

Quantifiers; FOL I; “Proving” God’s Existence

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Intro to Logic
2/17/2022

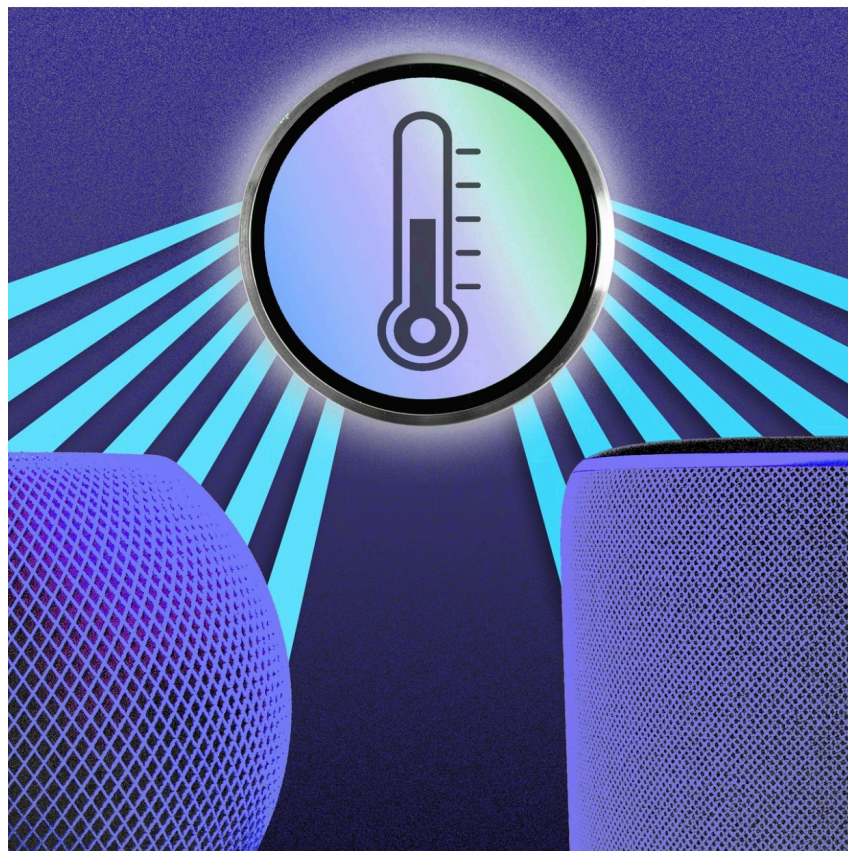


Logic-&-AI In The News

PERSONAL TECHNOLOGY: REVIEW

Why Apple, Amazon and Google Are Uniting on Smart-Home Tech: Matter Explained

The new standard, arriving this year, provides a common language so all your devices can communicate with each other



DAISY KORPICS/WALL STREET JOURNAL, ISTOCK (2); PIXELSQUID (2)

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Updated February 19, 2022 11:03 a.m. EST



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If you think about smart-home gadgets at all, you probably think about energy-saving thermostats or lights you control with an app. Most people don't worry about how they work, let alone how they might work together.

Some of tech's biggest players—Apple Inc. [AAPL -0.94% ▼](#), Alphabet Inc. [GOOGL -1.61% ▼](#)'s Google, Amazon. [AMZN -1.33% ▼](#) com Inc. and Samsung Electronics Co.—have established smart-home platforms, so your iPhone can turn off the lights or Alexa can change the thermostat without too much extra setup. But that still means shoppers must check if new products work with the tech they already have at home.

Compatibility issues and setup complexity have made people slow to go all-in with smart-home technology. A new standard, called Matter, aims to change that.

When it rolls out this year, Matter will act as a common language spoken by most new—and

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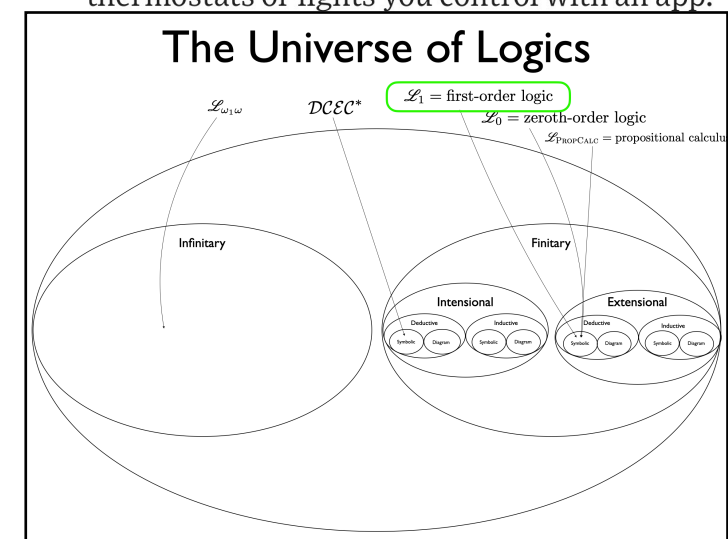
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Re Test I...

HyperGrader[®]
Required Homework
Problems:
Self-paced, yes! — but
interconnected!

BogusBiconditional

tertium_non_datur

Disj_Elim

BogusBiconditional

RipsSaysNo1

RipsSaysNo2

BogusBiconditional

tertium_non_datur

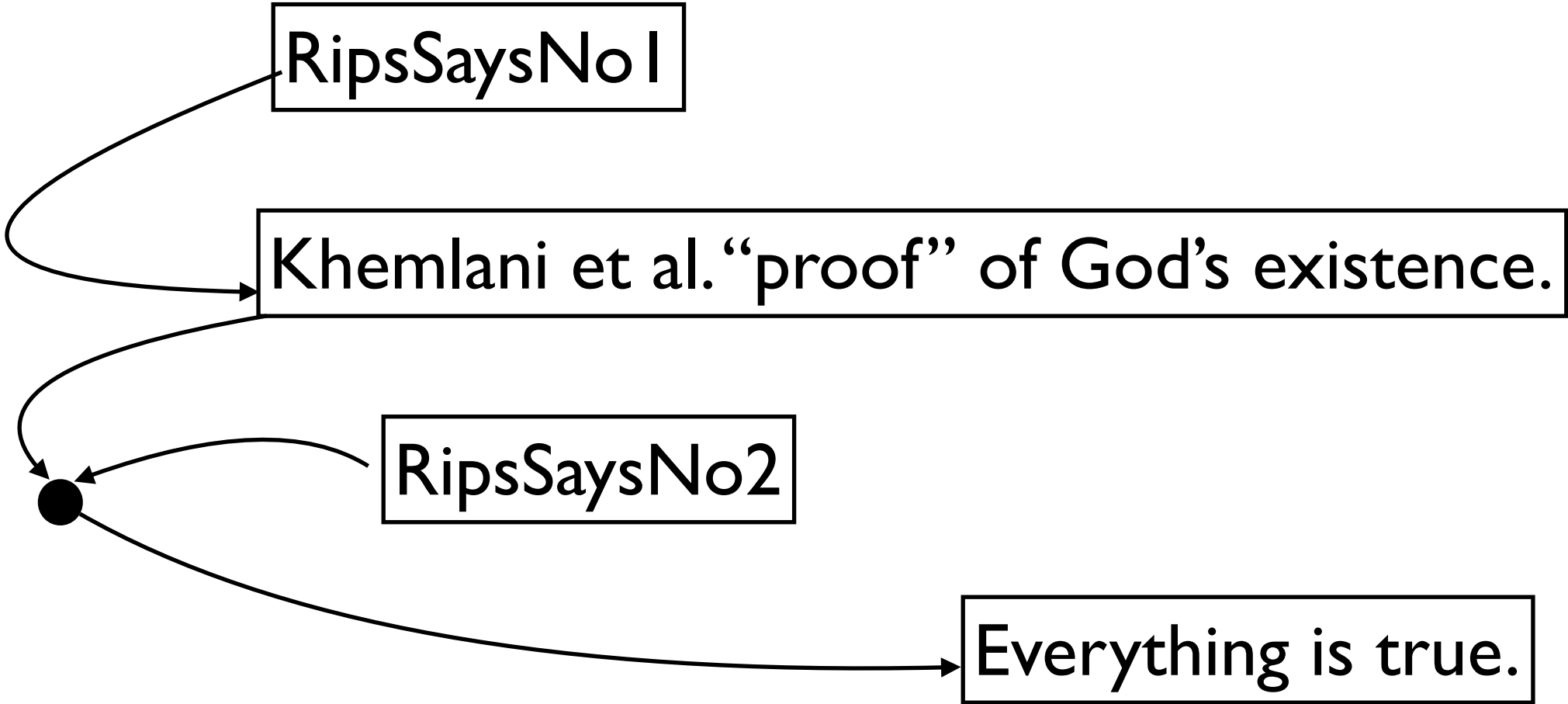
Disj_Elim

RipsSaysNo1

Khemlani et al. "proof" of God's existence.

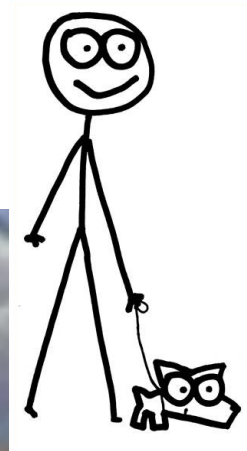
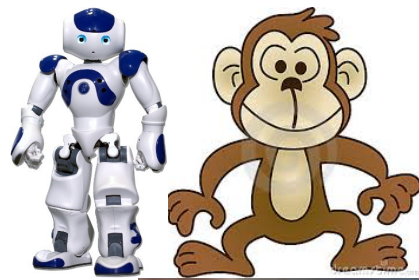
RipsSaysNo2

Everything is true.

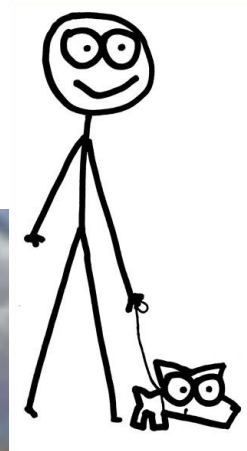
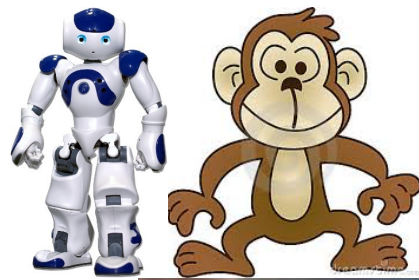


Quantifiers (etc) ...

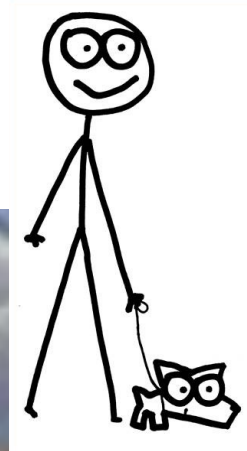
The Canyon of Discontinuity (or Darwin's Dread)



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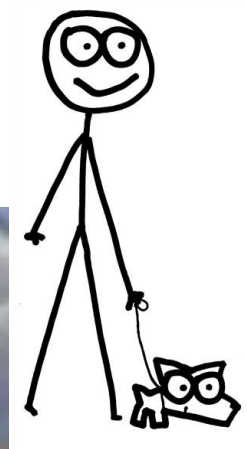


The Canyon of Discontinuity (or Darwin's Dread)



Relations and Functions!

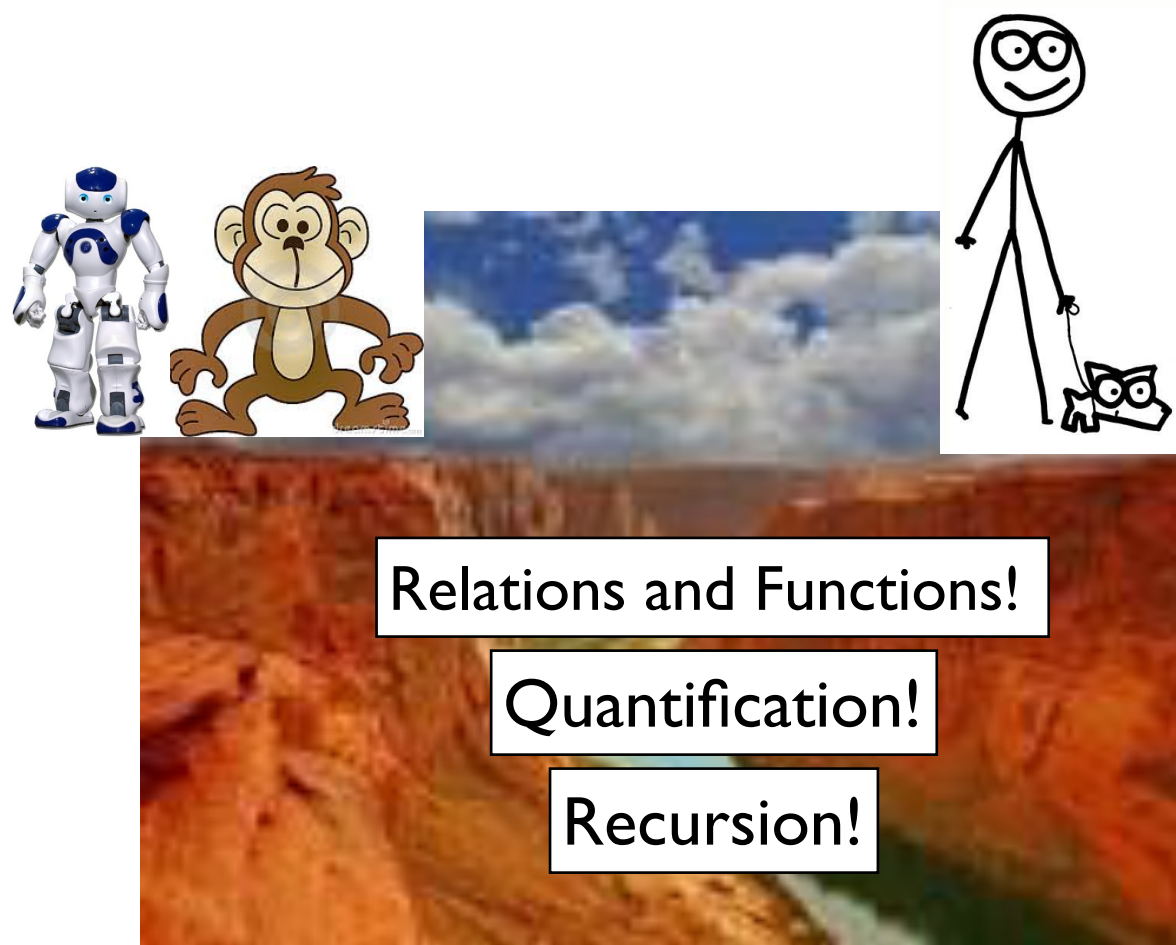
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Relations and Functions!

Quantification!

The Canyon of Discontinuity (or Darwin's Dread)



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Quantification!

Relations and Functions



Recursion!

Karkooking Problem ...

Everyone karkooks anyone who karkooks someone.

Alvin karkooks Bill.

Can you infer that everyone karkooks Bill?

ANSWER:

JUSTIFICATION:

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Quantification!

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Recursion!

ANSWER:

JUSTIFICATION:

Two Proposed Arguments; Valid?

- All mammals walk.
- Whales are mammals.
- Therefore:
- Whales walk.
- All of the Frenchmen in the room are wine-drinkers.
- Some of the wine-drinkers in the room are gourmets.
- Therefore:
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We can of course easily symbolize and settle the matter in HyperSlate[®] (PC oracle permitted now)! (Show this.). Doing so is *impossible* in the prop calc, and likewise impossible in zeroth-order logic!

Two Proposed Arguments; Valid?

- All mammals walk. $\forall x[M(x) \rightarrow W(x)]$

- Whales are mammals. $\forall x(Wh(x) \rightarrow M(x))$

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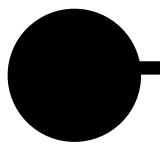
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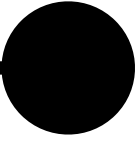
**Historically speaking
(recall) ...**



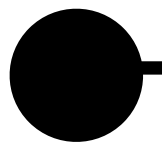
350 BC



Euclid



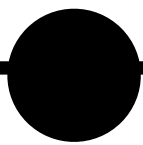
2020



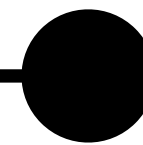
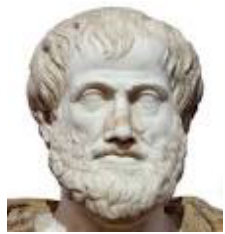
350 BC



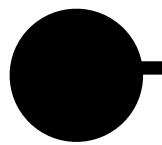
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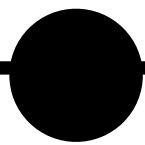
300 BC



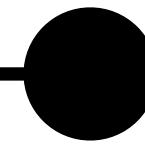
2020



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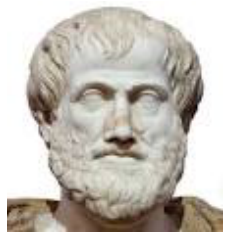
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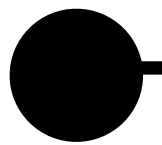
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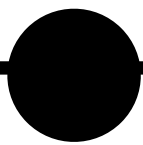
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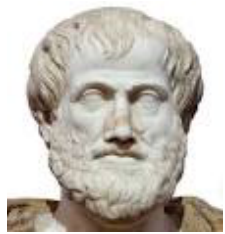
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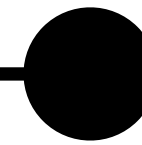
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Organon



2020

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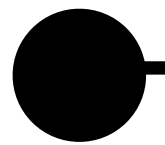
“He’s using syllogisms!”

E.g.,

All As are Bs.

All Bs are Cs.

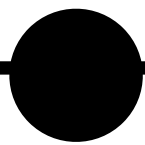
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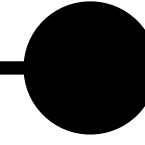
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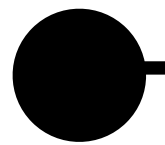
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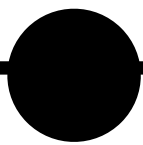
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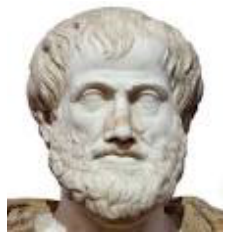
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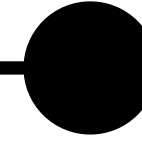


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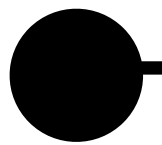
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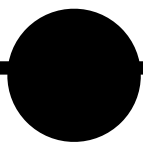
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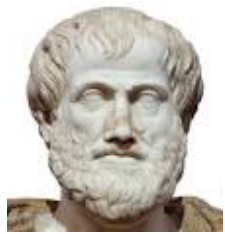
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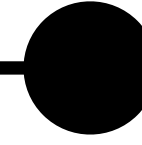


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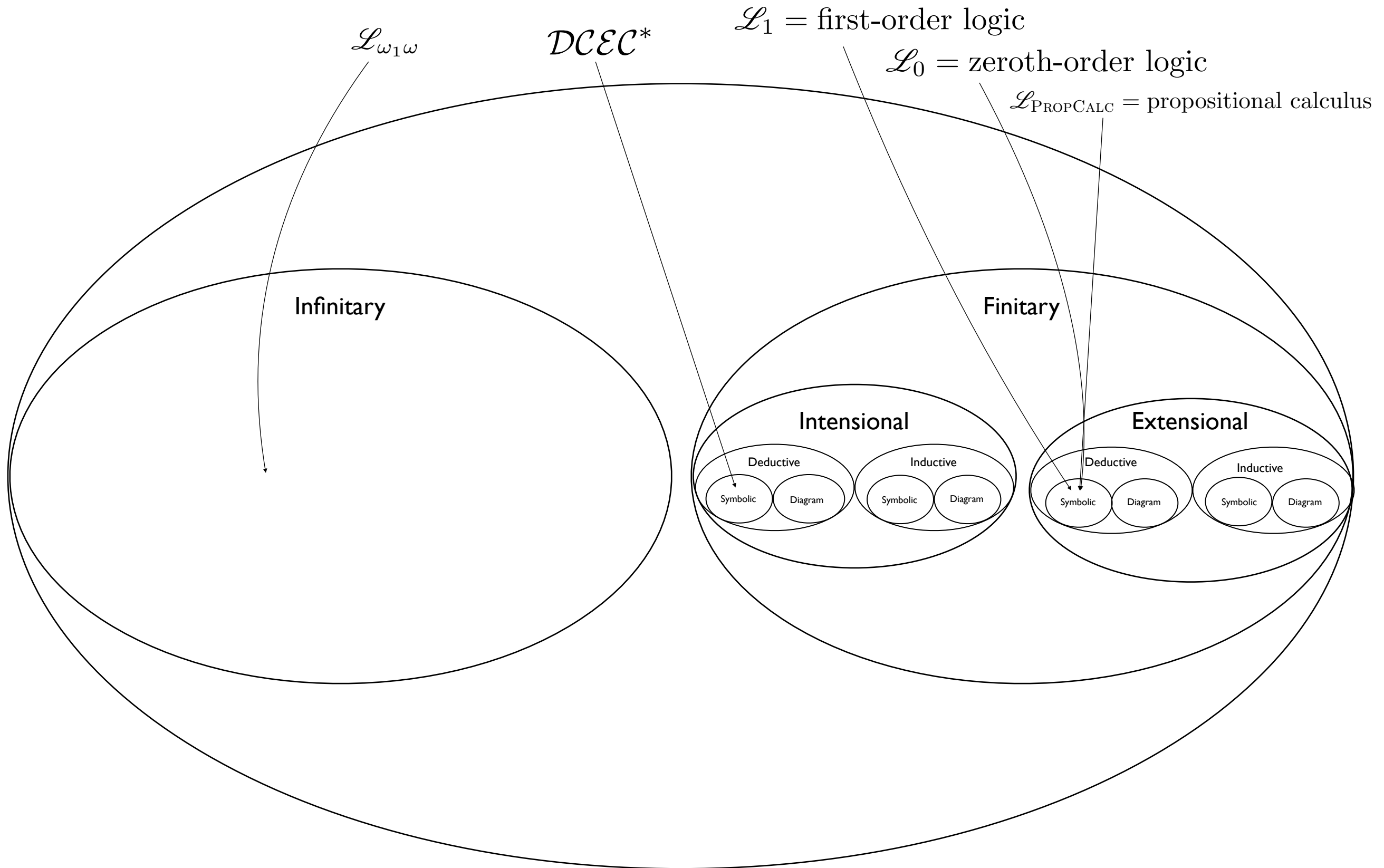
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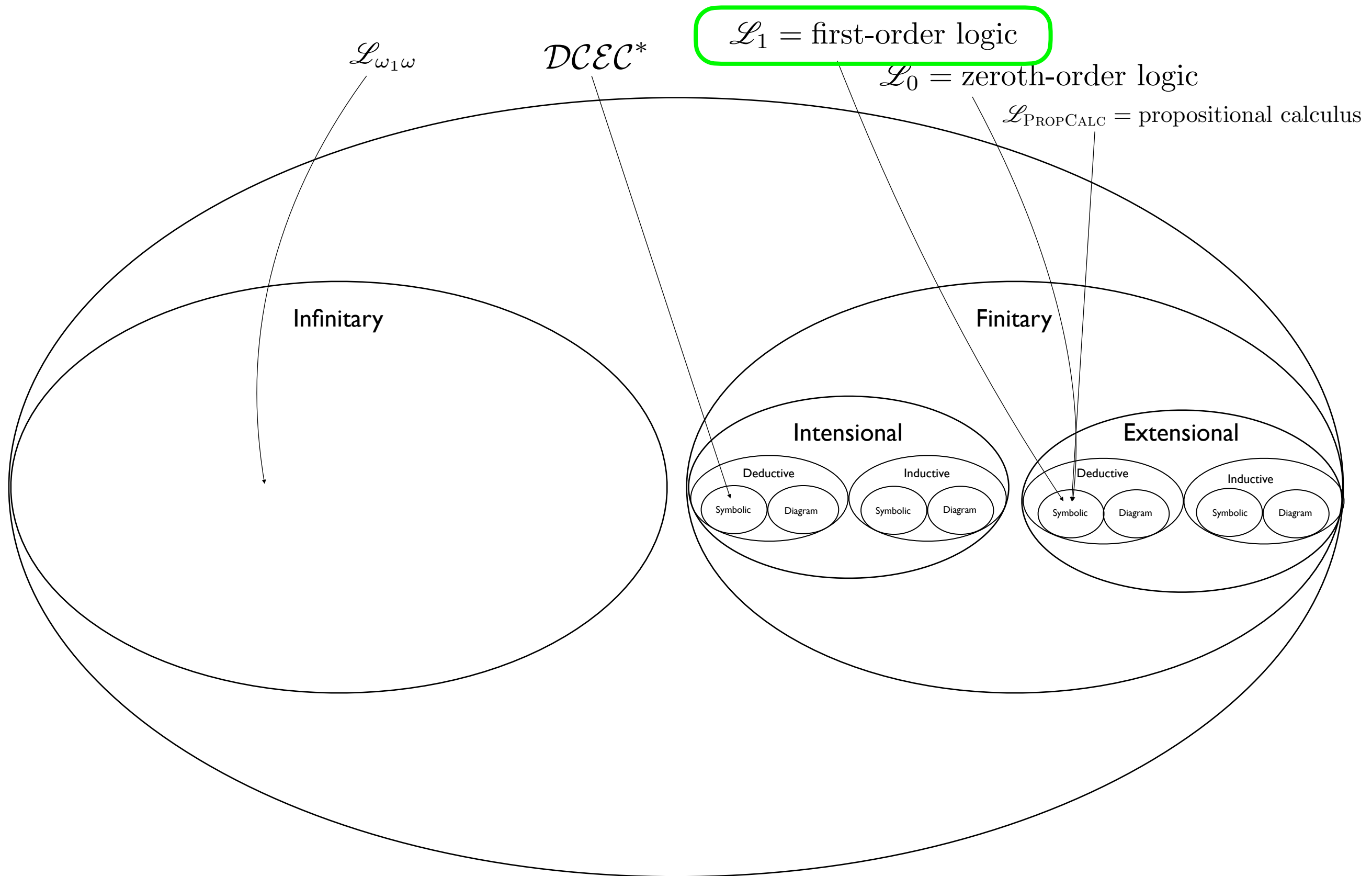


2020

The Universe of Logics



The Universe of Logics



First Two New (Easy!!) Inference Rules in FOL

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- universal elimination

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 - If everything is an R , then the particular thing a is an R .

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Scott's Version of Gödel's Proof, Verified by AI

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$\mathcal{L}_3 + \text{modal logic S5}$

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\mathcal{L}_3 + modal logic S5

First Two New (Easy!!) Inference Rules in FOL

● universal elimination

● If everything is an D , then the particular

A1 Either a property or its negation is positive, but not both:	$\forall\phi[P(\neg\phi) \leftrightarrow \neg P(\phi)]$
A2 A property necessarily implied by a positive property is positive:	$\forall\phi\forall\psi[(P(\phi) \wedge \Box\forall x[\phi(x) \rightarrow \psi(x)]) \rightarrow P(\psi)]$
T1 Positive properties are possibly exemplified:	$\forall\phi[P(\phi) \rightarrow \Diamond\exists x\phi(x)]$
D1 A <i>God-like</i> being possesses all positive properties:	$G(x) \leftrightarrow \forall\phi[P(\phi) \rightarrow \phi(x)]$
A3 The property of being God-like is positive:	$P(G)$
C Possibly, God exists:	$\Diamond\exists xG(x)$
A4 Positive properties are necessarily positive:	$\forall\phi[P(\phi) \rightarrow \Box P(\phi)]$
D2 An <i>essence</i> of an individual is a property possessed by it and necessarily implying any of its properties:	$\phi \text{ ess. } x \leftrightarrow \phi(x) \wedge \forall\psi(\psi(x) \rightarrow \Box\forall y(\phi(y) \rightarrow \psi(y)))$
T2 Being God-like is an essence of any God-like being:	$\forall x[G(x) \rightarrow G \text{ ess. } x]$
D3 <i>Necessary existence</i> of an individual is the necessary exemplification of all its essences:	$NE(x) \leftrightarrow \forall\phi[\phi \text{ ess. } x \rightarrow \Box\exists y\phi(y)]$
A5 Necessary existence is a positive property:	$P(NE)$
T3 Necessarily, God exists:	$\Box\exists xG(x)$

Scott's Version of Gödel's Proof, Verified by AI

$\mathcal{L}_3 + \text{modal logic S5}$

Benighted “Understanding” of Logic

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COGNITIVE SCIENCE
A Multidisciplinary Journal



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DOI: 10.1111/cogs.12634

Facts and Possibilities: A Model-Based Theory of Sentential Reasoning

Sangeet S. Khemlani,^a Ruth M. J. Byrne,^b Philip N. Johnson-Laird^{c,d}

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Abstract

This article presents a fundamental advance in the theory of mental models as an explanation of reasoning about facts, possibilities, and probabilities. It postulates that the meanings of compound assertions, such as conditionals (*if*) and disjunctions (*or*), unlike those in logic, refer to conjunctions of epistemic possibilities that hold in default of information to the contrary. Various factors such as general knowledge can modulate these interpretations. New information can always override sentential inferences; that is, reasoning in daily life is defeasible (or nonmonotonic). The theory is a dual process one: It distinguishes between intuitive inferences (based on system 1) and deliberative inferences (based on system 2). The article describes a computer implementation of the theory, including its two systems of reasoning, and it shows how the program simulates crucial predictions that evidence corroborates. It concludes with a discussion of how the theory contrasts with those based on logic or on probabilities.

Keywords: Deduction; Logic; Mental models; Nonmonotonicity; Reasoning; Possibility

1. Introduction

People reason about facts, possibilities, and probabilities. Psychologists have carried out many studies of factual inferences, such as:

1. If the card is an ace then it is a heart.
The card is an ace.
Therefore, the card is a heart.

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seem true a priori and those that are contingent is “an unempirical dogma of empiricism.” Not anymore. The empirical studies we have described show that individuals innocent of philosophical niceties judged that assertions can be true (or false) a priori as a result of their meaning.

In logic, if a material conditional is false then its *if*-clause is true. So a very short proof for the existence of God is sound in logic:

38. It is not the case that if God exists then atheism is correct.
Therefore, God exists.

Its premise is true, and it implies both that God exists and that atheism is not correct. It therefore follows from this conjunction that God exists. In the model theory, a conditional’s meaning is not a material implication, not a conditional probability, not a set of possible worlds, and not an inferential relation. It is instead a conjunction of possibilities, each of which is assumed in default of information to the contrary. And so the falsity of a conditional does not imply that its *if*-clause is true, which renders the “proof” in (38) invalid. Individuals judge that the following assertion is false:

39. If Sonia has pneumonia then she is healthy.

But its falsity does not imply that Sonia has pneumonia, and indeed individuals judge that it is possible that Sonia does not have pneumonia (Quelhas et al., 2016). Only one case is impossible:

Sonia has pneumonia Sonia is healthy

That is why (39) is false. The modulation algorithm we described mirrors these evaluations.

Yet a complex sort of modulation is at present beyond the program. As Byrne (1989) showed, individuals draw their own conclusion from premises, such as:

42. If she meets her friend then she will go to a play.
She meets her friend.

They infer that she will go to a play. But when the premises have a further conditional of the following sort added to them:

41. If she has enough money then she will go to a play.

reasoners tend not to make the inference (see also Byrne, Espino, & Santamaria, 1999). The additional premise reminds them of a necessary condition for going to a play: One needs money to pay for the tickets. But no premise has established this condition, and so they balk at the inference. The inference is complex, and the modulation algorithm has yet to capture it.

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