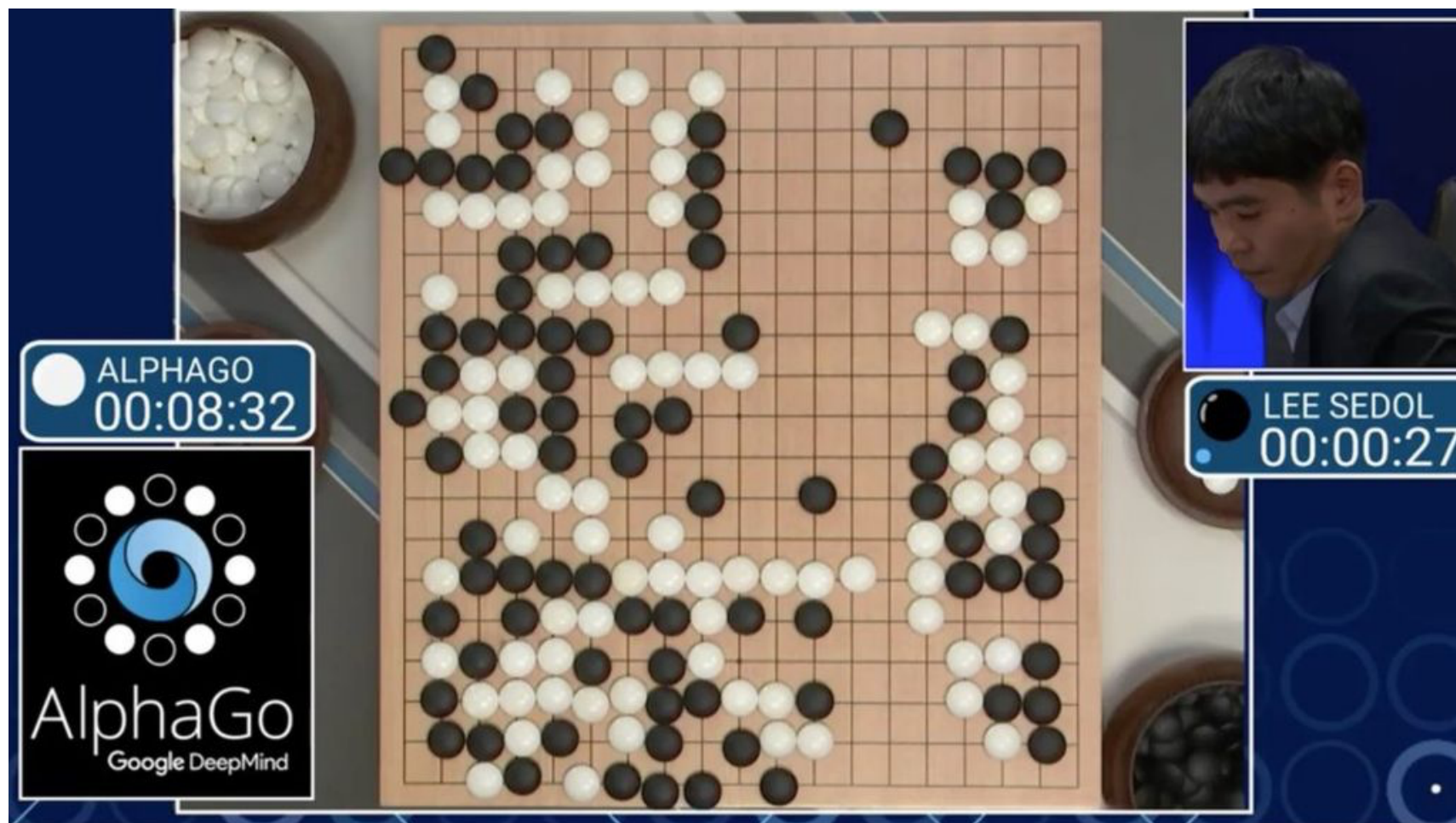
The *Entscheidungsproblem*

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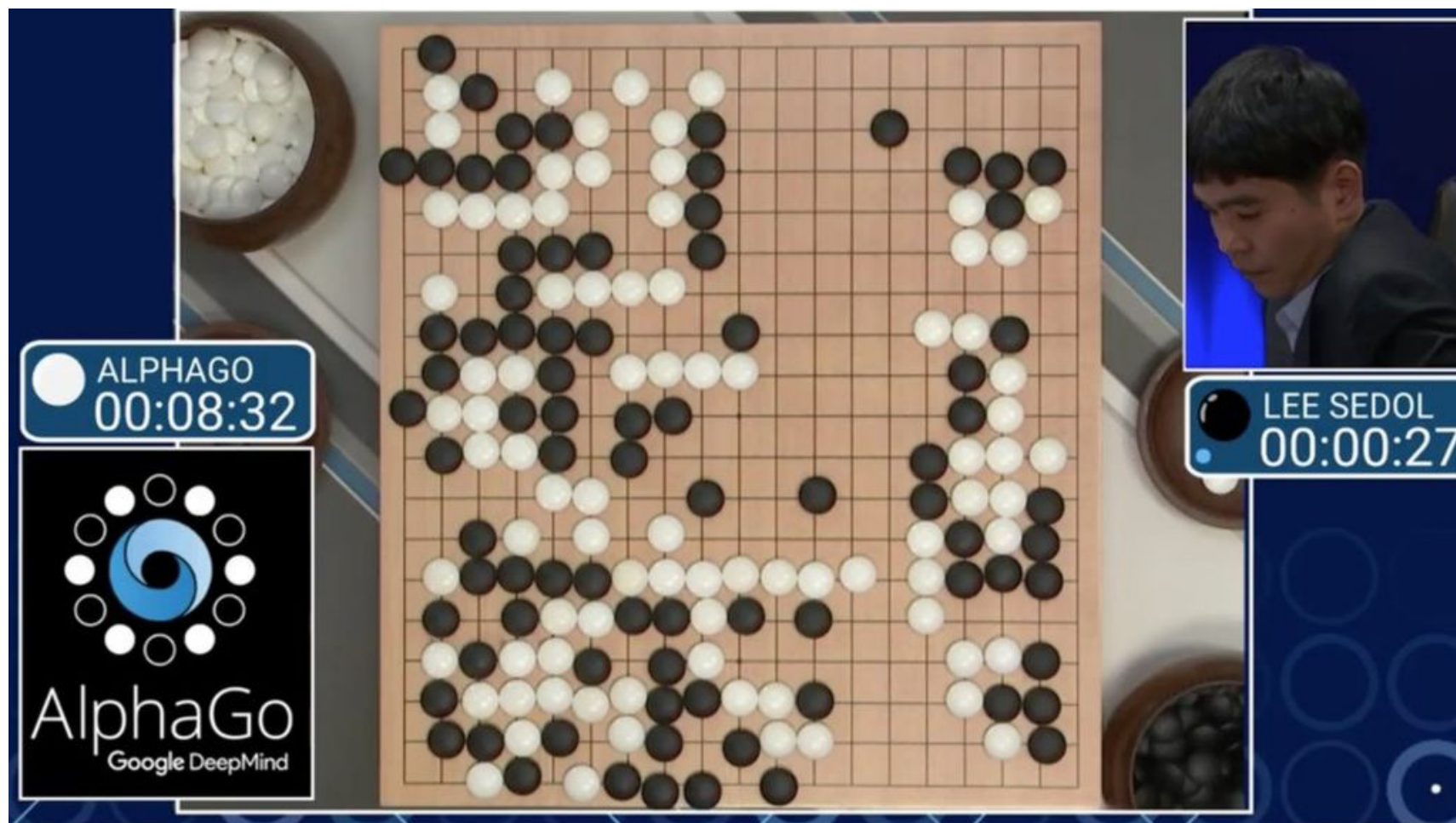






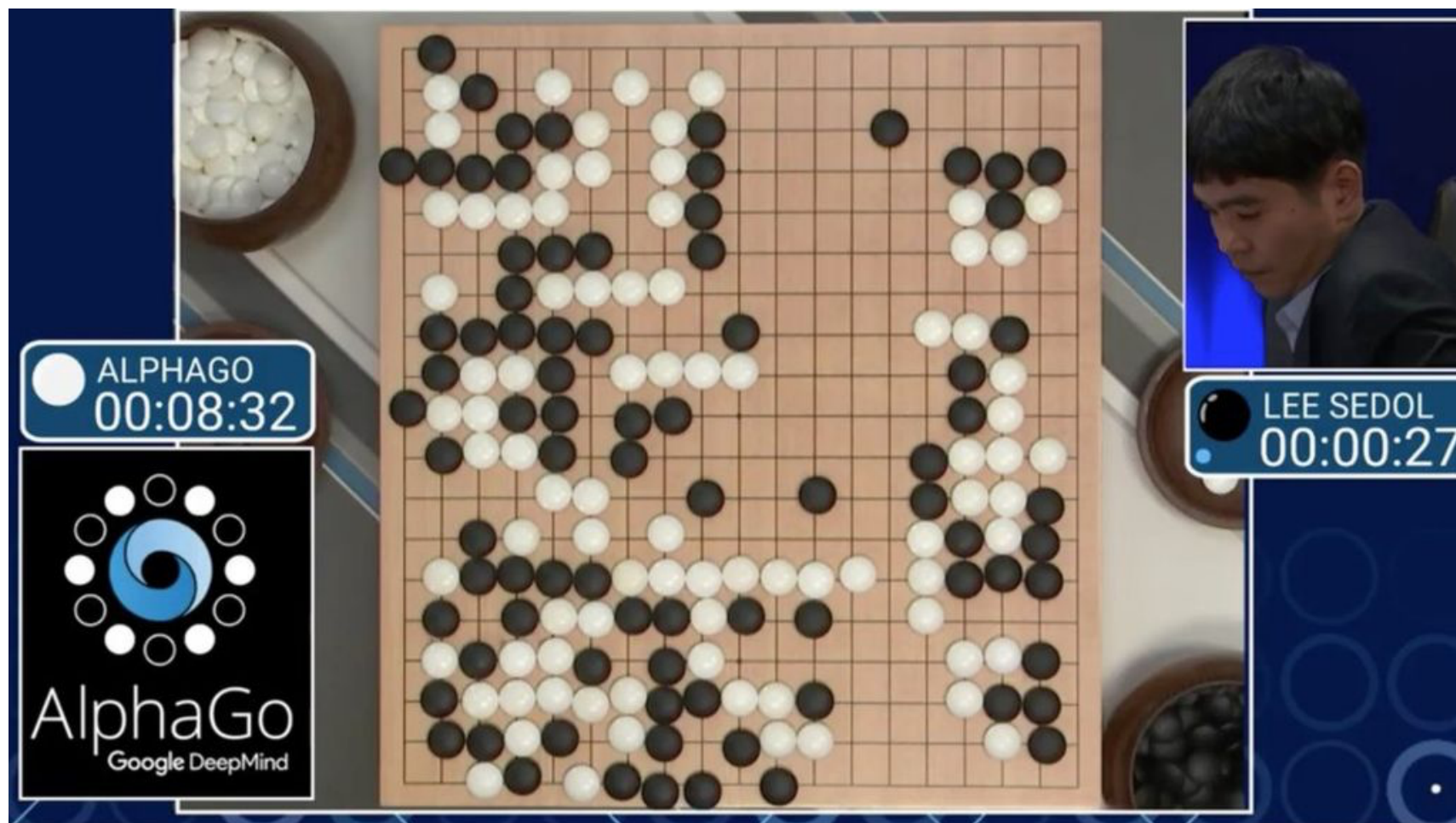


Praiseworthy *AI simplicter*, perhaps.



Praiseworthy *AI simplicter*, perhaps.

But certainly *not* AI = HI!



Praiseworthy *AI simplicter*, perhaps.

But certainly *not* AI = HI!

“AlphaGo, from the perspective of South, how many majuscule Roman letters are in black? Why do you say that?”

Logico-Mathematical Landscape that Has Them Turning in Their Graves

Super-Serious Human Cognitive Power

Serious Human Cognitive Power

Entscheidungsproblem

Mere Calculative Cognitive Power

Logico-Mathematical Landscape that Has Them Turning in Their Graves

Super-Serious Human Cognitive Power

Serious Human Cognitive Power



Descartes

Entscheidungsproblem

Mere Calculative Cognitive Power

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Descartes



Leibniz

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Descartes



Leibniz



Church

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Descartes



Leibniz



Church



Gödel

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Entscheidungsproblem

Mere Calculative Cognitive Power

Logico-Mathematical Landscape that Has Them Turning in Their Graves

Analytical Hierarchy

Serious Human Cognitive Power



Descartes



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Entscheidungsproblem

Mere Calculative Cognitive Power

Logico-Mathematical Landscape that Has Them Turning in Their Graves

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Arithmetical Hierarchy



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Entscheidungsproblem

Mere Calculative Cognitive Power

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Analytical Hierarchy

Arithmetical Hierarchy



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Turing

Entscheidungsproblem

Polynomial Hierarchy

Logico-Mathematical Landscape that Has Them Turning in Their Graves

Analytical Hierarchy

Arithmetical Hierarchy



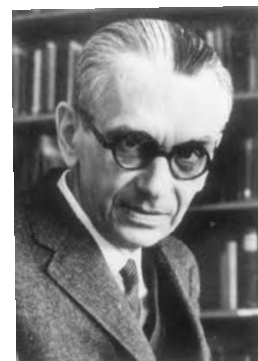
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Leibniz



Church



Gödel



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Entscheidungsproblem

Polynomial Hierarchy

$$P \subseteq NP \subseteq PSPACE = NPSPACE \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$$

Logico-Mathematical Landscape that Has Them Turning in Their Graves

Analytical Hierarchy

Arithmetical Hierarchy



Descartes



Leibniz



Church



Gödel



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 Π_2
 Σ_2
 Π_1
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Entscheidungsproblem

Polynomial Hierarchy

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Descartes



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Gödel



Go:AlphaGo



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Descartes



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Church



Gödel



Turing

Jeopardy!:



Go:AlphaGo



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Church



Gödel



Turing

Chess: Deep Blue



Jeopardy!:



Go: AlphaGo



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Descartes

Checkers: Chinook



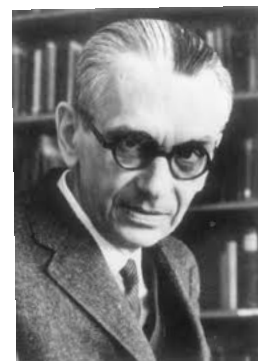
Leibniz

Chess: Deep Blue



Church

Jeopardy!:



Gödel

Go: AlphaGo



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Logico-Mathematical Landscape that Has Them Turning in Their Graves

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The first (procedural) programmer!



Descartes

Checkers: Chinook



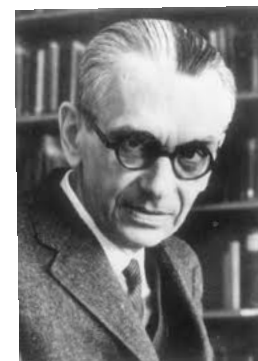
Leibniz

Chess: Deep Blue



Church

Jeopardy!:



Gödel

Go: AlphaGo



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Leibniz



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Gödel



Turing

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Jeopardy!:



Chess: Deep Blue
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Church



Turing

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Jeopardy!:



Chess: Deep Blue
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Turing

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Jeopardy!:



Chess: Deep Blue
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Jeopardy!:



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Jeopardy!:



Chess: Deep Blue



Checkers: Chinook



Go: AlphaGo



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Jeopardy!:



Chess: Deep Blue





Checkers: Chinook

Go: AlphaGo



$P \subseteq NP \subseteq PSPACE = NPSPACE \subseteq EXPTIME \subseteq NEXPTIME \subseteq EXPSPACE$

Rengo Kriegspiel



U.S. Go Congress | Crosstabs | Free E-Journal | Upcoming Events | Ratings | Kids & Teens | Latest Go News

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American Go E-Journal

US Go Congress Goes a Little Crazy

Wednesday August 13, 2014



"White plays capturing black, putting herself and black into atari," calls Crazy Go TD Terry Benson. He officiated several games of Rengo Kriegspiel on Tuesday evening – a pair go game in which all four players face away from the main board and play their stones on their own empty board in front of them; the only clues about where their opponents — and even their partner — have played comes when they make an illegal move, or play where their own team or their opponents already have stones. Rengo Kriegspiel is only one of dozens of variants on the game of go that were played by an enthusiastic crowd of around 100 players. Familiar games include Magnetic Go, 4 Color Go, Tessellation Go, 3D Go, Spiral Go, and Blind Go. "After all these years, it's still crazy," said TD and Crazy Go founder Terry Benson. New Crazy Go games, never before played at a Go Congress, were even invented on the spot. Four players donned sleeping masks to block their vision and transformed Blind Go into Rengo Blind Go, and a few other players added the fundamentals of Tiddlywinks to their go game. Spectators and players alike are enthusiastic about the creativity of the games and the fun of adding a little Crazy to Go; "Crazy Go is my favorite part of the Congress!" said Bob Crites.

- report/photos by Karoline Li



CATEGORIES:

ALL

CALENDAR

COLUMNS

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REDMOND REVIEWS

THE JANICE KIM FILES

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EVENTS/TOURNAMENTS

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IMSA ELITE MIND GAMES

OTHER

N.A. GO CONVENTION

PAIR GO

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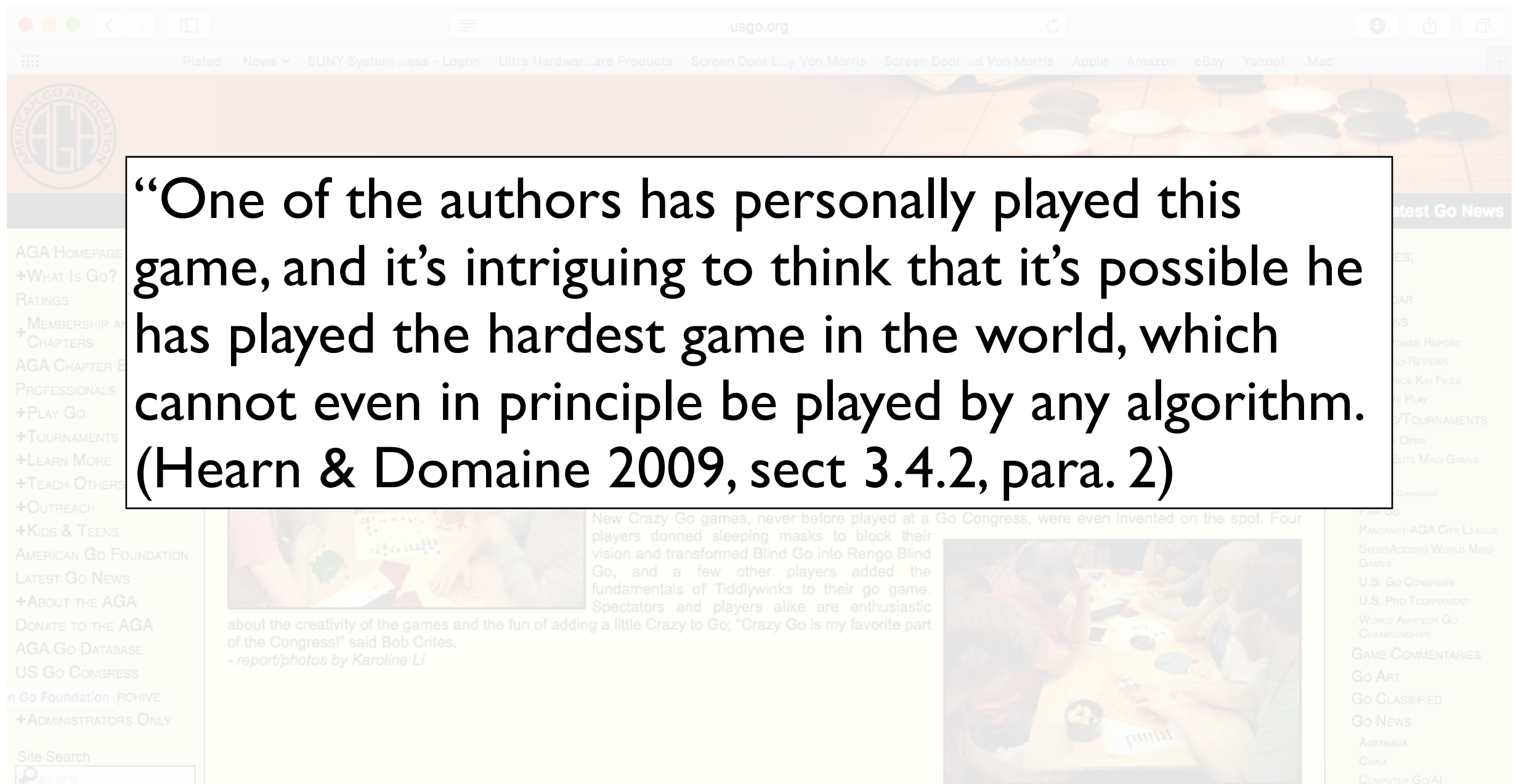
AUSTRALIA

CHINA

COMPUTER GO/AI

Rengo Kriegspiel

“One of the authors has personally played this game, and it’s intriguing to think that it’s possible he has played the hardest game in the world, which cannot even in principle be played by any algorithm. (Hearn & Domaine 2009, sect 3.4.2, para. 2)



But starting simpler ...

Tabular “Deduction” (Example)

Logic Puzzles

Story

	Eduardo	Greg	Jay	Patrick	Salvador	indigo	lime	maroon	orange	red	Fullerton	Hollister	San Pedro	Templeton	Urbandale
22 minutes															
23 minutes															
24 minutes															
25 minutes															
26 minutes															
Fullerton															
Hollister															
San Pedro															
Templeton															
Urbandale															
indigo															
lime															
maroon															
orange															
red															

5K Fun Run

Valero's 5k Fun Run was held yesterday in the downtown district. Determine the shirt color and hometown of each of the top five runners, and match each to their finishing time.

- Patrick, who is from Templeton and finished with a time of 24 minutes, wore neither the red nor the maroon shirt.
- The runner in the orange shirt finished one minute before the one in the
- finished in
- wasn't
- om
- testant
- maroon
- one finished two minutes before Greg.
- The runner who finished in 25 minutes wore the lime shirt.
- Jay didn't finish with the fastest time.
- The runner from San Pedro was either the one in the orange shirt or Eduardo.

Tabular “Deduction” (Example)

Logic Puzzles

Story

	Eduardo	Greg	Jay	Patrick	Salvador	indigo	lime	maroon	orange	red	Fullerton	Hollister	San Pedro	Templeton	Urbandale
22 minutes															
23 minutes															
24 minutes															
25 minutes															
26 minutes															
Fullerton															
Hollister															
San Pedro															
Templeton															
Urbandale															
indigo															
lime															
maroon															
orange															
red															

- Patrick, who is from Templeton and finished with a time of 24 minutes, wore neither the red nor the maroon shirt.
- The runner in the orange shirt finished one minute before the one in the maroon shirt.
- The runner who finished in 23 minutes (who wasn't Eduardo) wasn't from Hollister.
- The Urbandale contestant wore the red shirt.
- The runner in the maroon shirt finished two minutes before Greg.
- The runner who finished in 25 minutes wore the lime shirt.
- Jay didn't finish with the fastest time.
- The runner from San Pedro was either the one in the orange shirt or Eduardo.

Tabular “Deduction” (Example)

Logic Puzzles

Story

	Eduardo	Greg	Jay	Patrick	Salvador	indigo	lime	maroon	orange	red	Fullerton	Hollister	San Pedro	Templeton	Urbandale
22 minutes															
23 minutes															
24 minutes															
25 minutes															
26 minutes															
Fullerton				X											
Hollister				X											
San Pedro				X											
Templeton	X	X	X	●	X										
Urbandale				X											
indigo															
lime															
maroon															
orange															
red															

- Patrick, who is from Templeton and finished with a time of 24 minutes, wore neither the red nor the maroon shirt.
- The runner in the orange shirt finished one minute before the one in the maroon shirt.
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Tabular “Deduction” (Example)

Logic Puzzles

Story

	Eduardo	Greg	Jay	Patrick	Salvador	indigo	lime	maroon	orange	red	Fullerton	Hollister	San Pedro	Templeton	Urbandale
22 minutes															
23 minutes															
24 minutes															
25 minutes															
26 minutes															
Fullerton				X											
Hollister				X											
San Pedro				X											
Templeton	X	X	X	●	X										
Urbandale				X											
indigo															
lime															
maroon															
orange															
red															

1. Patrick, who is from Templeton and finished with a time of 24 minutes, wore neither the red nor the maroon shirt.

2. The runner in the orange shirt finished one minute before the one in the maroon shirt.

3. The runner who finished in 23 minutes (who wasn't Eduardo) wasn't from Hollister.

4. The Urbandale contestant wore the red shirt.

6. The runner who finished in 25 minutes wore the lime shirt.

7. Jay didn't finish with the fastest time.

8. The runner from San Pedro was either the one in the orange shirt or Eduardo.

In HyperSlate ...

Tabular “Deduction” (Example)

Logic Puzzles

Story

	Eduardo	Greg	Jay	Patrick	Salvador	indigo	lime	maroon	orange	red	Fullerton	Hollister	San Pedro	Templeton	Urbandale
22 minutes															
23 minutes															
24 minutes															
25 minutes															
26 minutes															
Fullerton				X						X					
Hollister				X						X					
San Pedro				X						X					
Templeton	X	X	X	●	X					X					
Urbandale				X		X	X	X	X	●					
indigo															
lime															
maroon															
orange															
red															

- Patrick, who is from Templeton and finished with a time of 24 minutes, wore neither the red nor the maroon shirt.
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Tabular “Deduction” (Example)

Logic Puzzles

Story

	Eduardo	Greg	Jay	Patrick	Salvador	indigo	lime	maroon	orange	red	Fullerton	Hollister	San Pedro	Templeton	Urbandale
22 minutes															
23 minutes															
24 minutes															
25 minutes															
26 minutes															
Fullerton				X						X					
Hollister				X						X					
San Pedro				X						X					
Templeton	X	X	X	●	X					X					
Urbandale				X		X	X	X	X	●					
indigo															
lime															
maroon															
orange															
red															

These two cells tell you something about the cell in yellow.

- Patrick, who is from Templeton and finished with a time of 24 minutes, wore neither the red nor the maroon shirt.
- The runner in the orange shirt finished one minute before the one in the maroon shirt.
- The runner who finished in 23 minutes (who wasn't Eduardo) wasn't from Hollister.
- The Urbandale contestant wore the red shirt.
- The runner in the maroon shirt finished two minutes before Greg.
- The runner who finished in 25 minutes wore the lime shirt.
- Jay didn't finish with the fastest time.
- The runner from San Pedro was either the one in the orange shirt or Eduardo.

Tabular “Deduction”: It’s Taught!



Example

Grace, Dylan, Kira, and Diego are each wearing different colored shirts. Grace’s shirt is red. Dylan’s shirt is not white. Kira’s shirt is not green. Diego’s shirt is not yellow or white. What color shirt is each person wearing?

First, make a chart to show what you know.

- Each shirt is a different color.
- Grace’s shirt is red.
- Dylan’s shirt is not white.
- Kira’s shirt is not green.
- Diego’s shirt is not yellow or white.

	Red	White	Green	Yellow
Grace	yes	no	no	no
Dylan	no	no		
Kira	no		no	
Diego	no	no	yes	no

Then use reasoning and the information in the chart to complete the chart and find the answer.

Grace’s shirt is red, so no other shirt can be red.

Diego’s shirt is not red, white, or yellow, so it must be green.

Dylan’s shirt must be yellow because it cannot be red, white, or green.

That means Kira’s shirt must be white.

Solve

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IMHO very bad idea—if *before* real learning of deduction to answer “Why, exactly? Prove it!”

Tabular “deduction” not the skill that’s needed.

8:29 AM

iPad

8:29 AM

91

Recall from Lesson 4-8 that the complex numbers $a + bi$ and $a - bi$ are conjugates. Similarly, the irrational numbers $a + \sqrt{b}$ and $a - \sqrt{b}$ are conjugates. If a complex number or an irrational number is a root of a polynomial equation with rational coefficients, so is its conjugate.

TAKE NOTE Theorem

Conjugate Root Theorem

If $P(x)$ is a polynomial with *rational* coefficients, then irrational roots of $P(x) = 0$ that have the form $a + \sqrt{b}$ occur in conjugate pairs. That is, if $a + \sqrt{b}$ is an irrational root with a and b rational, then $a - \sqrt{b}$ is also a root.

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Every quadratic polynomial equation has two roots, every cubic polynomial equation has three roots, and so on.

This result is related to the *Fundamental Theorem of Algebra*. The German mathematician Carl Friedrich Gauss (1777–1855) is credited with proving this theorem.

TAKE NOTE Theorem

The Fundamental Theorem of Algebra

If $P(x)$ is a polynomial of degree $n \geq 1$, then $P(x) = 0$ has exactly n roots, including multiple and complex roots.

iPad

From Algebra 2

Practice and Problem-Solving Exercises - Contir

Determine whether each of the following statements is **always**, **sometimes**, or **never** true.

- 41. A polynomial function with real coefficients has real zeros.
- 42. Polynomial functions with complex coefficients have one complex zero.
- 43. A polynomial function that does not intercept the x -axis has complex roots only.
- 44. **Reasoning** A 4th-degree polynomial function has zeros at 3 and $5 - i$. Can $4 + i$ also be a zero of the function? Explain your reasoning.
- 45. **Open-Ended** Write a polynomial function that has four possible rational zeros but no actual rational zeros.
- 46. **Reasoning** Show that the Fundamental Theorem of Algebra must be true for all quadratic polynomial functions.

C • Challenge

- 47. Use the Fundamental Theorem of Algebra and the Conjugate Root Theorem to show that any odd degree polynomial equation with real coefficients has at least one real root.
- 48. **Reasoning** What is the maximum number of points of intersection between the graphs of a quartic and a quintic polynomial function?
- 49. **Reasoning** What is the least possible degree of a polynomial with rational coefficients, leading coefficient 1, constant term 5, and zeros at $\sqrt{2}$ and $\sqrt{3}$? Show that such a polynomial has a rational zero and indicate this zero.

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Foundations of Computer Science, CSCI 2200, RPI, Spring 2021

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Foundations of Computer Science, CSCI 2200, RPI, Spring 2021

Quizzes and Exams

- [3 Quizzes](#)
- [Cumulative midterm](#)
- [Cumulative final](#)

Quiz 1	Solution
------------------------	--------------------------

Midterm	Solution
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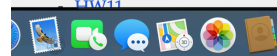
Quiz 2	Solution
------------------------	--------------------------

Quiz 3	Solution
------------------------	--------------------------

Final	Solution
-----------------------	--------------------------

Homeworks

- [HW1](#)
- [HW2](#)
- [HW3](#)
- [HW4](#)
- [HW5](#)
- [HW6](#)
- [HW7](#)
- [HW8](#)
- [HW9](#)
- [HW10](#)
- [HW11](#)



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Foundations of Computer Science, CSCI 2200, RPI, Spring 2021

Quizzes and Exams

(d) The negation of “The reaction to every action is equal and opposite” is:

- ☐ A “There are actions whose reactions are not equal and not opposite”.
- ☐ B “There are actions whose reactions are either not equal or not opposite”.
- ☐ C “For every action, the reaction is not equal and not opposite”.
- ☐ D “For every action, the reaction is either not equal or not opposite”.
- ☐ E None of the above.



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Foundations of Computer Science, CSCI 2200, RPI, Spring 2021

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The Game of LogiNim \mathcal{L}

In HyperSlate®

The Game of LogiNim \mathcal{L} in HyperSlate®

Selmer Bringsjord

Motalen LLC

0220210900NY

A *logacist directed acyclic hypergraph*, hereafter simply a *hypergraph*, is a pair

$$\mathcal{H} := \langle N, A \rangle$$

where

- each *node* $\nu \in N$ contains some formula $\phi \in \mathcal{L}$, where \mathcal{L} is a background formal language, possibly including a label l_ϕ for the node, and the set of all assumptions on which inference of ϕ may rely;
- each *arc* $a \in A$ is a pair composed of a label l_σ for some $\sigma \in \mathcal{I}$, a collection of inference schemata, and one of $\{\textcolor{red}{r}, \textcolor{green}{g}\}$;
- arcs are directed; and
- no *cycles* are permitted.

Back to FOL ...

Our Final New Inference Rule in FOL

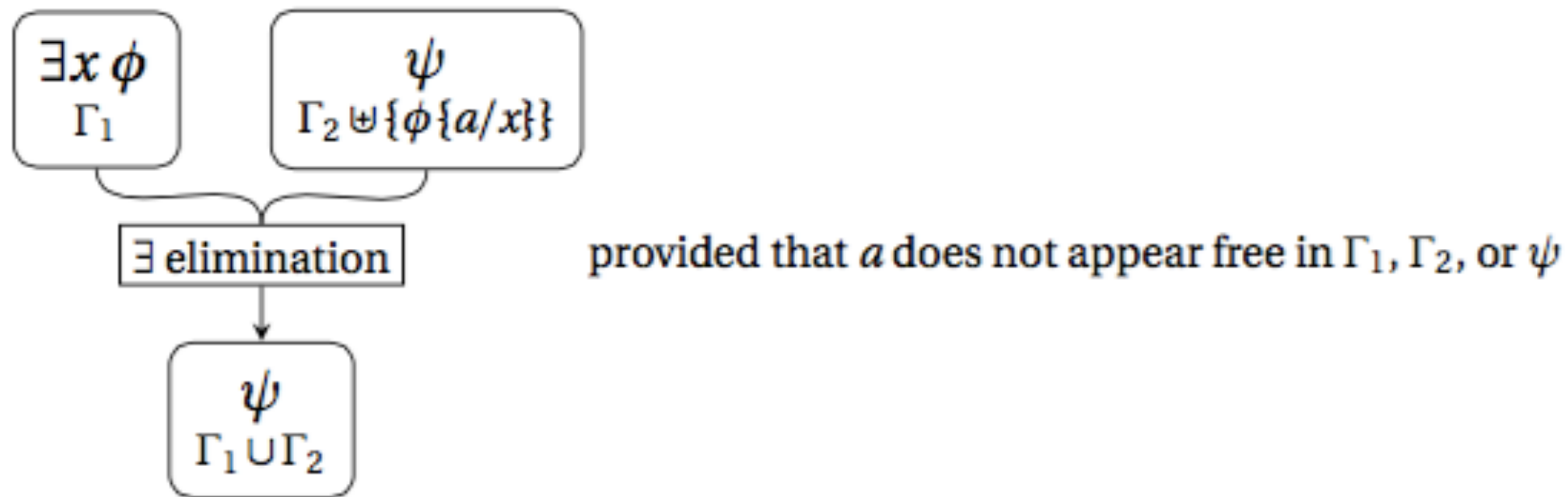
Our Final New Inference Rule in FOL

- existential elimination (intuitively put):

Our Final New Inference Rule in FOL

- existential elimination (intuitively put):
 - If we know that (i) there's something x which is an R , and (ii) on the supposition that a is an arbitrary representative (a “witness”) of such an x we can prove P , then we are permitted to deduce P from (i) alone.

existential elimination, precise version:

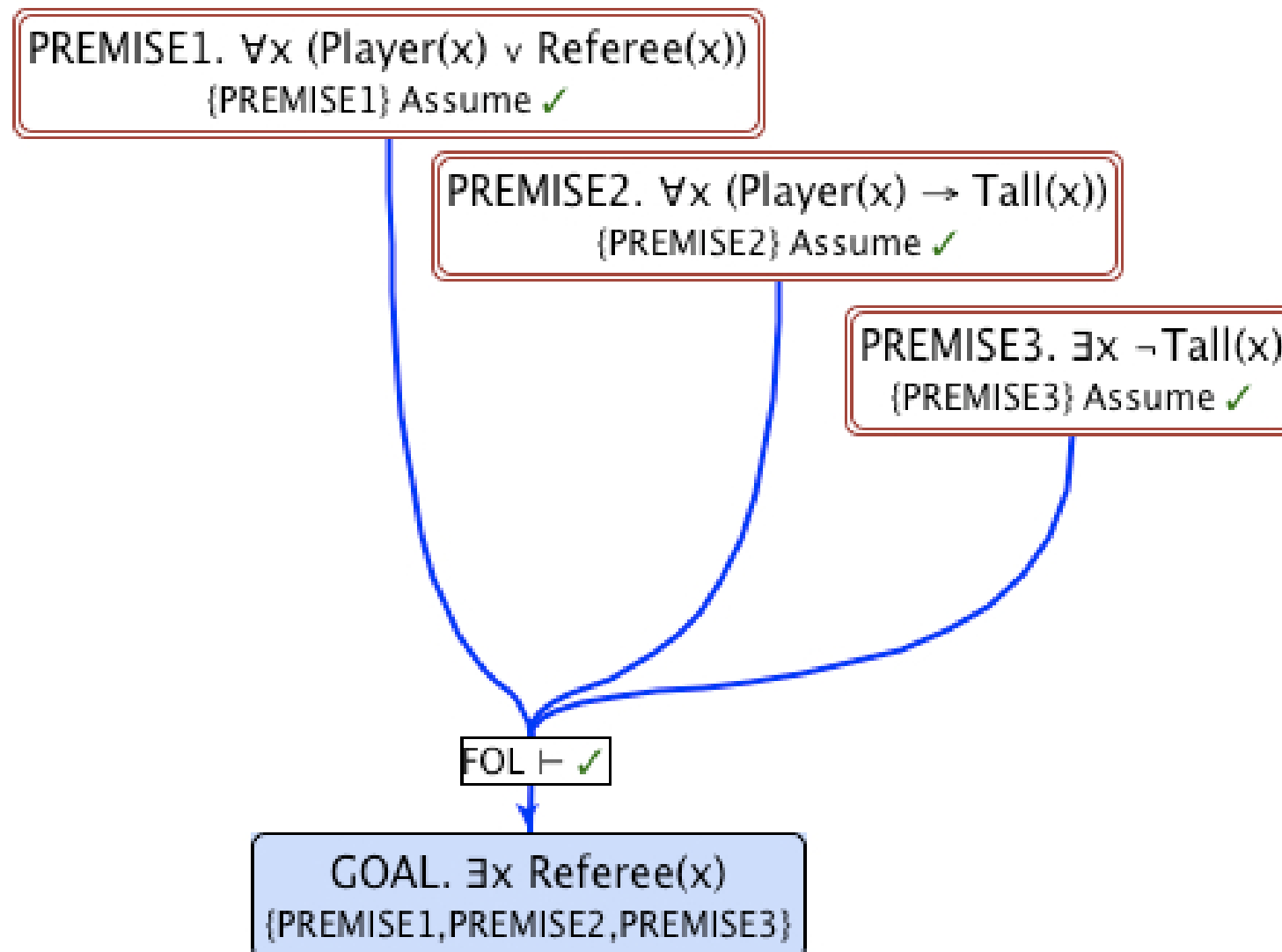


Starting State of Workspace

(Assumes a domain of e.g. players on a
March-madness basketball court.)

Starting State of Workspace

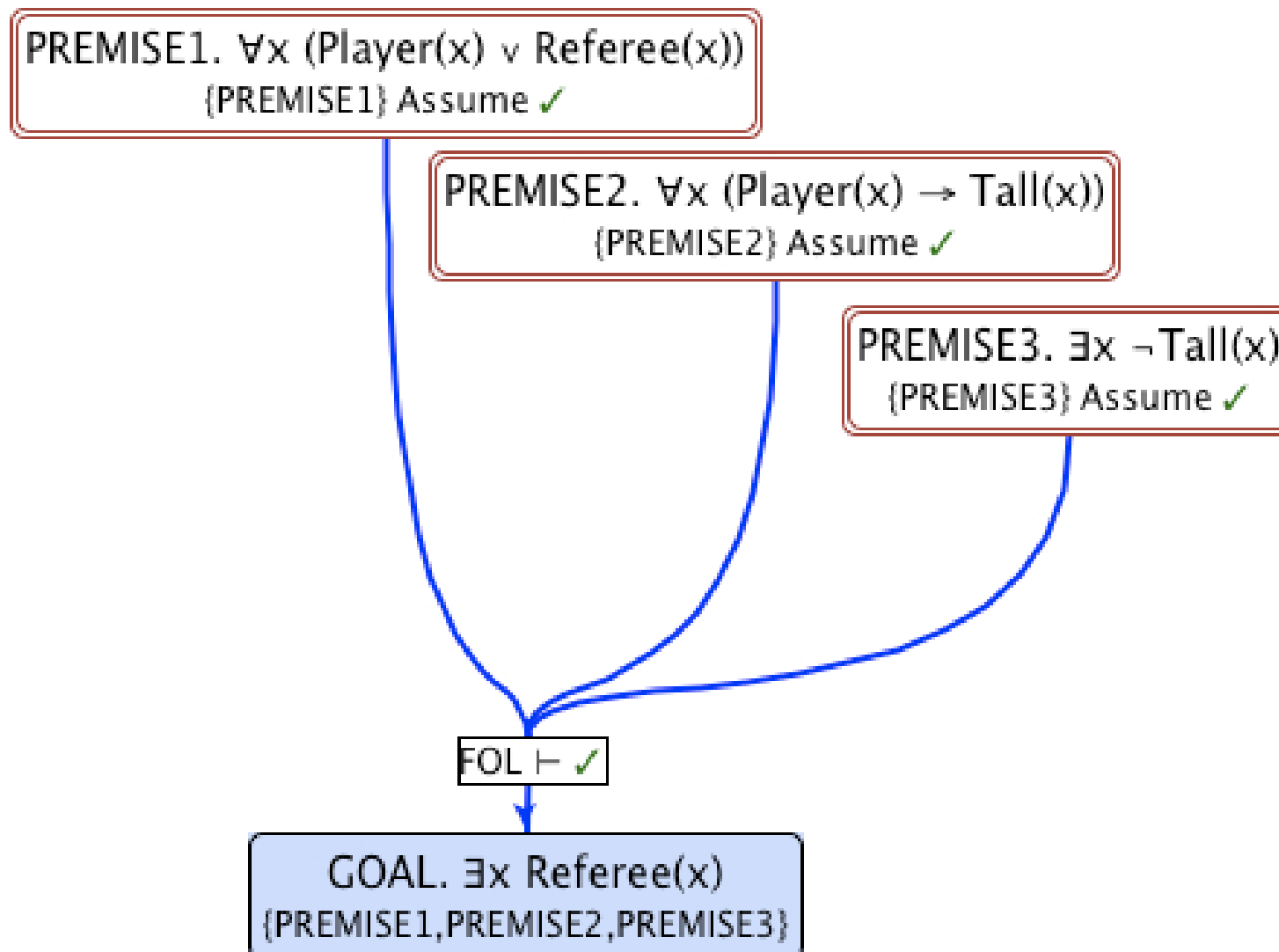
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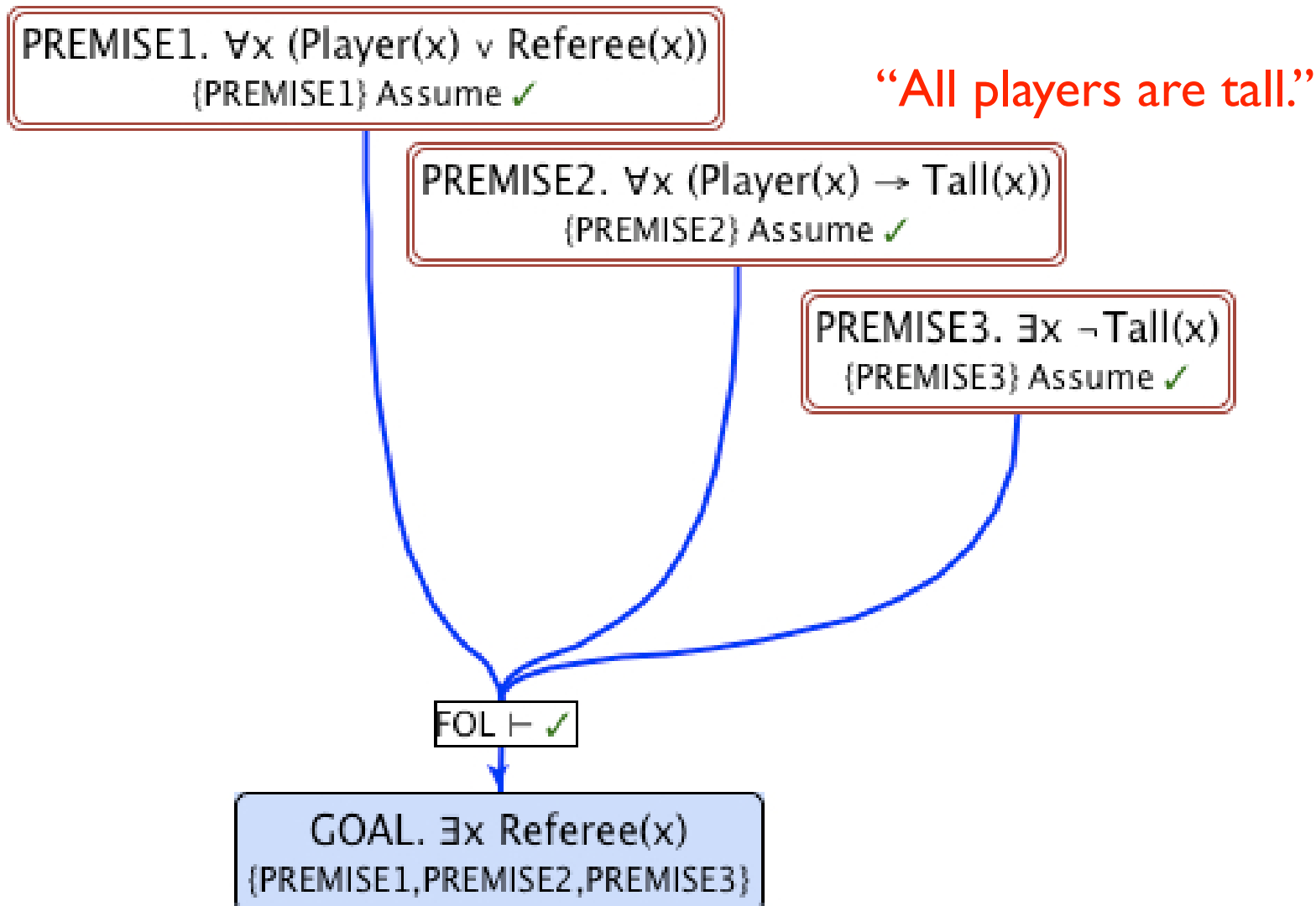
“Each and every thing is
either a player or a referee.”



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“Each and every thing is
either a player or a referee.”

PREMISE1. $\forall x (\text{Player}(x) \vee \text{Referee}(x))$
{PREMISE1} Assume ✓

“All players are tall.”

PREMISE2. $\forall x (\text{Player}(x) \rightarrow \text{Tall}(x))$
{PREMISE2} Assume ✓

PREMISE3. $\exists x \neg \text{Tall}(x)$
{PREMISE3} Assume ✓

“There’s a non-tall thing.”

FOL \vdash ✓

GOAL. $\exists x \text{Referee}(x)$
{PREMISE1, PREMISE2, PREMISE3}

Step 1

PREMISE1. $\forall x (\text{Player}(x) \vee \text{Referee}(x))$
{PREMISE1} Assume ✓

PREMISE2. $\forall x (\text{Player}(x) \rightarrow \text{Tall}(x))$
{PREMISE2} Assume ✓

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{PREMISE3} Assume ✓

5. $\neg \text{Tall}(a)$
{5} Assume ✓

GOAL. $\exists x \text{Referee}(x)$
FOL \vdash ✗

Step I

PREMISE1. $\forall x (\text{Player}(x) \vee \text{Referee}(x))$
{PREMISE1} Assume ✓

PREMISE2. $\forall x (\text{Player}(x) \rightarrow \text{Tall}(x))$
{PREMISE2} Assume ✓

PREMISE3. $\exists x \neg \text{Tall}(x)$
{PREMISE3} Assume ✓

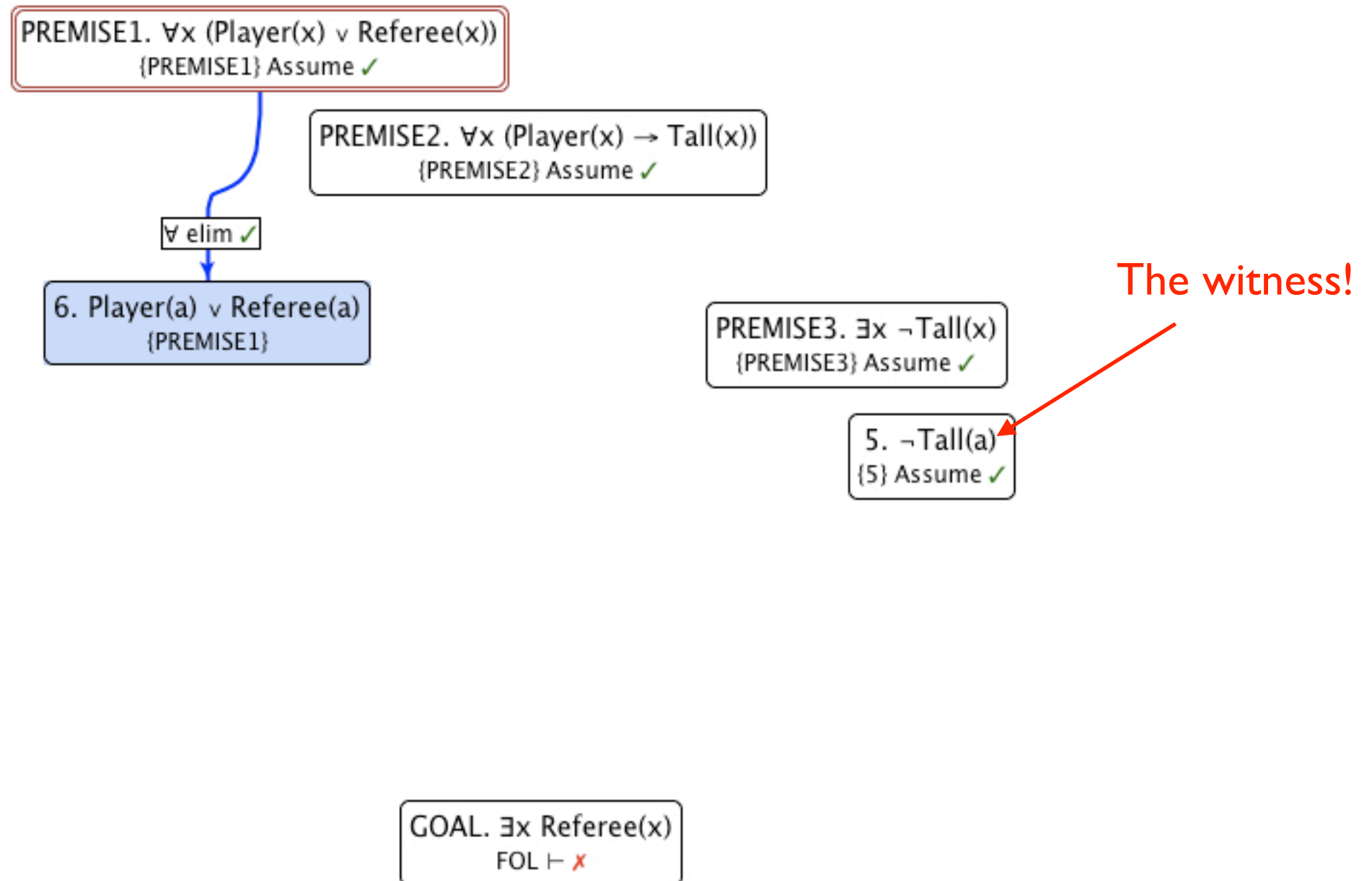
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The witness!

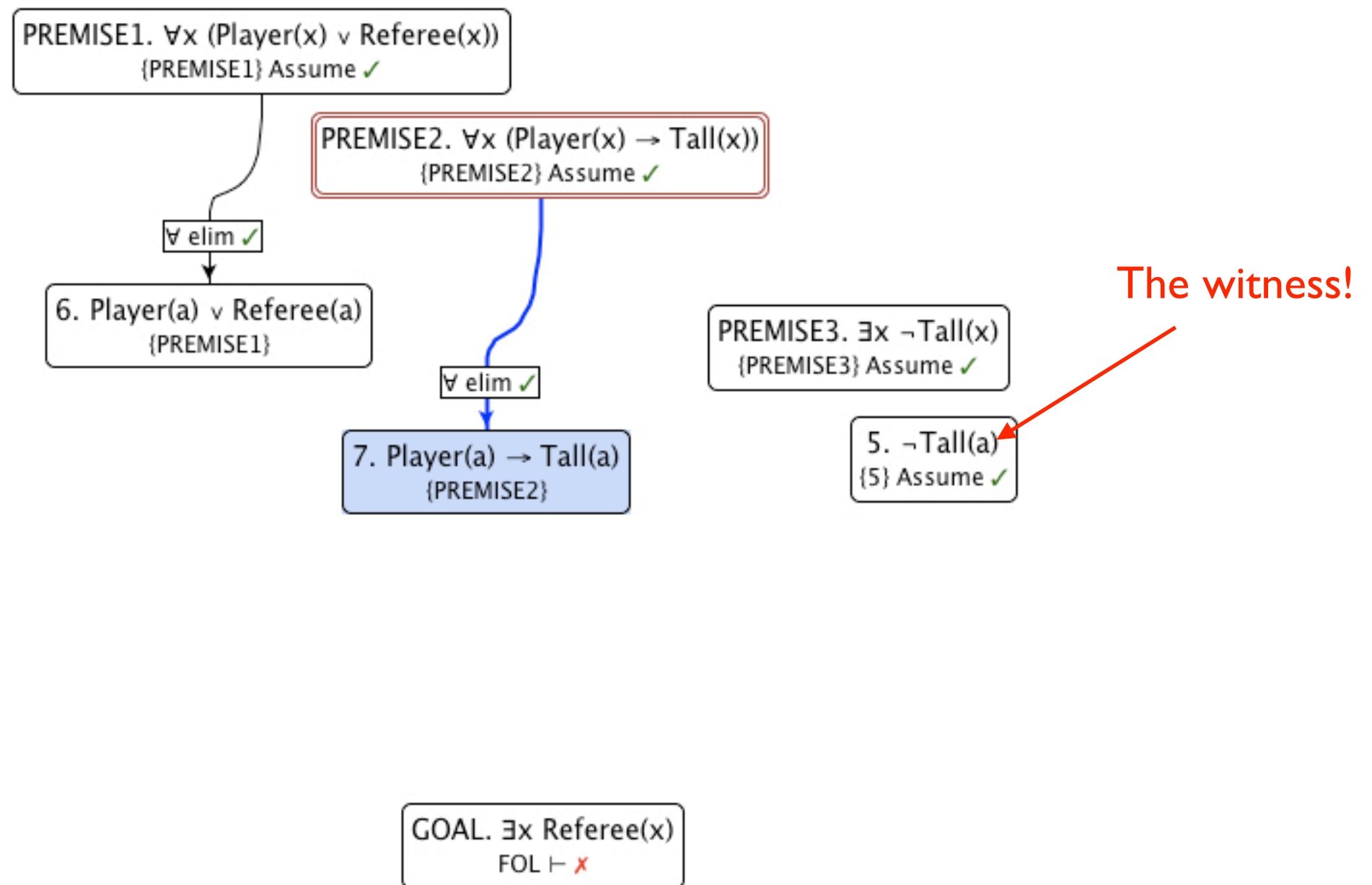


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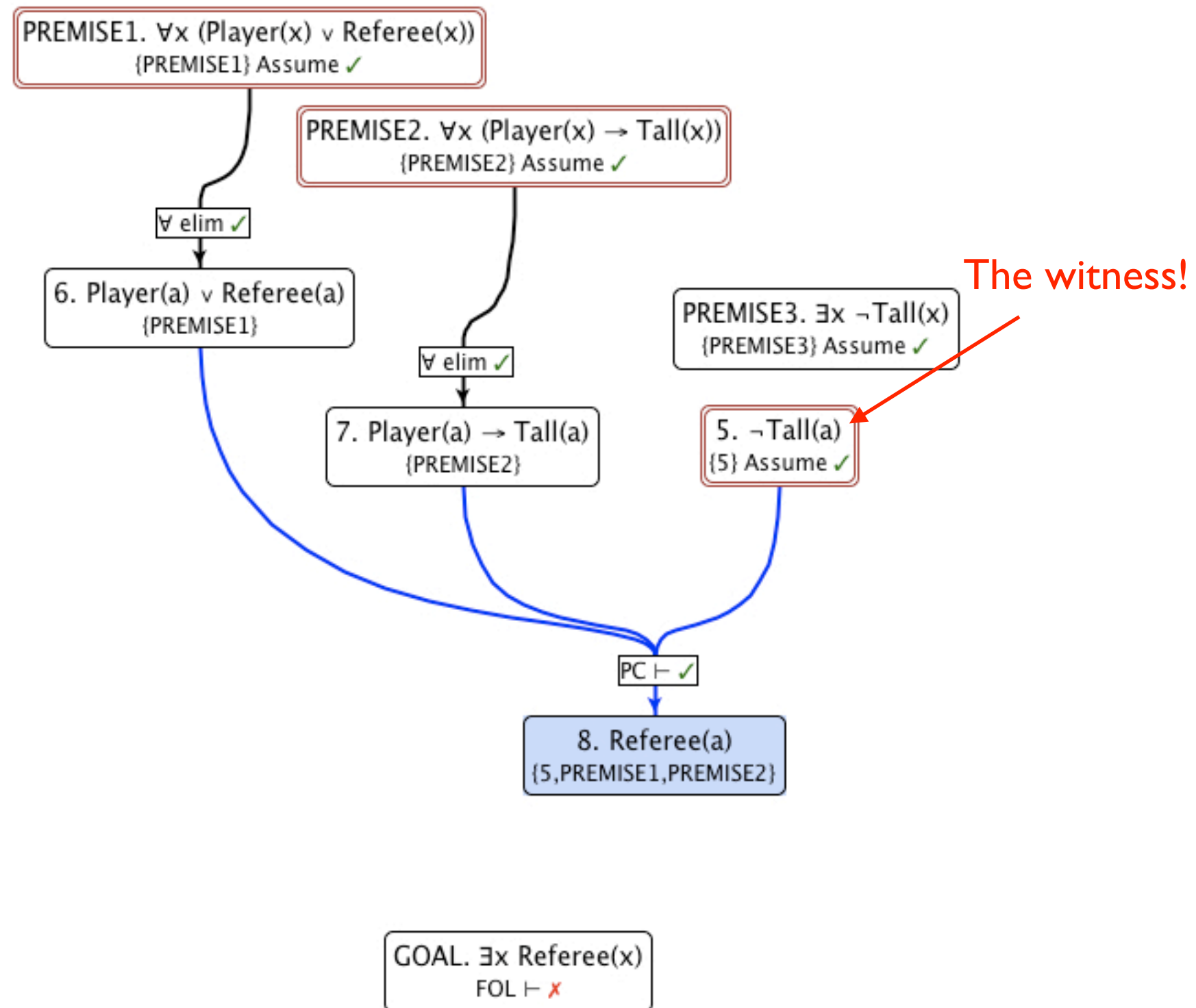
Step 2



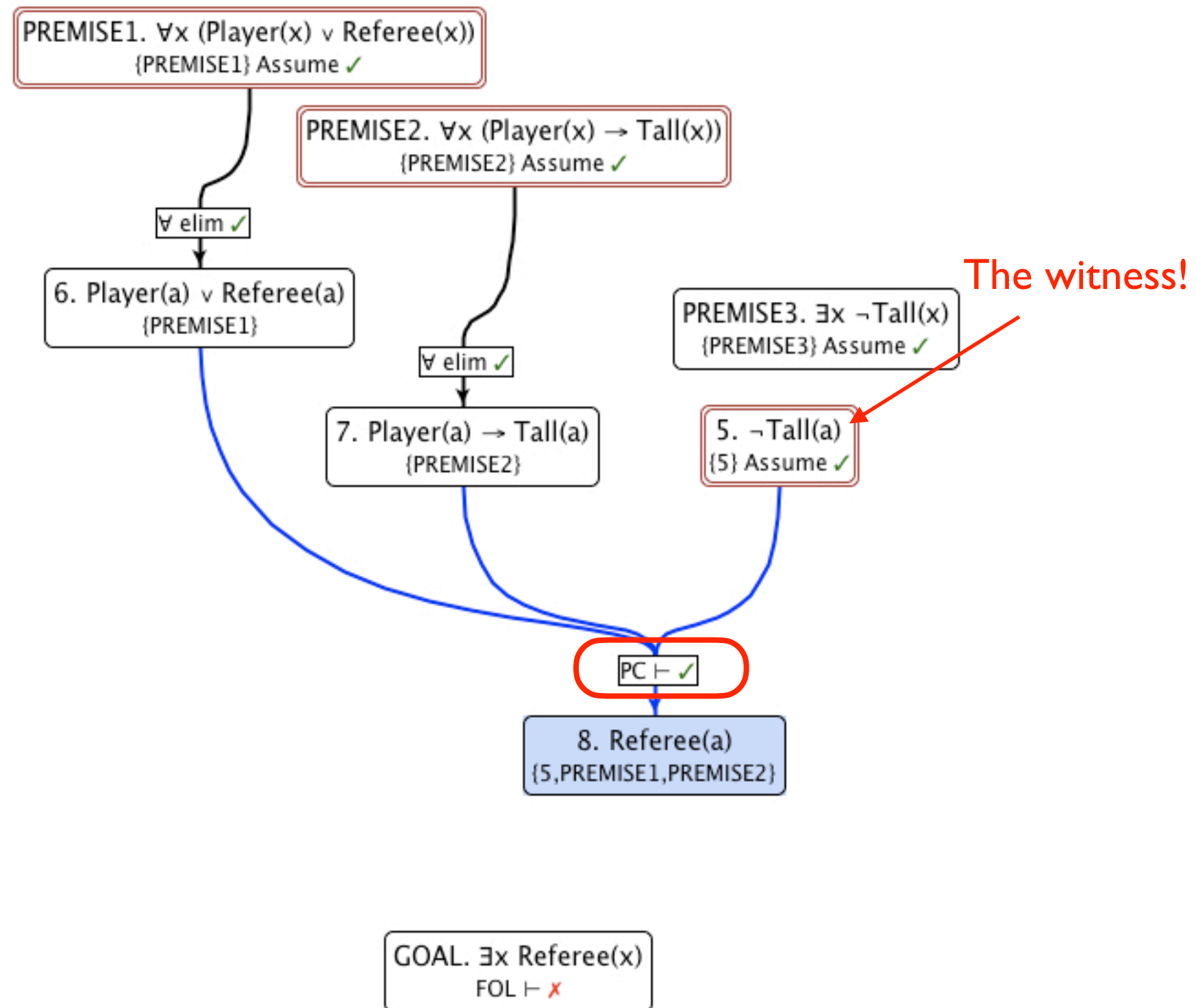
Step 3



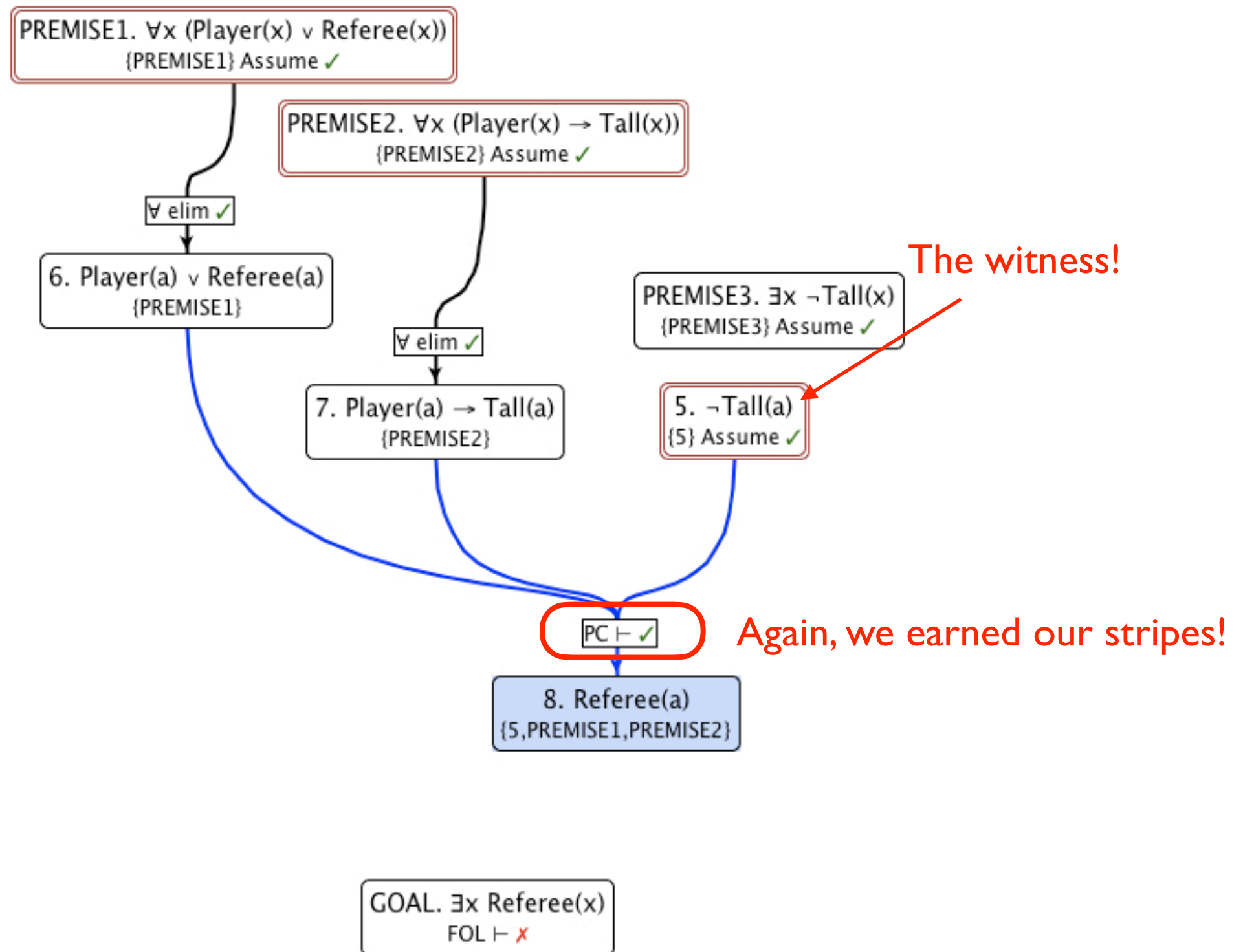
Step 4



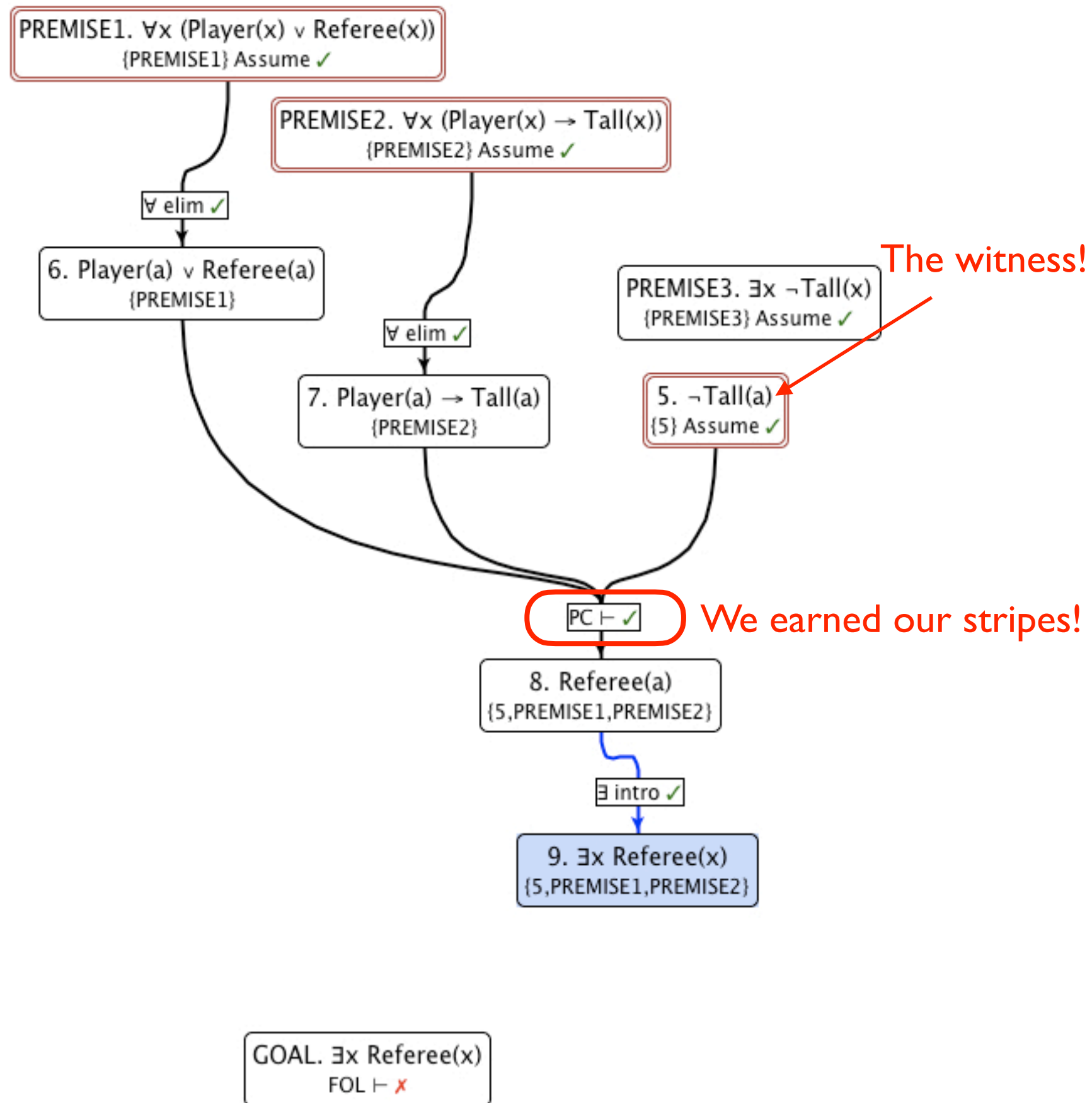
Step 4



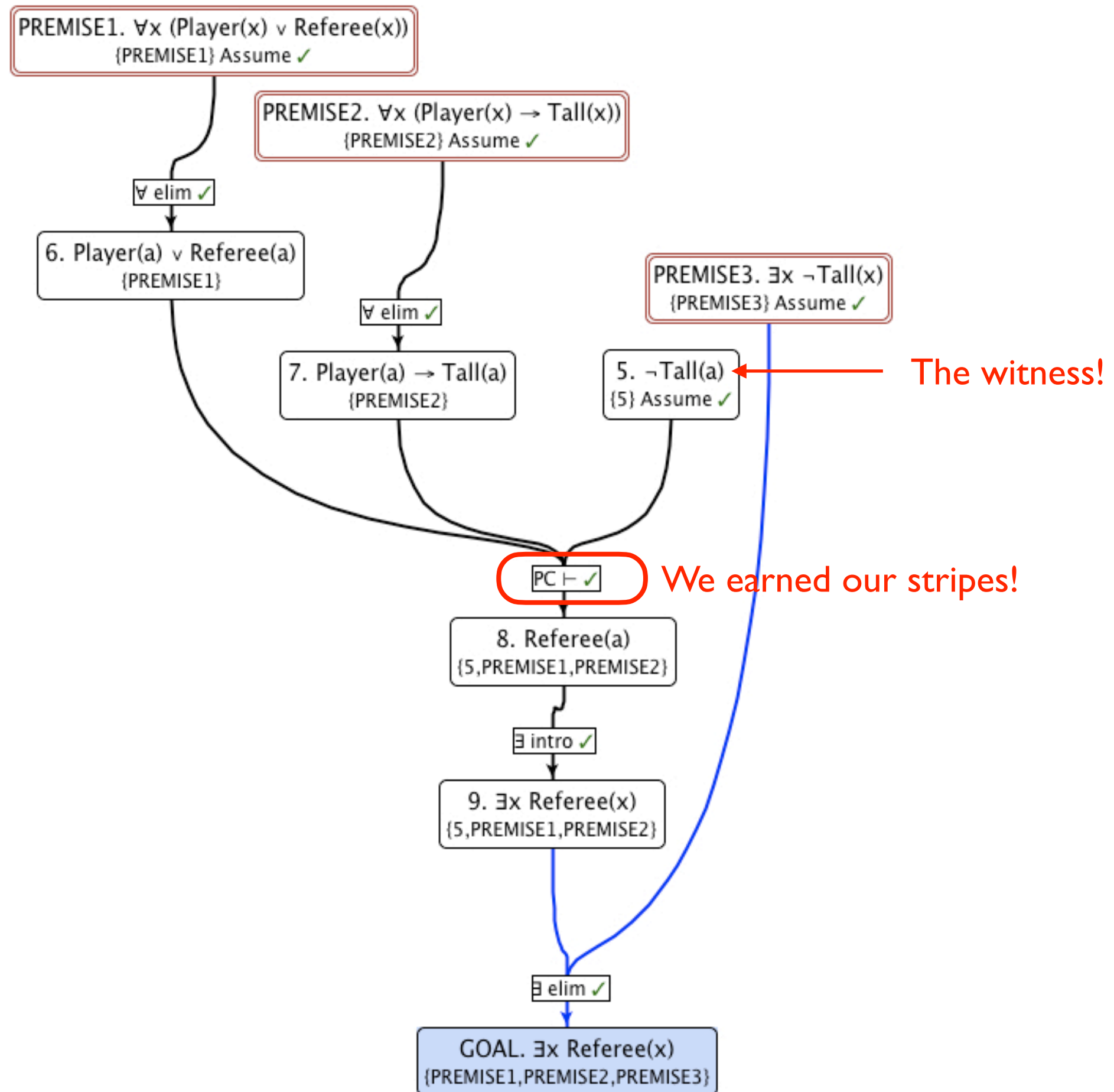
Step 4



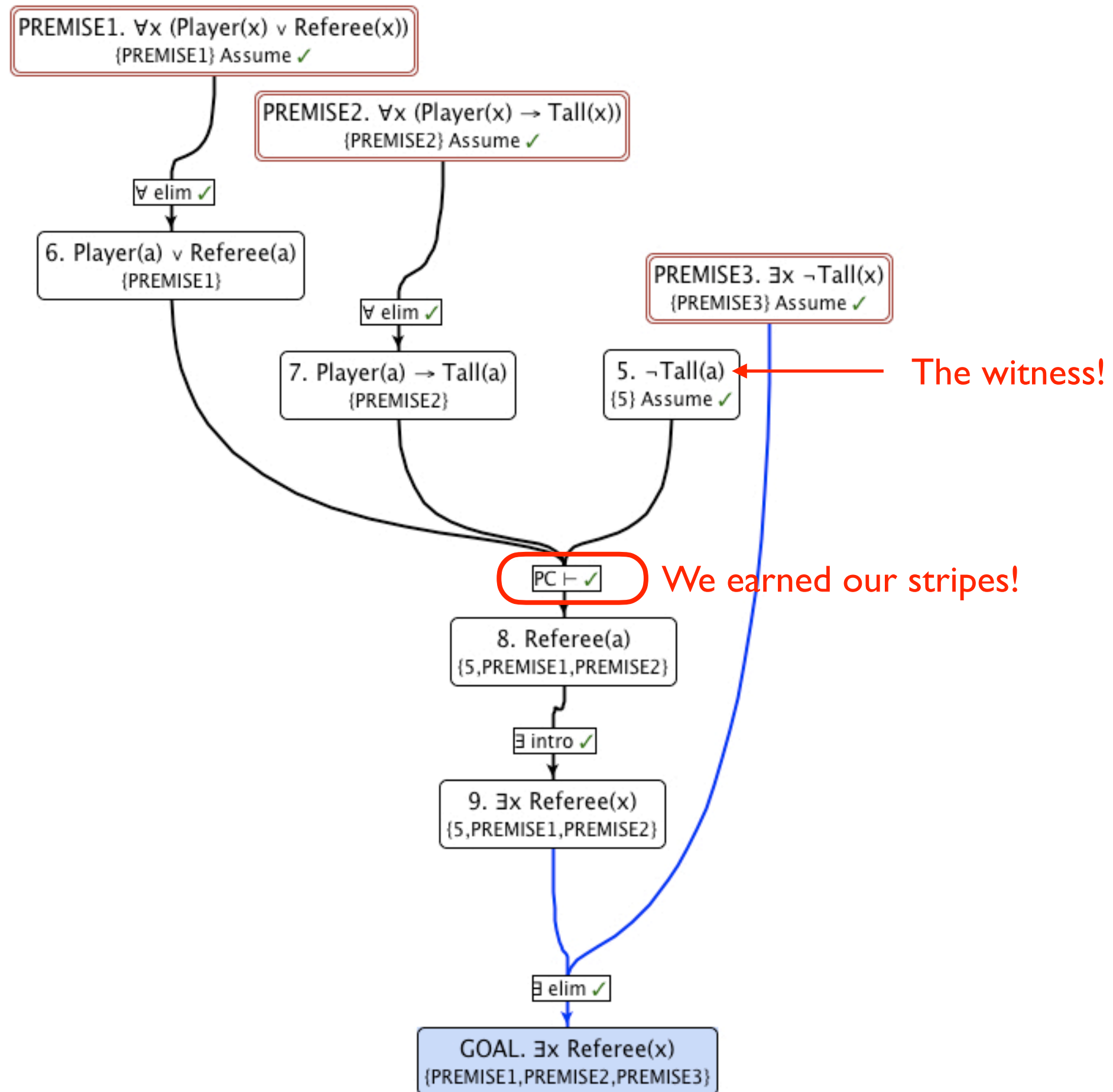
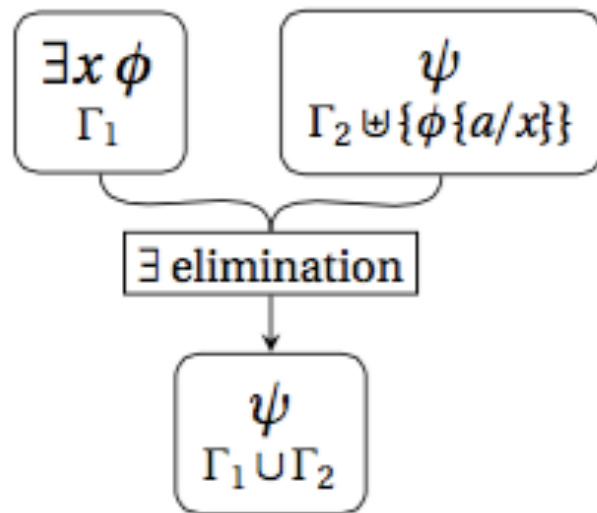
Step 5



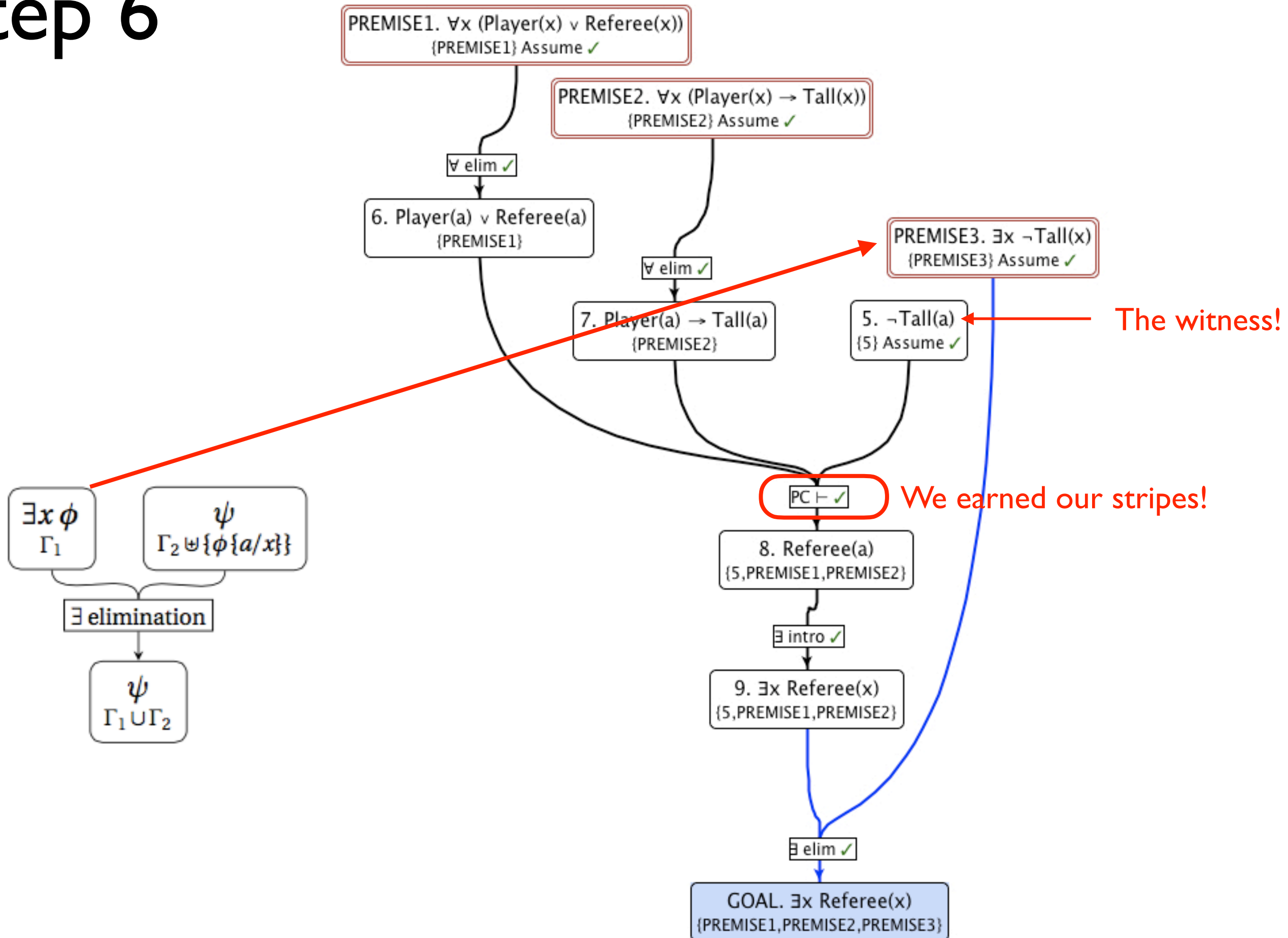
Step 6



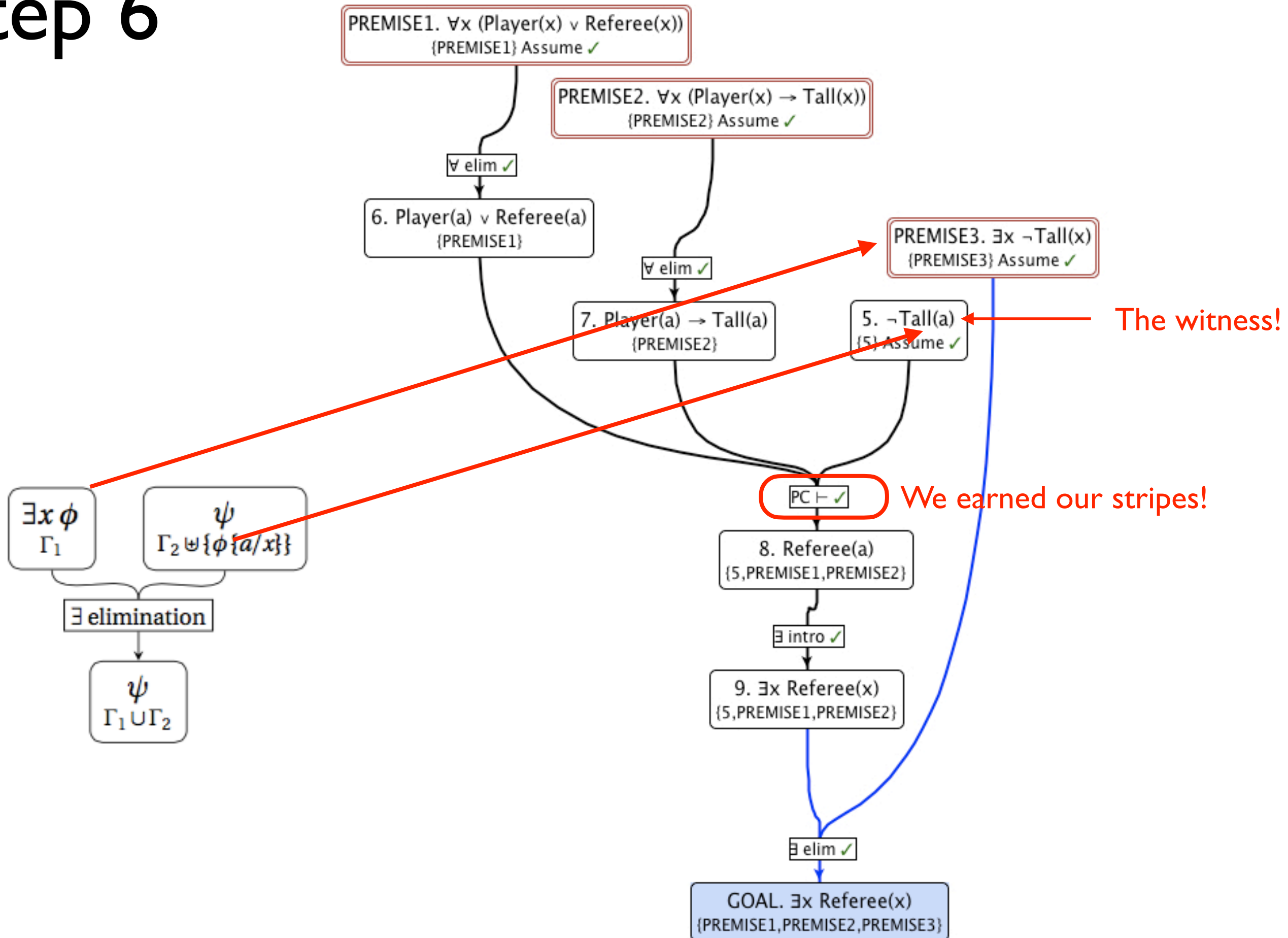
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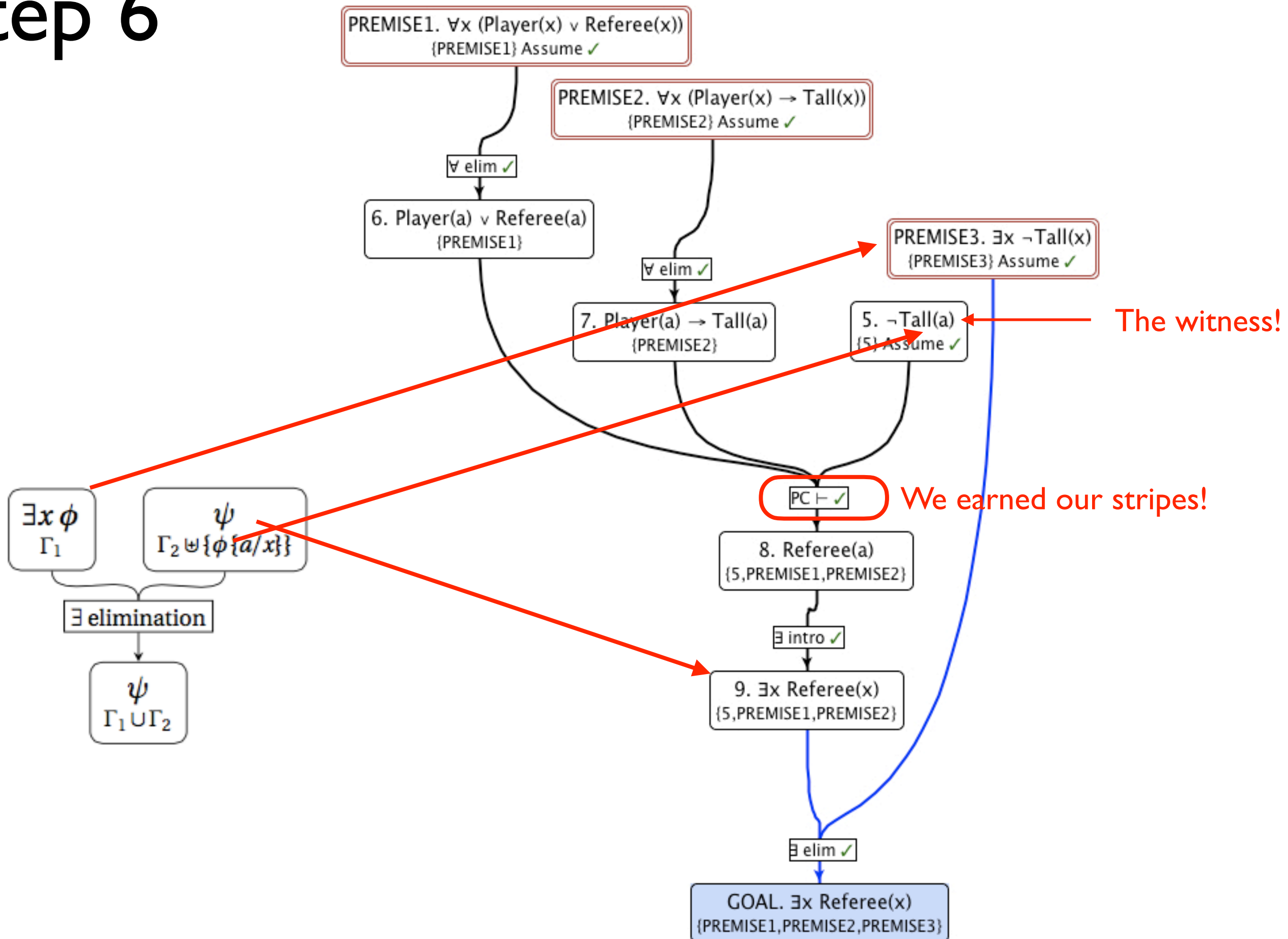
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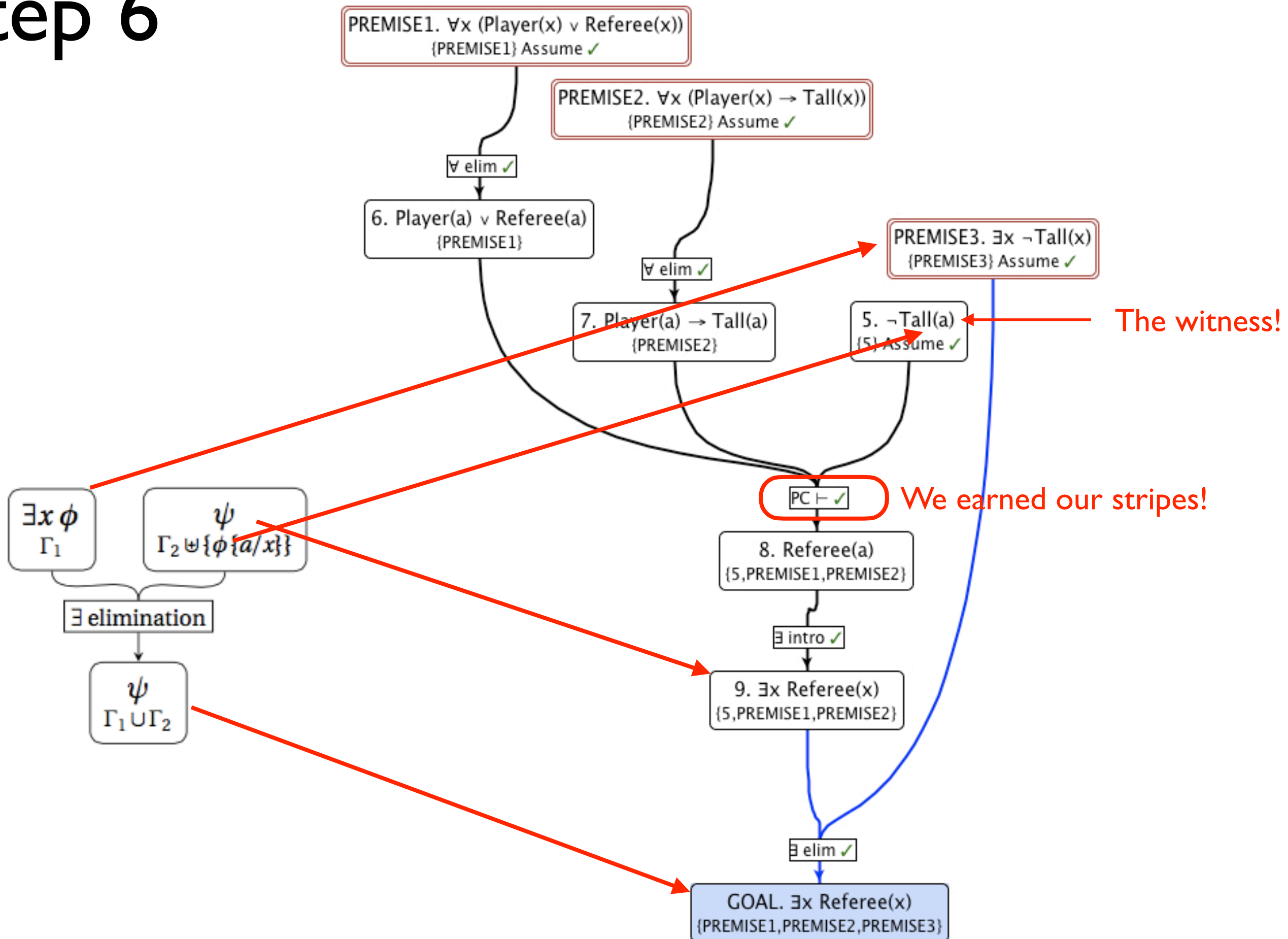
Step 6



Step 6



Step 6



$$\{\forall x(\text{Scared}(x) \leftrightarrow \text{Small}(x)), \exists x \neg \text{Scared}(x)\} \vdash \exists x \neg \text{Small}(x)$$

$$\{\exists x, y \text{Contiguous}(x, y), \forall x, y(\text{Contiguous}(x, y) \rightarrow \neg \text{SameCountry}(x, y))\} \vdash \exists x, y \neg \text{SameCountry}(x, y)$$

*Hvis du forstår det, kan
du bevise det.*