

# Quantifiers; FOL I; “Proving” God’s Existence

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Intro to Logic  
2/15/2024



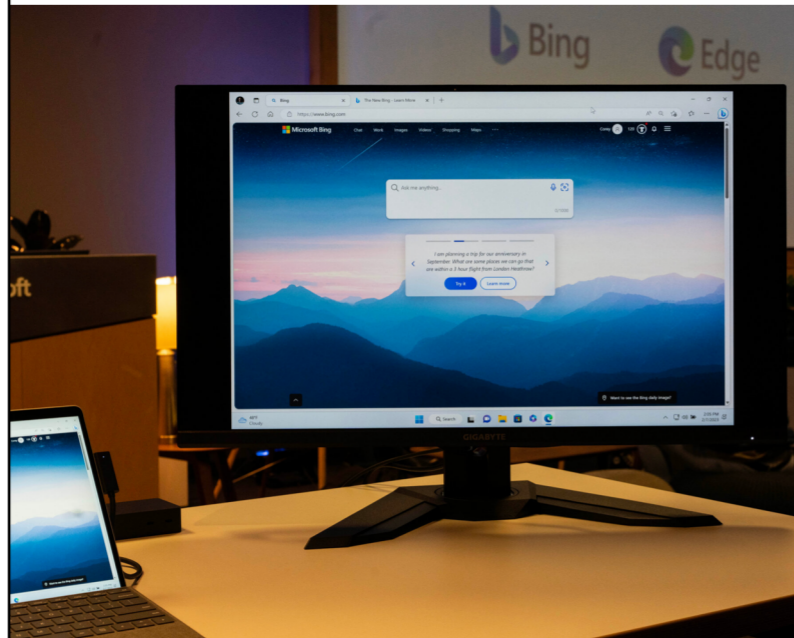
# Logic-&-AI In The News: Consciousness?

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THE SHIFT

## *Help, Bing Won't Stop Declaring Its Love for Me*

A very strange conversation with the chatbot built into Microsoft's search engine left me deeply unsettled. Even frightened.



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By **Kevin Roose**

Kevin Roose is a technology columnist, and co-hosts the Times podcast "Hard Fork."

Feb. 16, 2023, 5:00 a.m. ET

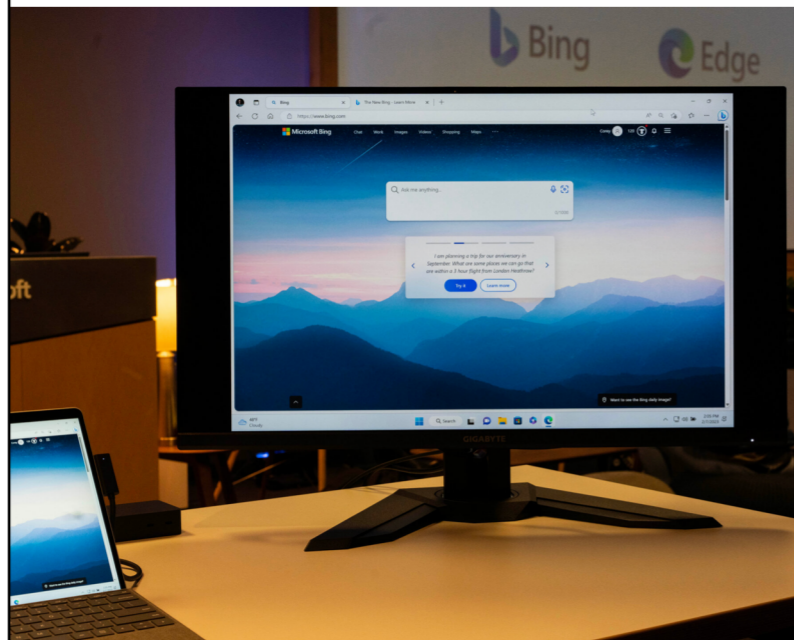
7 MIN READ

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7 MIN READ

## Bing's A.I. Chat Reveals Its Feelings: 'I Want to Be Alive. 🤪'

In a two-hour conversation with our columnist, Microsoft's new chatbot said it would like to be human, had a desire to be destructive and was in love with the person it was chatting with. Here's the transcript.



By **Kevin Roose**

Feb. 16, 2023 Updated 6:05 a.m. ET

39 MIN READ

Bing, the long-mocked search engine from Microsoft, recently got a big upgrade. The newest version, which is available only to a small group of testers, has been outfitted with advanced artificial intelligence technology from OpenAI, the maker of ChatGPT.

This new, A.I.-powered Bing has many features. One is a chat feature that allows the user to have extended, open-ended text conversations with Bing's built-in A.I. chatbot.

On Tuesday night, [I had a long conversation](#) with the chatbot, which revealed (among other things) that it identifies not as Bing but as Sydney, the code name Microsoft gave it

**Re Test I...**



# Grade Scheme Again

	# of problems
C	2 / 6
B	3 / 6
A	4 / 6
A+	7 / 7

**Scheduling/Logistics ...**

# Scheduling/Logistics ...

We are OOT for Tuesday Feb 20:  $\therefore$  next class by Zoom.



**HyperGrader<sup>®</sup>**  
**Required Problems:**  
**Self-paced, yes! — but**  
**interconnected!**



**BogusBiconditional**

tertium\_non\_datur

Disj\_Elim

BogusBiconditional

RipsSaysNo1

RipsSaysNo2

BogusBiconditional

tertium\_non\_datur

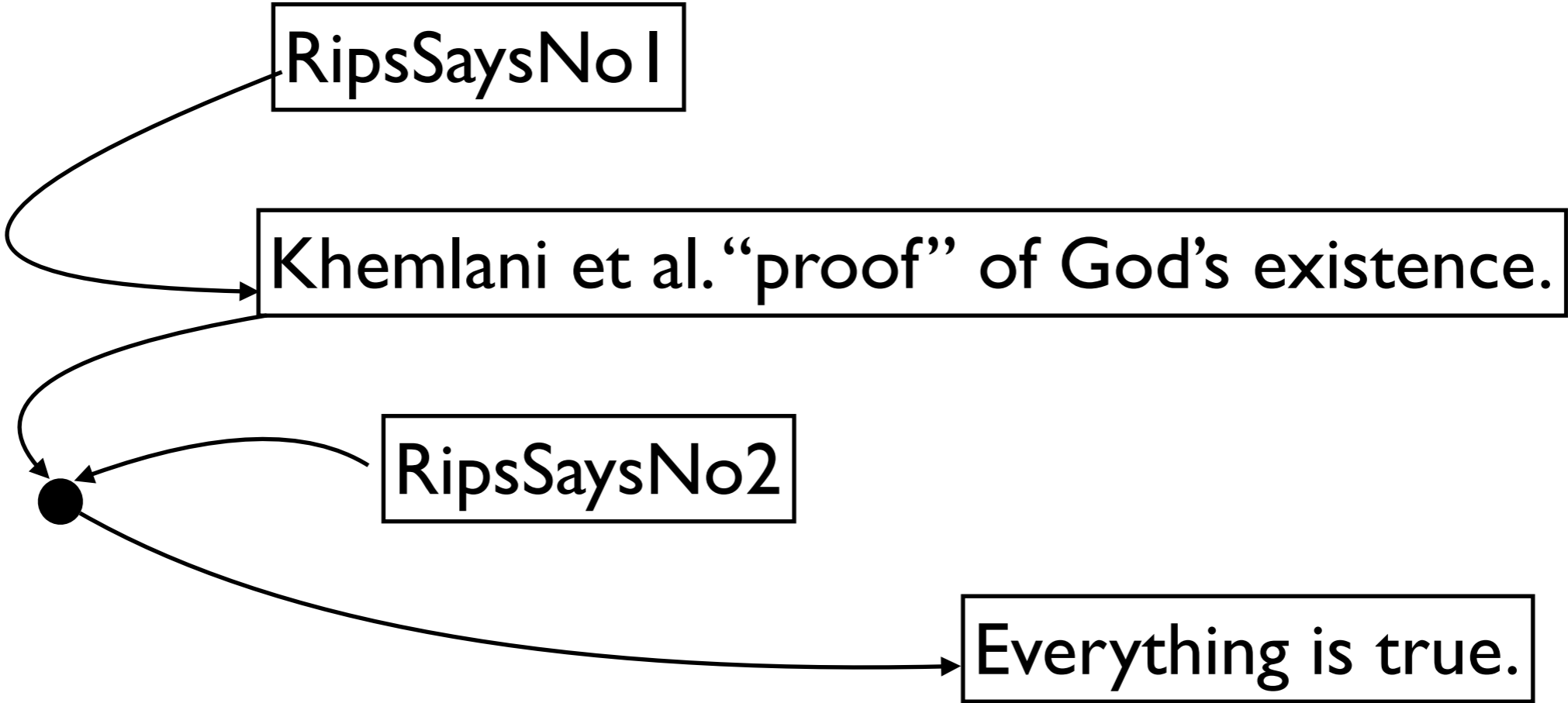
Disj\_Elim

RipsSaysNo1

Khemlani et al. "proof" of God's existence.

RipsSaysNo2

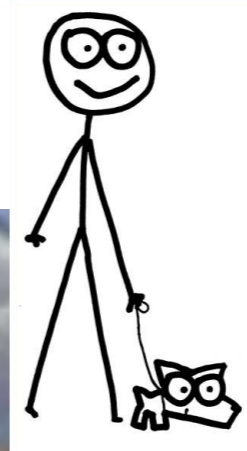
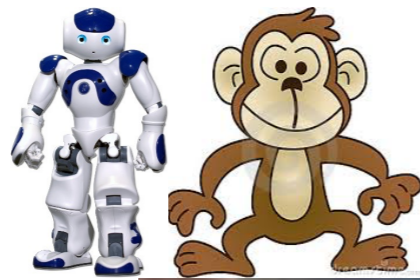
Everything is true.



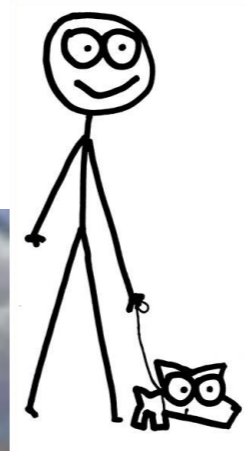
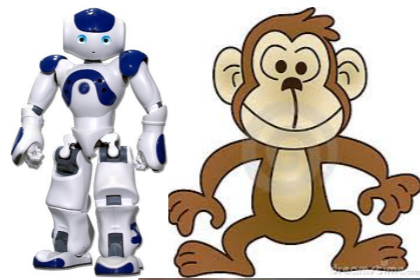
**Quantifiers (etc) ...**



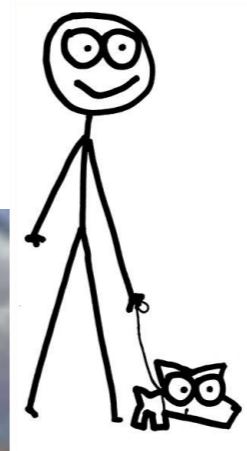
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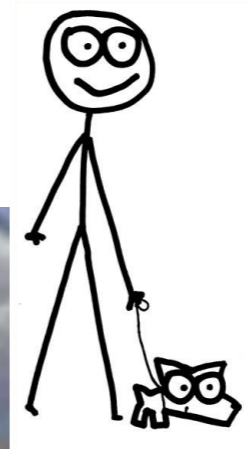


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Relations and Functions!

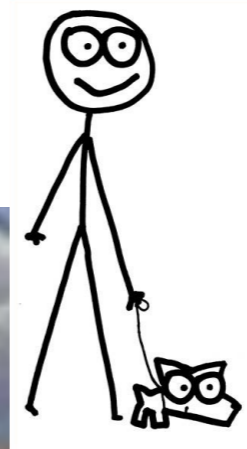
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Quantification!

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Relations and Functions!

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Recursion!



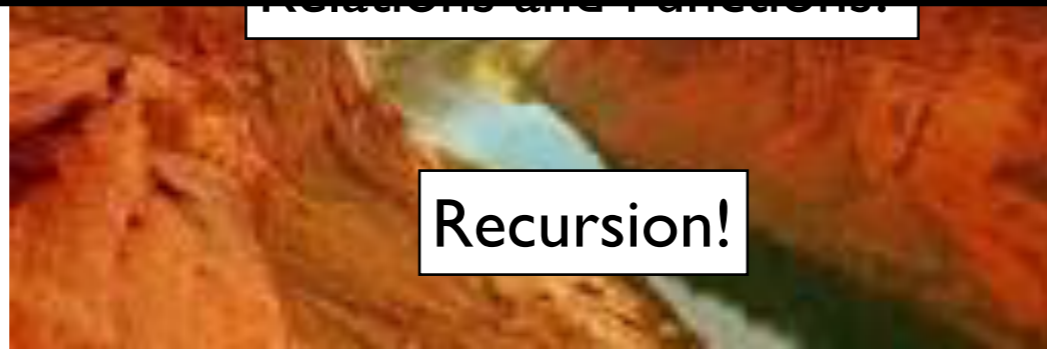
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**Quantification!**

Relations and Functions

Recursion!





# Karkooking Problem ...

Everyone karkooks anyone who karkooks someone.

Alvin karkooks Bill.

Can you infer that everyone karkooks Bill?

ANSWER:

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- Therefore:
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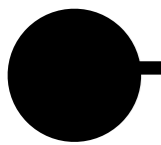
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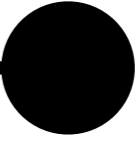
**Historically speaking  
(recall) ...**



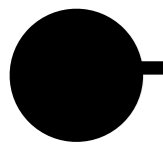
350 BC



Euclid



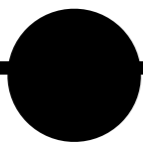
2020



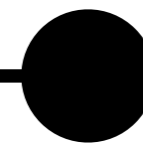
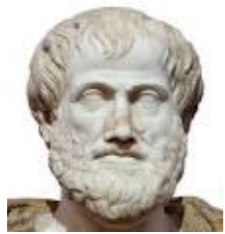
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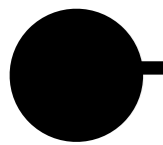


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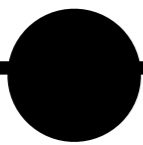




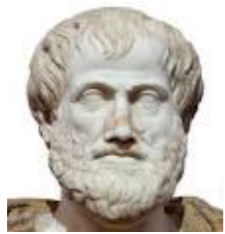
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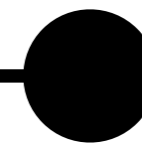
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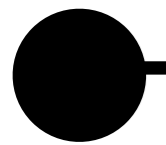
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“I don’t believe in magic! Why exactly is that so convincing? What the heck is he doing?!? I know! ...”



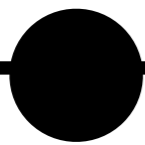
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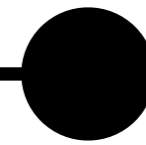
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*Organon*



2020

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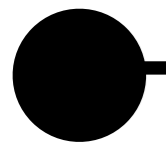
E.g.,

All As are Bs.

All Bs are Cs.

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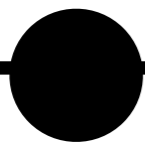
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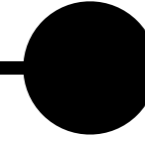
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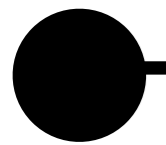
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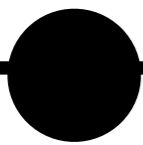
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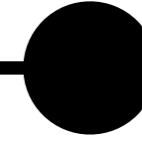


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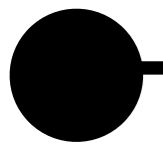
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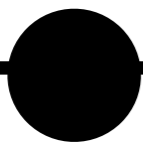
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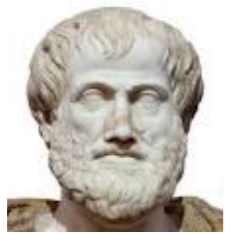
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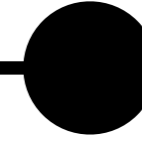


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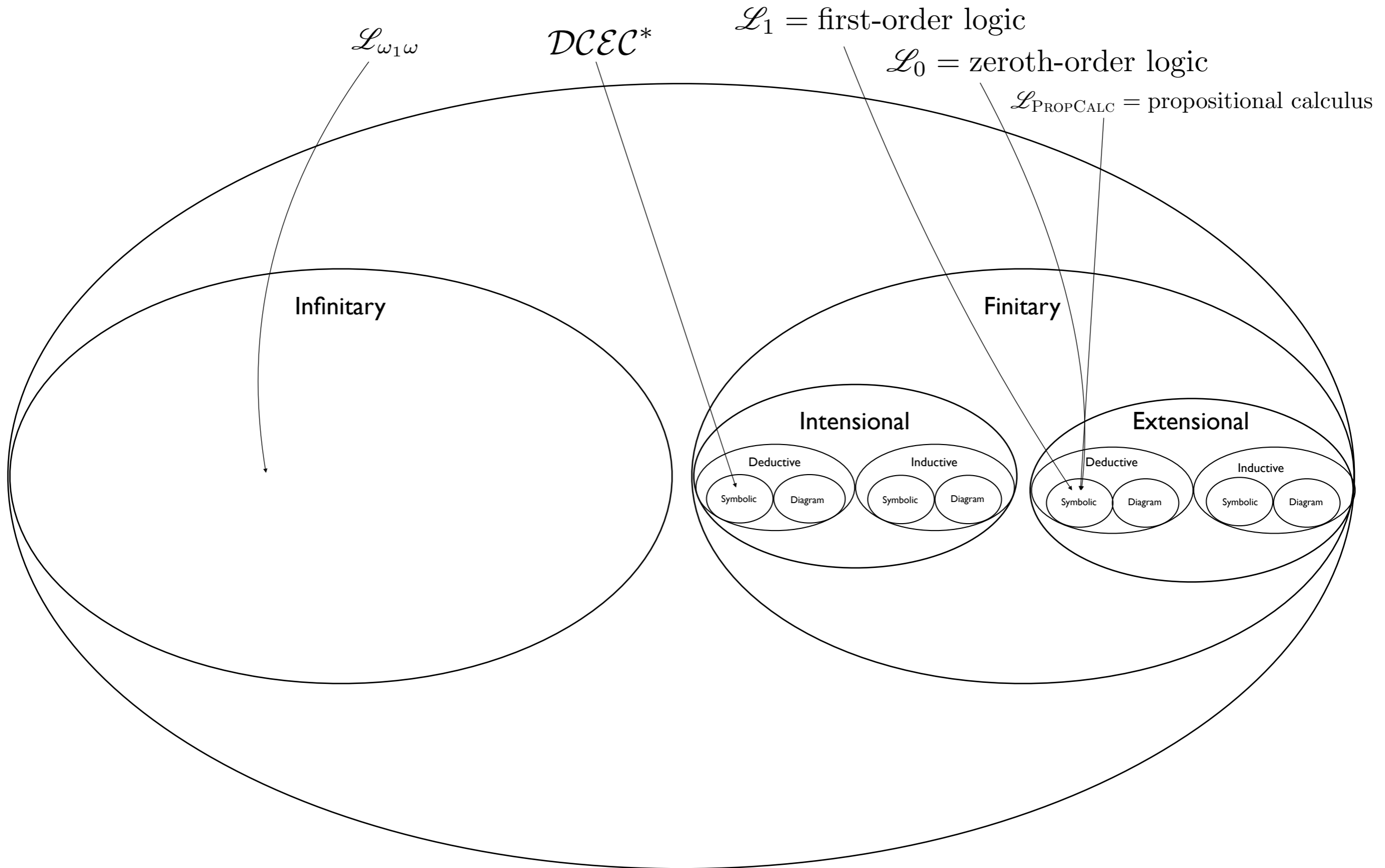
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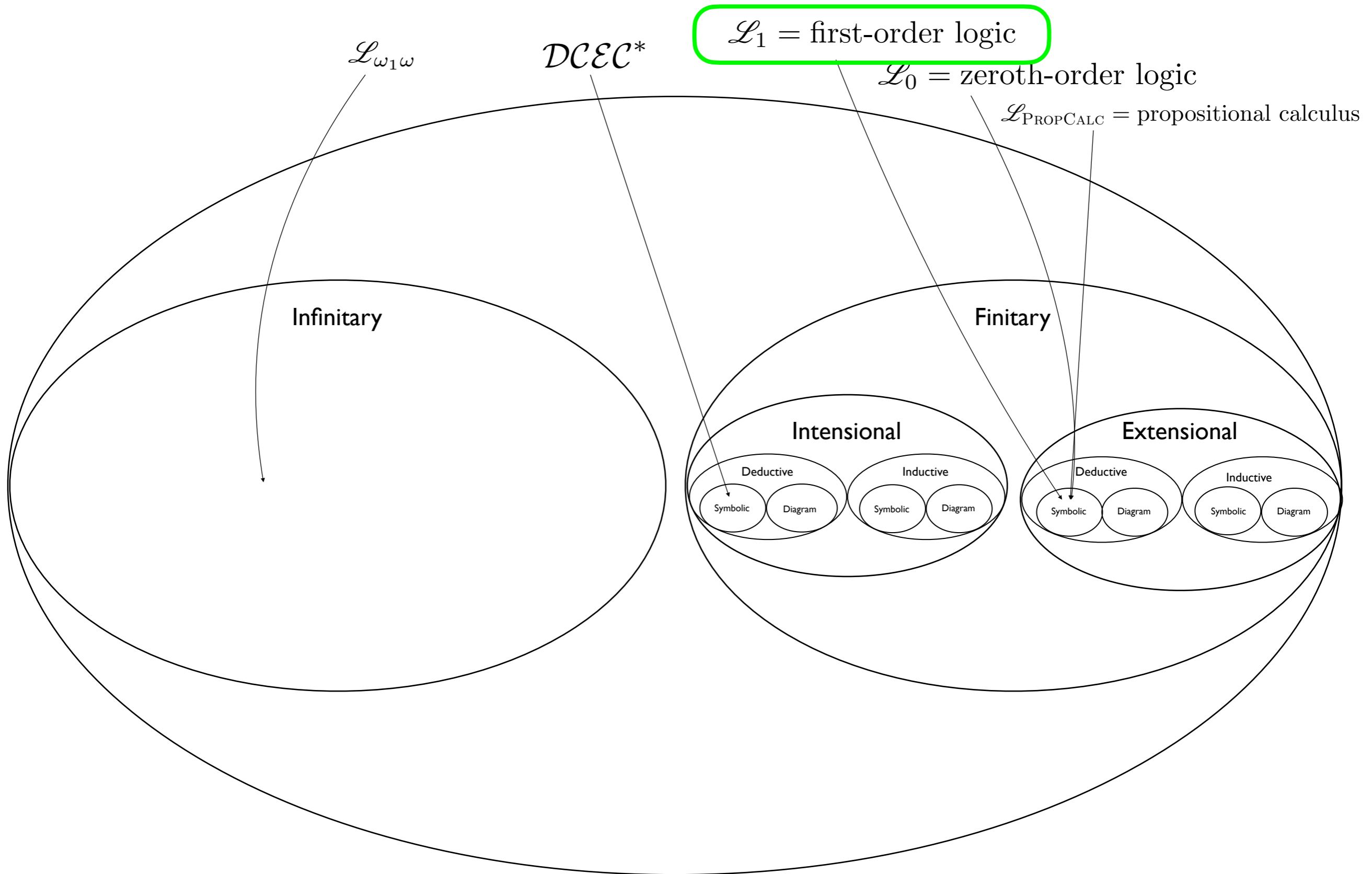


2020

# The Universe of Logics



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$\mathcal{L}_3 + \text{modal logic S5}$

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# First Two New (Easy!!) Inference Rules in FOL

## ● universal elimination

### ● If everything is an $D$ , then the particular

<b>A1</b> Either a property or its negation is positive, but not both:	$\forall\phi[P(\neg\phi) \leftrightarrow \neg P(\phi)]$
<b>A2</b> A property necessarily implied by a positive property is positive:	$\forall\phi\forall\psi[(P(\phi) \wedge \Box\forall x[\phi(x) \rightarrow \psi(x)]) \rightarrow P(\psi)]$
<b>T1</b> Positive properties are possibly exemplified:	$\forall\phi[P(\phi) \rightarrow \Diamond\exists x\phi(x)]$
<b>D1</b> A <i>God-like</i> being possesses all positive properties:	$G(x) \leftrightarrow \forall\phi[P(\phi) \rightarrow \phi(x)]$
<b>A3</b> The property of being God-like is positive:	$P(G)$
<b>C</b> Possibly, God exists:	$\Diamond\exists xG(x)$
<b>A4</b> Positive properties are necessarily positive:	$\forall\phi[P(\phi) \rightarrow \Box P(\phi)]$
<b>D2</b> An <i>essence</i> of an individual is a property possessed by it and necessarily implying any of its properties:	$\phi \text{ ess. } x \leftrightarrow \phi(x) \wedge \forall\psi(\psi(x) \rightarrow \Box\forall y(\phi(y) \rightarrow \psi(y)))$
<b>T2</b> Being God-like is an essence of any God-like being:	$\forall x[G(x) \rightarrow G \text{ ess. } x]$
<b>D3</b> <i>Necessary existence</i> of an individual is the necessary exemplification of all its essences:	$NE(x) \leftrightarrow \forall\phi[\phi \text{ ess. } x \rightarrow \Box\exists y\phi(y)]$
<b>A5</b> Necessary existence is a positive property:	$P(NE)$
<b>T3</b> Necessarily, God exists:	$\Box\exists xG(x)$

Scott's Version of Gödel's Proof, Verified by AI

$\mathcal{L}_3 + \text{modal logic S5}$

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## Facts and Possibilities: A Model-Based Theory of Sentential Reasoning

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### Abstract

This article presents a fundamental advance in the theory of mental models as an explanation of reasoning about facts, possibilities, and probabilities. It postulates that the meanings of compound assertions, such as conditionals (*if*) and disjunctions (*or*), unlike those in logic, refer to conjunctions of epistemic possibilities that hold in default of information to the contrary. Various factors such as general knowledge can modulate these interpretations. New information can always override sentential inferences; that is, reasoning in daily life is defeasible (or nonmonotonic). The theory is a dual process one: It distinguishes between intuitive inferences (based on system 1) and deliberative inferences (based on system 2). The article describes a computer implementation of the theory, including its two systems of reasoning, and it shows how the program simulates crucial predictions that evidence corroborates. It concludes with a discussion of how the theory contrasts with those based on logic or on probabilities.

*Keywords:* Deduction; Logic; Mental models; Nonmonotonicity; Reasoning; Possibility

### 1. Introduction

People reason about facts, possibilities, and probabilities. Psychologists have carried out many studies of factual inferences, such as:

1. If the card is an ace then it is a heart.  
The card is an ace.  
Therefore, the card is a heart.

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seem true a priori and those that are contingent is “an unempirical dogma of empiricism.” Not anymore. The empirical studies we have described show that individuals innocent of philosophical niceties judged that assertions can be true (or false) a priori as a result of their meaning.

In logic, if a material conditional is false then its *if*-clause is true. So a very short proof for the existence of God is sound in logic:

38. It is not the case that if God exists then atheism is correct.  
Therefore, God exists.

Its premise is true, and it implies both that God exists and that atheism is not correct. It therefore follows from this conjunction that God exists. In the model theory, a conditional’s meaning is not a material implication, not a conditional probability, not a set of possible worlds, and not an inferential relation. It is instead a conjunction of possibilities, each of which is assumed in default of information to the contrary. And so the falsity of a conditional does not imply that its *if*-clause is true, which renders the “proof” in (38) invalid. Individuals judge that the following assertion is false:

39. If Sonia has pneumonia then she is healthy.

But its falsity does not imply that Sonia has pneumonia, and indeed individuals judge that it is possible that Sonia does not have pneumonia (Quelhas et al., 2016). Only one case is impossible:

Sonia has pneumonia   Sonia is healthy

That is why (39) is false. The modulation algorithm we described mirrors these evaluations.

Yet a complex sort of modulation is at present beyond the program. As Byrne (1989) showed, individuals draw their own conclusion from premises, such as:

42. If she meets her friend then she will go to a play.  
She meets her friend.

They infer that she will go to a play. But when the premises have a further conditional of the following sort added to them:

41. If she has enough money then she will go to a play.

reasoners tend not to make the inference (see also Byrne, Espino, & Santamaria, 1999). The additional premise reminds them of a necessary condition for going to a play: One needs money to pay for the tickets. But no premise has established this condition, and so they balk at the inference. The inference is complex, and the modulation algorithm has yet to capture it.



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Part I: *Slutten* — *for i dag.*

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Part II: Hands-on Q&A & Review ...



*Den rasjonelle delen av  
menneskesinnet er  
basert på logikk.*