### The k-Order Ladder

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# Second-Order Logic and the k-Order Ladder ...

### FOL



# $\sqrt{FOL}$ Epistemic + FOL $_{\mathbf{B}_{d}\mathbf{B}_{v}\mathbf{B}_{d}Vv}$

# $\begin{array}{c} \checkmark \text{FOL} \\ \text{Epistemic + FOL} \text{ (for coverage of "killer" robots, later)} \\ \mathbf{B}_{d}\mathbf{B}_{v}\mathbf{B}_{d}Vv \end{array}$

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# $\sqrt{\text{FOL}}$ $\sqrt{\text{Epistemic}_{\mathbf{B}_d\mathbf{B}_v\mathbf{B}_dVv}} + \text{FOL}_{\text{(for coverage of "killer" robots, later)}}$

TOL

 $\exists X[X(j) \land \neg X(m) \land S(X)]$ 

### √ FOL

# √ Epistemic + FOL (for coverage of "killer" robots, later)

 $\mathbf{B}_d \mathbf{B}_v \mathbf{B}_d V v$ 

TOL

 $\exists X[X(j) \land \neg X(m) \land S(X)]$ 



### √ FOL

# $\sqrt{\text{Epistemic} + \text{FOL}}$ (for coverage of "killer" robots, later)

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The Contemporary Craft of Creating Characters Meets Today's Cognitive Architectures: A Case Study in Expressivity\*

Selmer Bringsjord • John Licato • Alexander Bringsjord version of 0121161500NY

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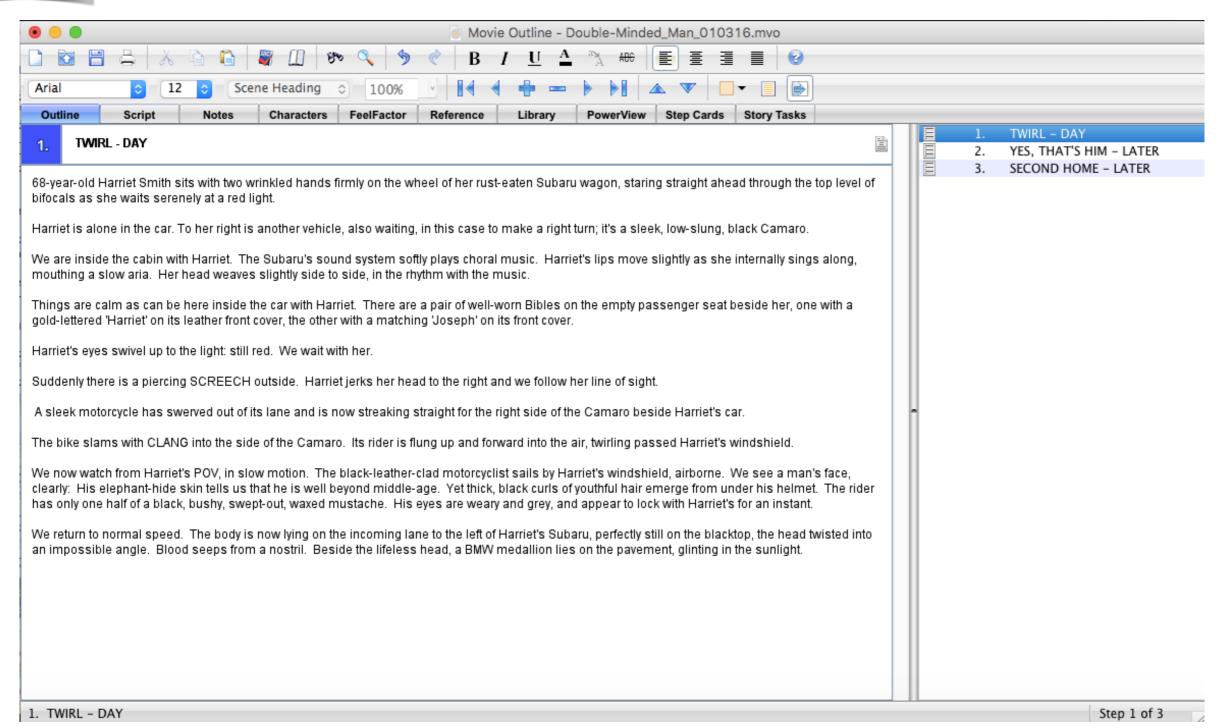
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<sup>\*</sup>We are indebted to two anonymous referees, and editor Jeremy Turner, for insightful suggestions and objections.

Any remaining deficiencies are due to our own failings.

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Double-Minded Man by

S Bringsjord & A Bringsjord

DRAFT #5 © June 30 2016

Selmer.Bringsjord@gmail.com

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### Double-Minded Man

### 1. TWIRL - DAY

68-year-old Harriet Smith sits with two wrinkled hands firmly on the wheel of her rust-eaten Subaru wagon, staring straight ahead through the top level of bifocals as she waits serenely at a red light.

Harriet is alone in the car. To her right is another vehicle, also waiting, in this case to make a right turn; it's a sleek, low-slung, black Camaro.

We are inside the cabin with Harriet. The Subaru's sound system softly plays choral music. Harriet's lips move slightly as she internally sings along, mouthing a slow aria. Her head weaves slightly side to side, in the rhythm with the music.

Things are calm as can be here inside the car with Harriet. There are a pair of well-worn Bibles on the empty passenger seat beside her, one with a gold-lettered 'Harriet' on its leather front cover, the other with a matching 'Joseph' on its front cover.

Harriet's eyes swivel up to the light; still red. We wait with her.

Suddenly there is a piercing SCREECH outside. Harriet jerks her head to the right and we follow her line of sight.

A sleek motorcycle has swerved out of its lane and is now streaking straight for the right side of the Camaro beside Harriet's car.

The bike slams with CLANG into the side of the Camaro. Its rider is flung up and forward into the air, twirling passed Harriet's windshield.

We now watch from Harriet's POV, in slow motion. The black-leather-clad motorcyclist sails by Harriet's windshield, airborne. We see a man's face, clearly: His elephant-hide skin tells us that he is well beyond middle-age. Yet thick, black curls of youthful hair emerge from under his helmet. The rider has only one half of a black, bushy, swept-out, waxed mustache. His eyes are weary and grey, and appear to lock with Harriet's for an instant.

We return to normal speed. The body is now lying on the incoming lane to the left of Harriet's Subaru, perfectly still on the blacktop, the head twisted into an impossible angle. Blood seeps from a nostril. Beside the lifeless head, a BMW medallion lies on the pavement, glinting in the sunlight.

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### $\exists X[X(joseph) \land \neg X(m(harriet, joseph)) \land Sleazy(X)]$

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 $Llama(a) \wedge Llama(b) \wedge Likes(a,b) \wedge Llama(fatherOf(a))$ 

**ZOL**  $Llama(a) \wedge Llama(b) \wedge Likes(a,b) \wedge Llama(fatherOf(a))$ 

There's some thing which is a llama and likes b (which is also a llama), and whose father is a llama too.

**ZOL**  $Llama(a) \wedge Llama(b) \wedge Likes(a,b) \wedge Llama(fatherOf(a))$ 

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Things x and y, along with the father of x, share a certain property (and x likes y).

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$$\exists x \exists y \exists R[R(x) \land R(y) \land Likes(x,y) \land R(fatherOf(x))]$$

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SOL  $\exists x \exists y \exists R[R(x) \land R(y) \land Likes(x,y) \land R(fatherOf(x))]$ 

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$$\exists x, y \; \exists R, R^2[R(x) \land R(y) \land R^2(x, y) \land Positive(R^2) \land R(fatherOf(x))]$$

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SOL 
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SOL

 $\mathcal{L}_2$ 

 $\mathscr{L}_0$ 

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 $\mathcal{L}_2$ 

 $\mathscr{L}_1$ 

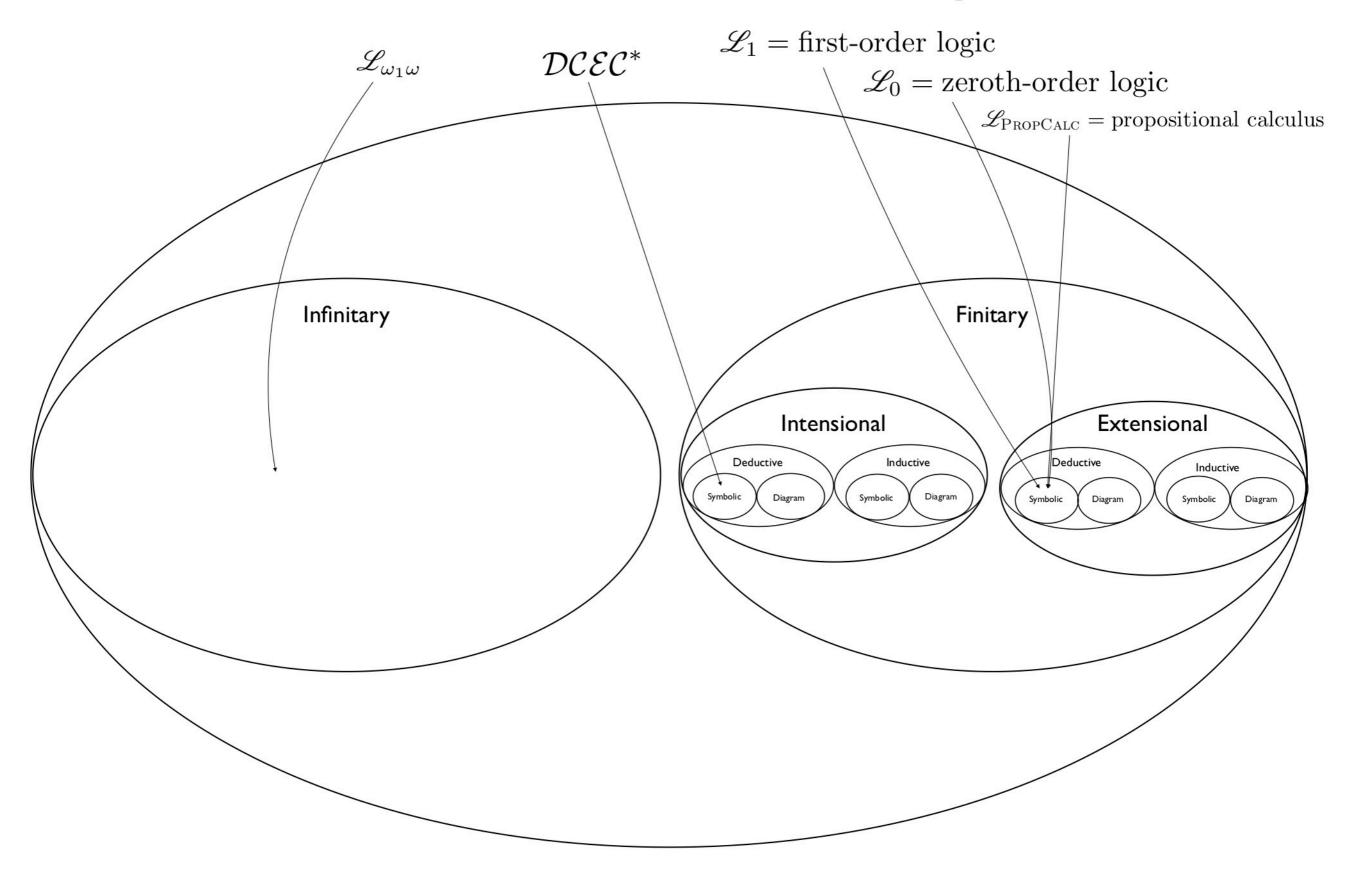
 $\mathscr{L}_0$ 

FOL 
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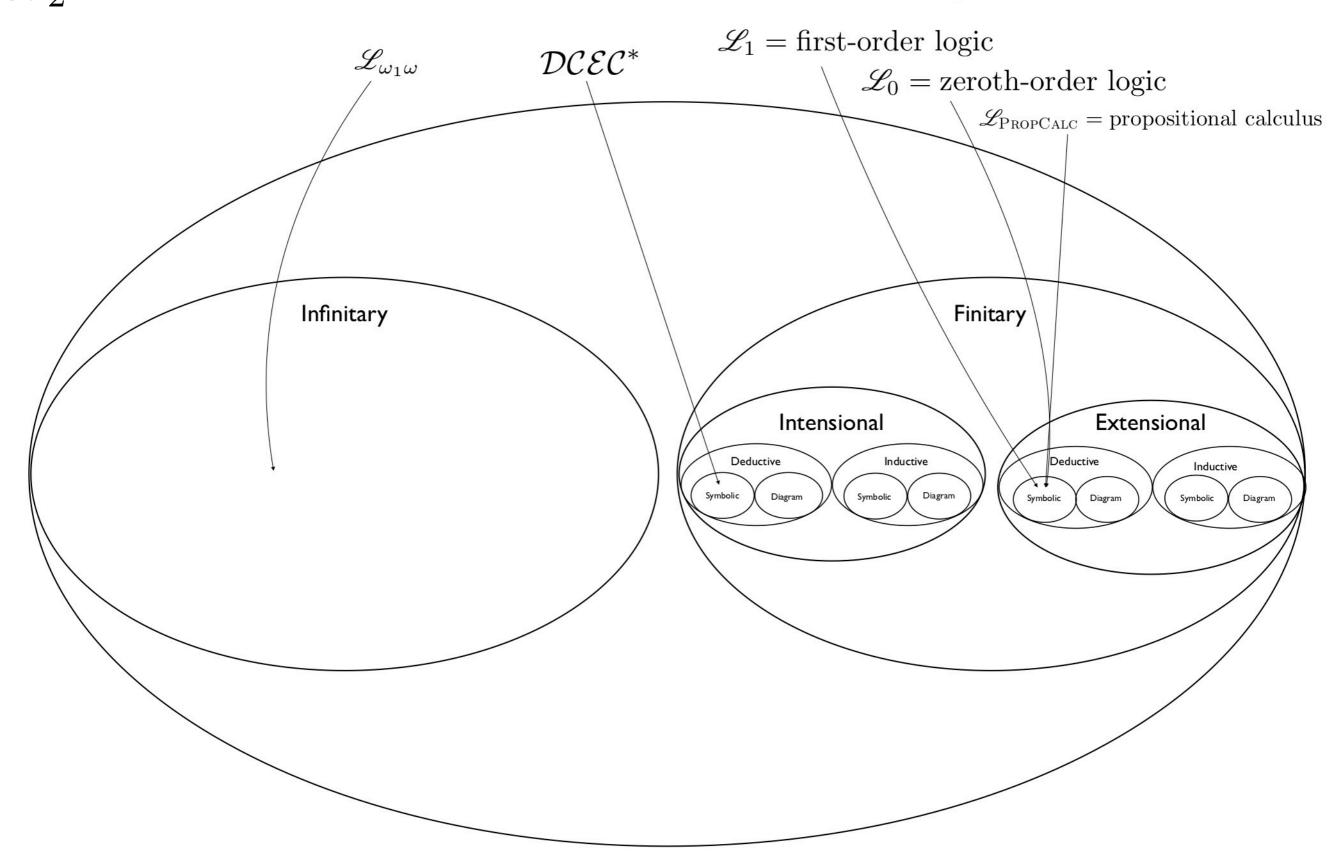
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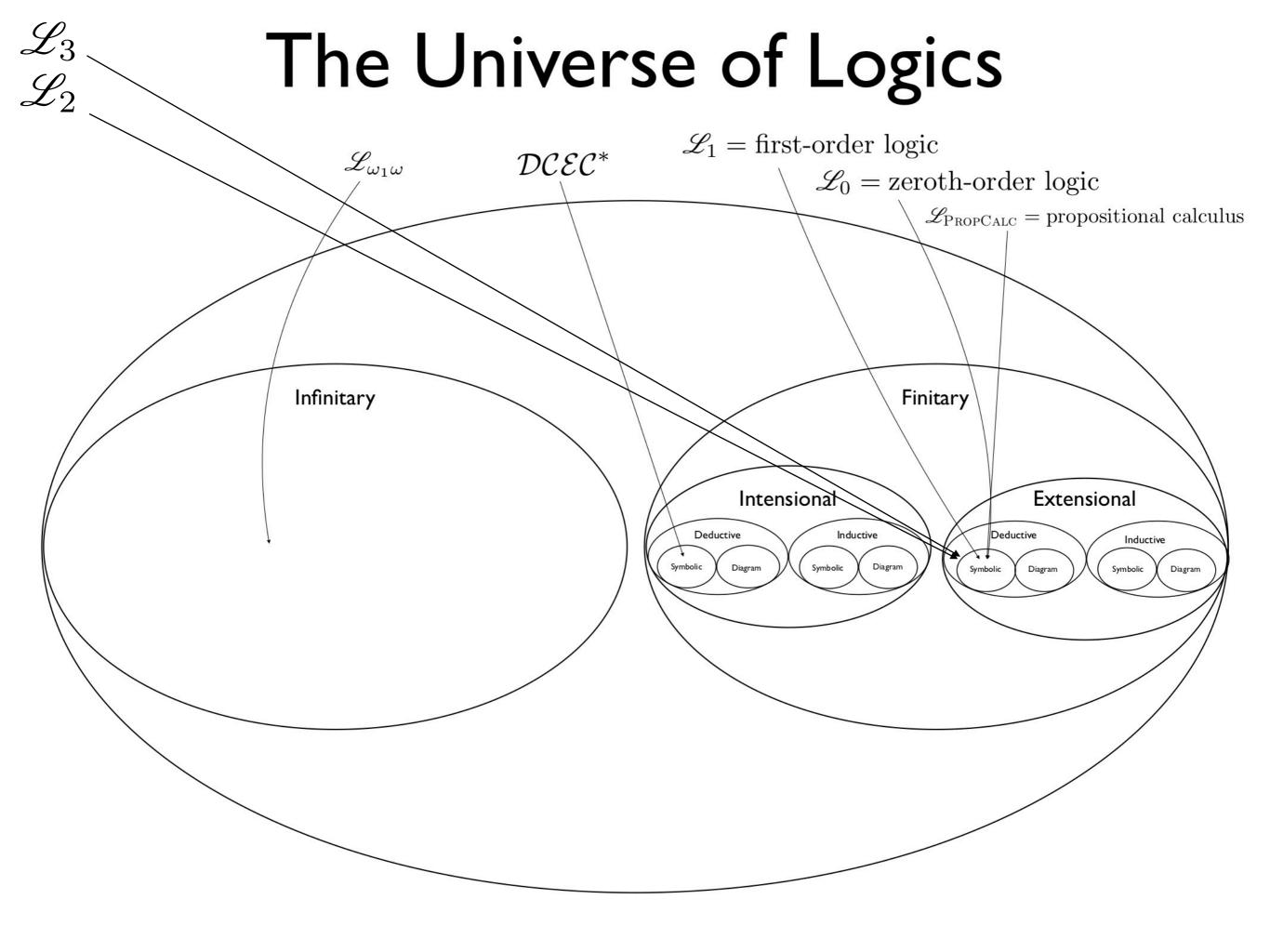
**ZOL** 
$$Llama(a) \wedge Llama(b) \wedge Likes(a,b) \wedge Llama(fatherOf(a))$$

# The Universe of Logics



# The Universe of Logics





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**TOL** 
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 $\mathcal{L}_2$ 

 $\mathscr{L}_1$ 

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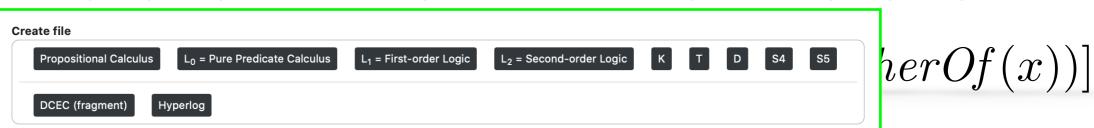
TOL

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 $\mathscr{L}_3$ 

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SOL L



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FOL

 $\mathscr{L}_1$ 

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ZOL

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 $\mathscr{L}_0$ 

•

TOL

 $\exists x, y \; \exists R, R^2[R(x) \land R(y) \land R^2(x, y) \land Peritive(R^2) \land R(fatherOf(x))]$ 

 $\mathcal{L}_3$ 

Things x and y, along with the father of x, share a certain property; and,  $x R^2s y$ , where x = x + y + y = 0 a positive property.

SOL L Propositional Calculus L<sub>0</sub> = Pure Predicate Calculus L<sub>1</sub> = First-order Logic L<sub>2</sub> = Second-order Logic K T D S4 S5

DCEC (fragment) Hyperlog

[nerOf(x))]

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FOL

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